INSTRUCTIONS TO CANDIDATES

• Note that ALL QUESTIONS ARE COMPULSORY.

• DIFFERENT QUESTIONS MAY HAVE DIFFERENT NUMBERS OF TOTAL MARKS. Take note of this in allocating time to questions.

• WRITE YOUR ANSWERS ON THE EXAM PAPER ITSELF. Write as legibly as possible.

• In the answer to any part of any question, you may use any function specified in an earlier part of that question. You may do this whether or not you actually provided a definition for the earlier part; nor will you be penalized in a later part if your answer to an earlier part is incorrect.

• Unless otherwise stated, you may use any function from the standard prelude, including the libraries Char, List, and Maybe. You need not write import declarations.

• As an aid to memory, some functions from the standard prelude that you may wish to use are listed on the next page. You need not use all the functions.

PLEASE INSERT YOUR NAME AND MATRICULATION NUMBER IN THE SPACE BELOW:
Figure 1: Basic functions

\[
\begin{align*}
&\text{div, mod :: } \text{Integral } a \Rightarrow a \rightarrow a \\
&(+), (*), (-), (/) :: \text{Num } a \Rightarrow a \rightarrow a \rightarrow a \\
&(<), (\le), (>), (\ge) :: \text{Ord } a \Rightarrow a \rightarrow a \rightarrow \text{Bool} \\
&(=), (/=) :: \text{Eq } a \Rightarrow a \rightarrow a \rightarrow \text{Bool} \\
&(&&), (||) :: \text{Bool} \rightarrow \text{Bool} \rightarrow \text{Bool} \\
&\text{not :: Bool } \rightarrow \text{Bool} \\
&\text{max, min :: Ord } a \Rightarrow a \rightarrow a \rightarrow a \\
&\text{isAlpha, isLower, isUpper, isDigit :: Char } \rightarrow \text{Bool} \\
&\text{toLower, toUpper :: Char } \rightarrow \text{Char}
\end{align*}
\]

\[
\begin{align*}
&\text{Figure 2: Library functions}
\end{align*}
\]

\[
\begin{align*}
&\text{sum, product :: (Num a) } \Rightarrow [a] \rightarrow a \\
&\text{and, or :: [Bool] } \rightarrow \text{Bool} \\
&\text{sum } [1.0,2.0,3.0] = 6.0 \\
&\text{and [True,False,True] = False} \\
&\text{product } [1,2,3,4] = 24 \\
&\text{or [True,False,True] = True} \\
&\text{maximum, minimum :: (Ord a) } \Rightarrow [a] \rightarrow a \\
&\text{reverse :: [a] } \rightarrow [a] \\
&\text{maximum } [3,1,4,2] = 4 \\
&\text{reverse } "\text{goodbye}" = "\text{eybdoog}" \\
&\text{minimum } [3,1,4,2] = 1 \\
&\text{concat :: [[a]] } \rightarrow [a] \\
&\text{concat } ["\text{go"},"\text{od"},"\text{bye"}] = "\text{goodbye}" \\
&\text{"\text{good" } ++ "\text{bye" } = "\text{goodbye"} \\
&\text{(!!) :: [a] } \rightarrow \text{Int} \rightarrow a \\
&\text{length :: [a] } \rightarrow \text{Int} \\
&\text{[9,7,5] !! 1 = 7} \\
&\text{length } [9,7,5] = 3 \\
&\text{head :: [a] } \rightarrow a \\
&\text{tail :: [a] } \rightarrow [a] \\
&\text{head } "\text{goodbye" } = 'g' \\
&\text{tail } "\text{goodbye" } = "\text{oodbye}" \\
&\text{init :: [a] } \rightarrow [a] \\
&\text{last :: [a] } \rightarrow a \\
&\text{init } "\text{goodbye" } = "\text{goodby}" \\
&\text{last } "\text{goodbye" } = 'e' \\
&\text{take :: Int } \rightarrow [a] \rightarrow [a] \\
&\text{drop :: Int } \rightarrow [a] \rightarrow [a] \\
&\text{take } 4 "\text{goodbye" } = "\text{good"} \\
&\text{drop } 4 "\text{goodbye" } = "\text{bye"} \\
&\text{takeWhile :: (a->Bool) } \rightarrow [a] \rightarrow [a] \\
&\text{dropWhile :: (a->Bool) } \rightarrow [a] \rightarrow [a] \\
&\text{takeWhile } \text{isLower } "\text{goodBye" } = "\text{good"} \\
&\text{dropWhile } \text{isLower } "\text{goodBye" } = "\text{Bye"} \\
&\text{elem :: (Eq a) } \Rightarrow a \rightarrow [a] \rightarrow \text{Bool} \\
&\text{replicate :: Int } \rightarrow a \rightarrow [a] \\
&\text{elem } 'd' "\text{goodbye" } = \text{True} \\
&\text{replicate } 5 'a' = "\text{*****"} \\
&\text{zip :: [a} \rightarrow [b] \rightarrow [(a,b)] \\
&\text{zip } [1,2,3,4] [1,4,9] = [(1,1),(2,4),(3,9)]
\end{align*}
\]
1. (a) Write a function \( f :: \text{Char} \rightarrow \text{Int} \) that converts a character to its score. Each letter starts with a score of one; one is added to the score of a character if it is a vowel (a, e, i, o, u) and one is added to the score of a character if it is upper case; a character that is not a letter scores zero. For example,

\[
\begin{align*}
  f \ 'A' &= 3 \\
  f \ 'B' &= 2 \\
  f \ 'a' &= 2 \\
  f \ 'b' &= 1 \\
  f \ '.', &= 0
\end{align*}
\]

(b) Using \( f \), define a function \( g :: \text{String} \rightarrow \text{Int} \) that given a string returns the product of the score of every letter in the string, ignoring any character that is not a letter. For example, \( g \ "aBc4E" \) returns 12. Your definition may use basic functions, list comprehension, and library functions, but not recursion.

(c) Again using \( f \), define a function, \( h :: \text{String} \rightarrow \text{Int} \) that behaves identically to \( g \), this time using basic functions and recursion, but not list comprehension or library functions.
2. (a) Write a function \( c :: \text{String} \rightarrow \text{String} \) that takes a list of characters and returns a list where each character is repeated a number of times corresponding to its position in the list: the first character appears once, the second twice, and so on. For example, \( c \ "abcd" \) returns "\text{abcccdddd}". Your definition may use basic functions, \textit{list comprehension}, and \textit{library functions}, but not recursion.

\[ 6 \text{ marks} \]

(b) Define a second function, \( d :: \text{String} \rightarrow \text{String} \) that behaves identically to \( c \), this time using basic functions, the library function append (\( ++ \)), and \textit{recursion}, but not list comprehension or other library functions. You may wish to define an auxiliary recursive function, which may behave in the same way as a library function.

\[ 9 \text{ marks} \]

(c) Write a QuickCheck property \( \text{prop\_cd} \) to confirm that \( c \) and \( d \) behave identically. Give the type signature of \( \text{prop\_cd} \) and its definition.

\[ 2 \text{ marks} \]