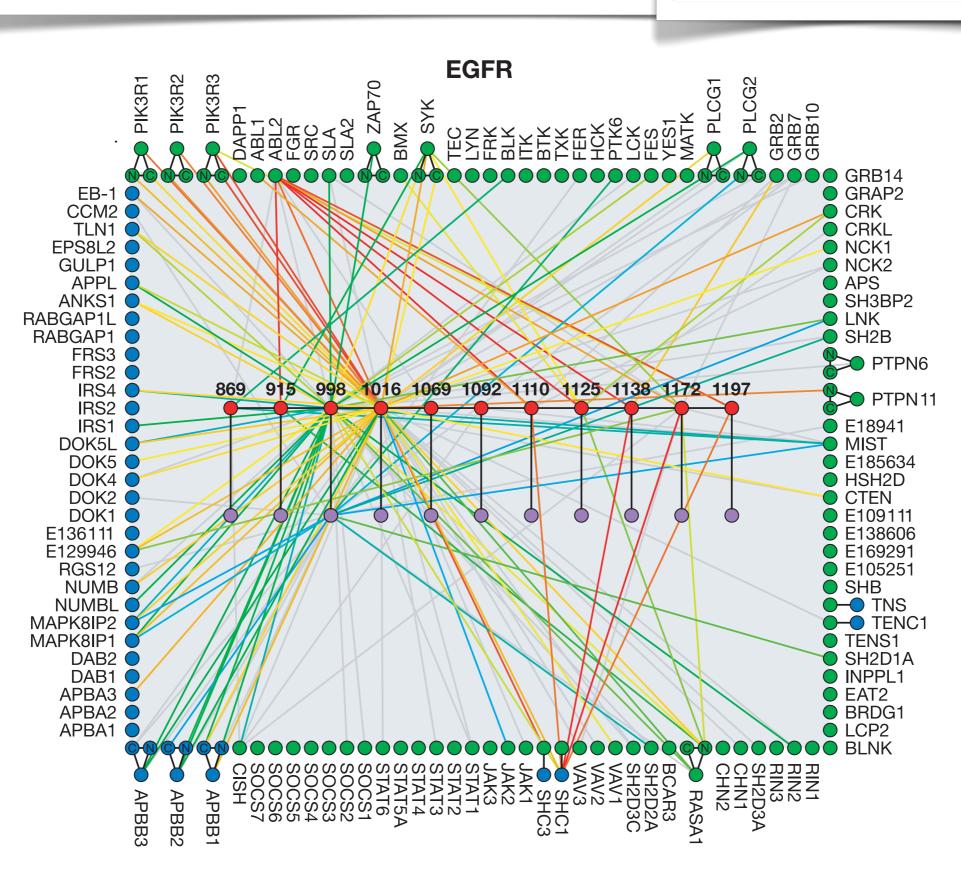
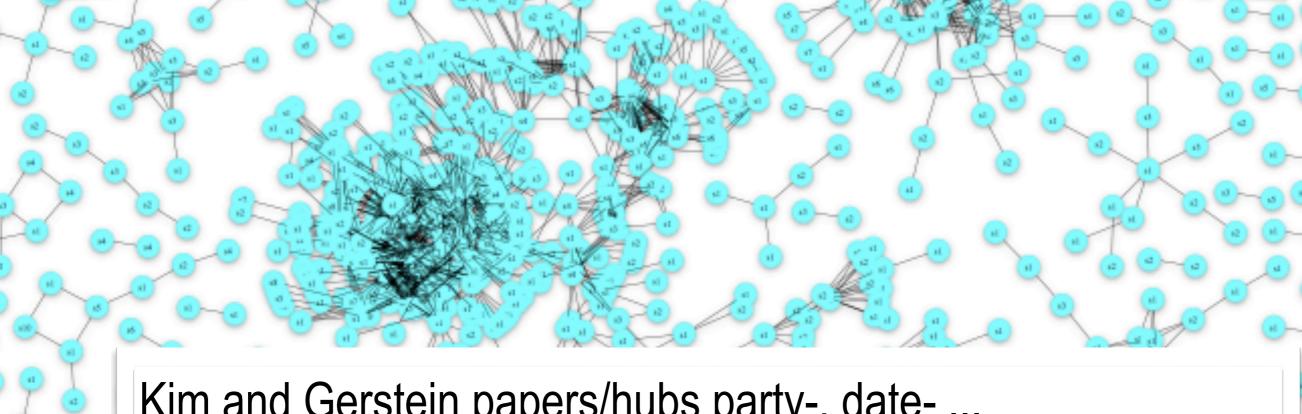
domains, sites, s

binding takes center stage



domains (cont')

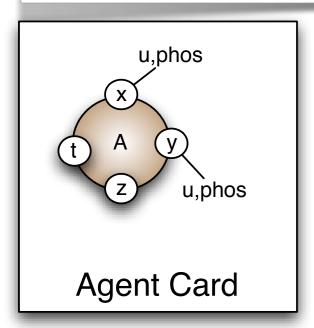


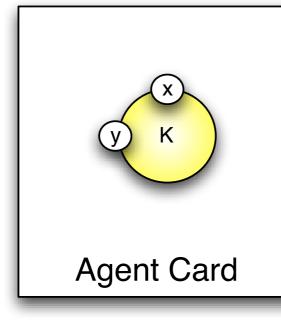
Kim and Gerstein papers/hubs party-, date- ...

what are the forces driving this mass action graph rewriting?

- randomness
 - causalities/conditional binding
 - geometric hindrance/structural biology

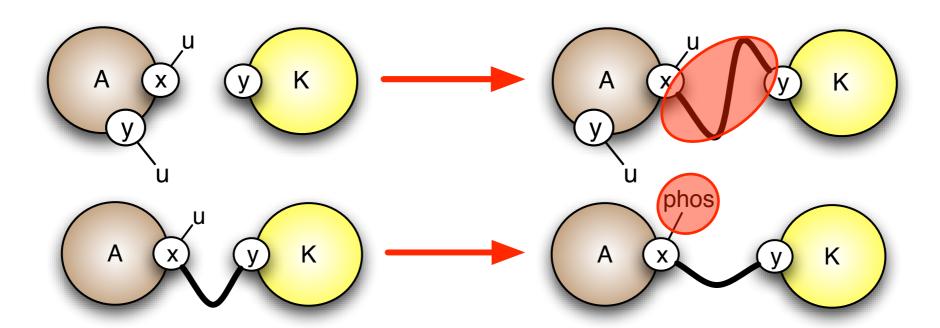
agents and rules





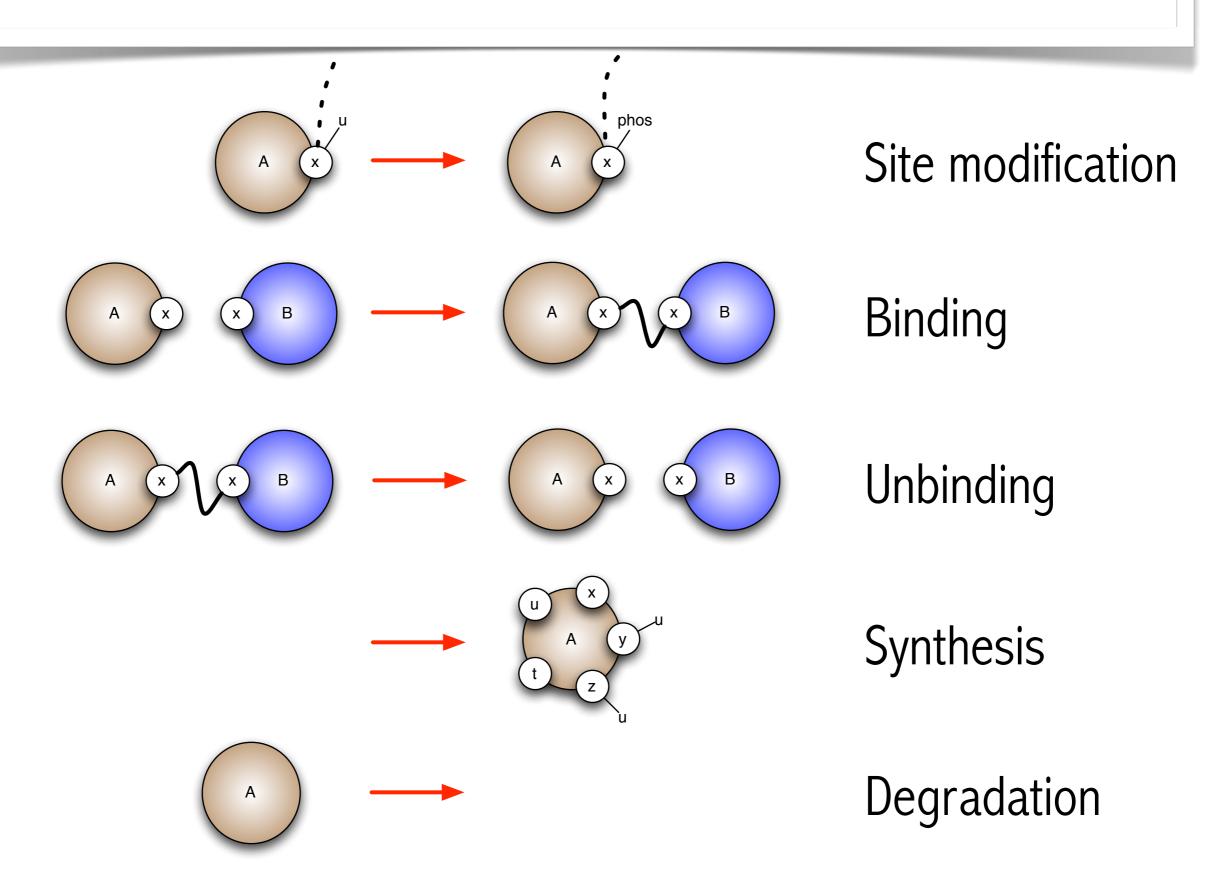
Protein A is activated by kinase K on site x.

Phosphorylated site y prevents kinase to activate x

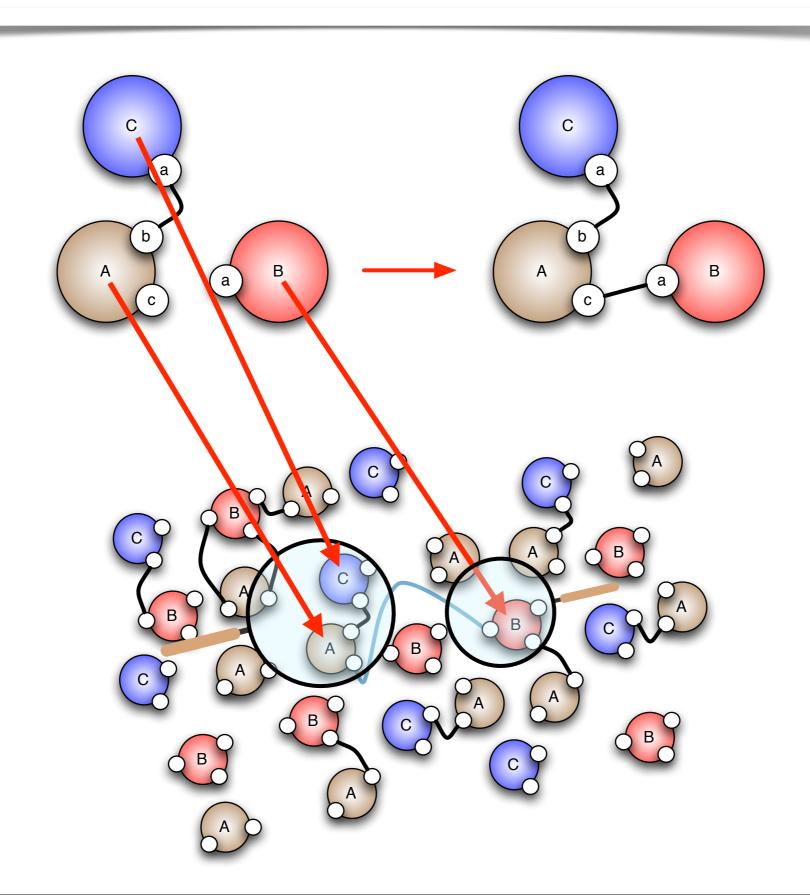


lhs=subgraph (don't care don't write)

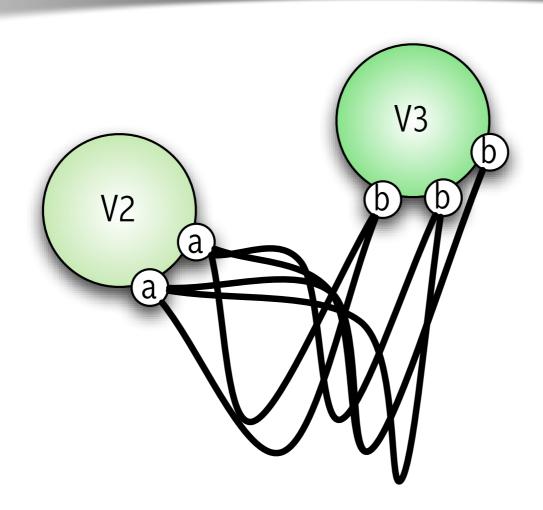
actions



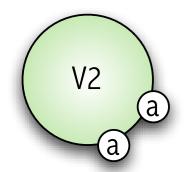
event:=rule application

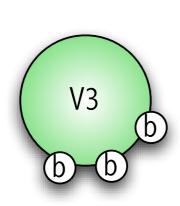


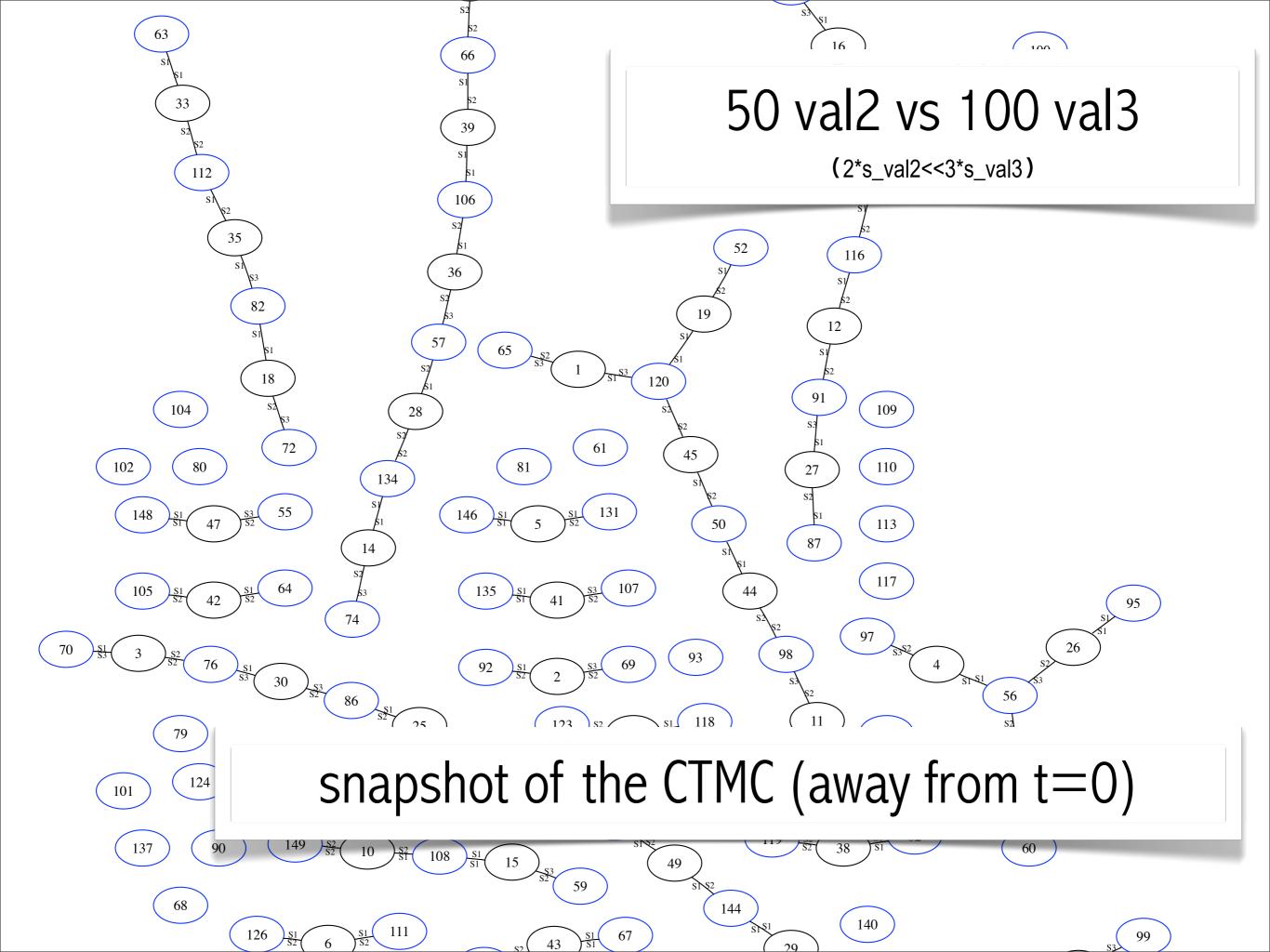
a simple mag with dim= ∞

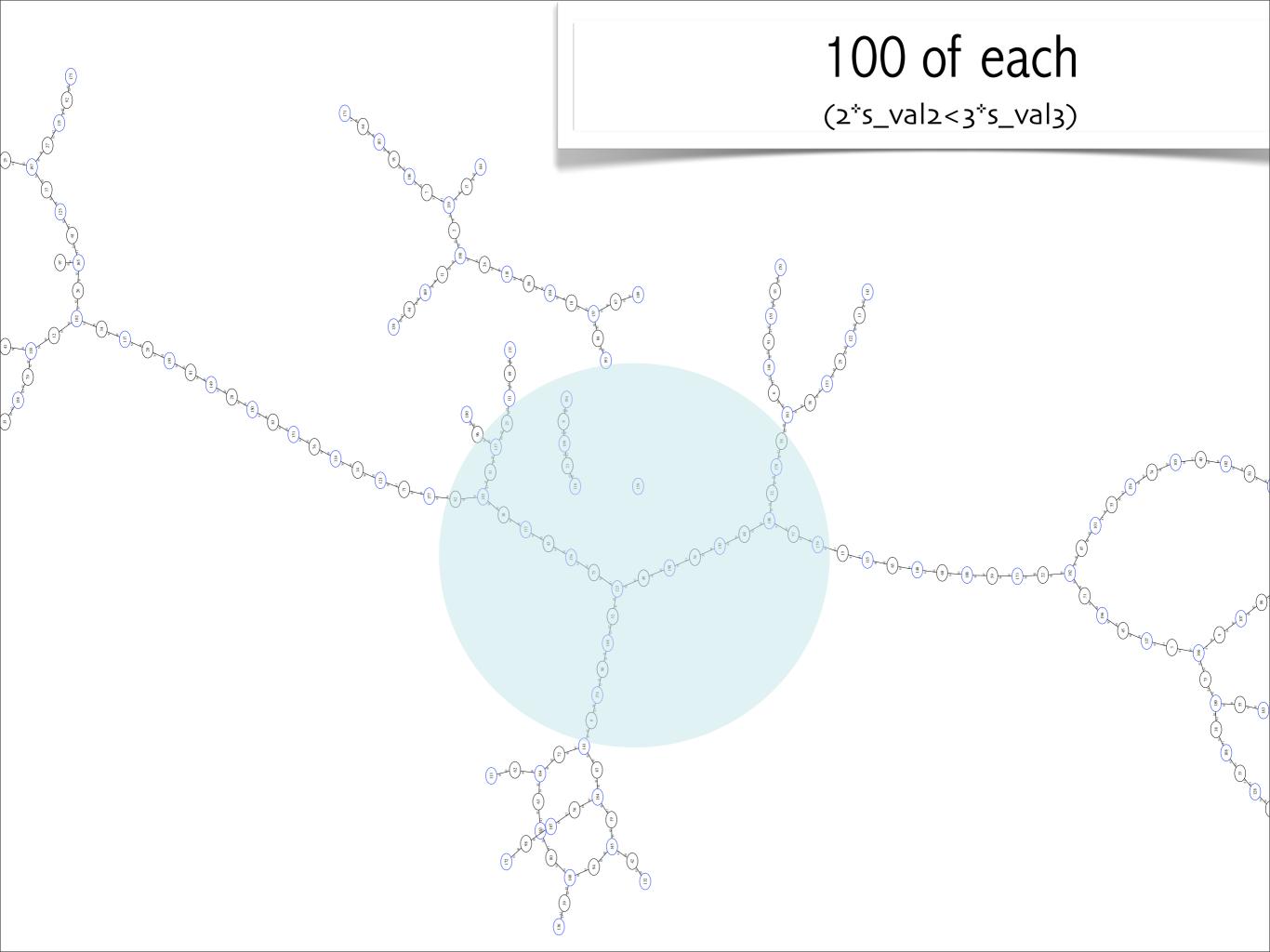


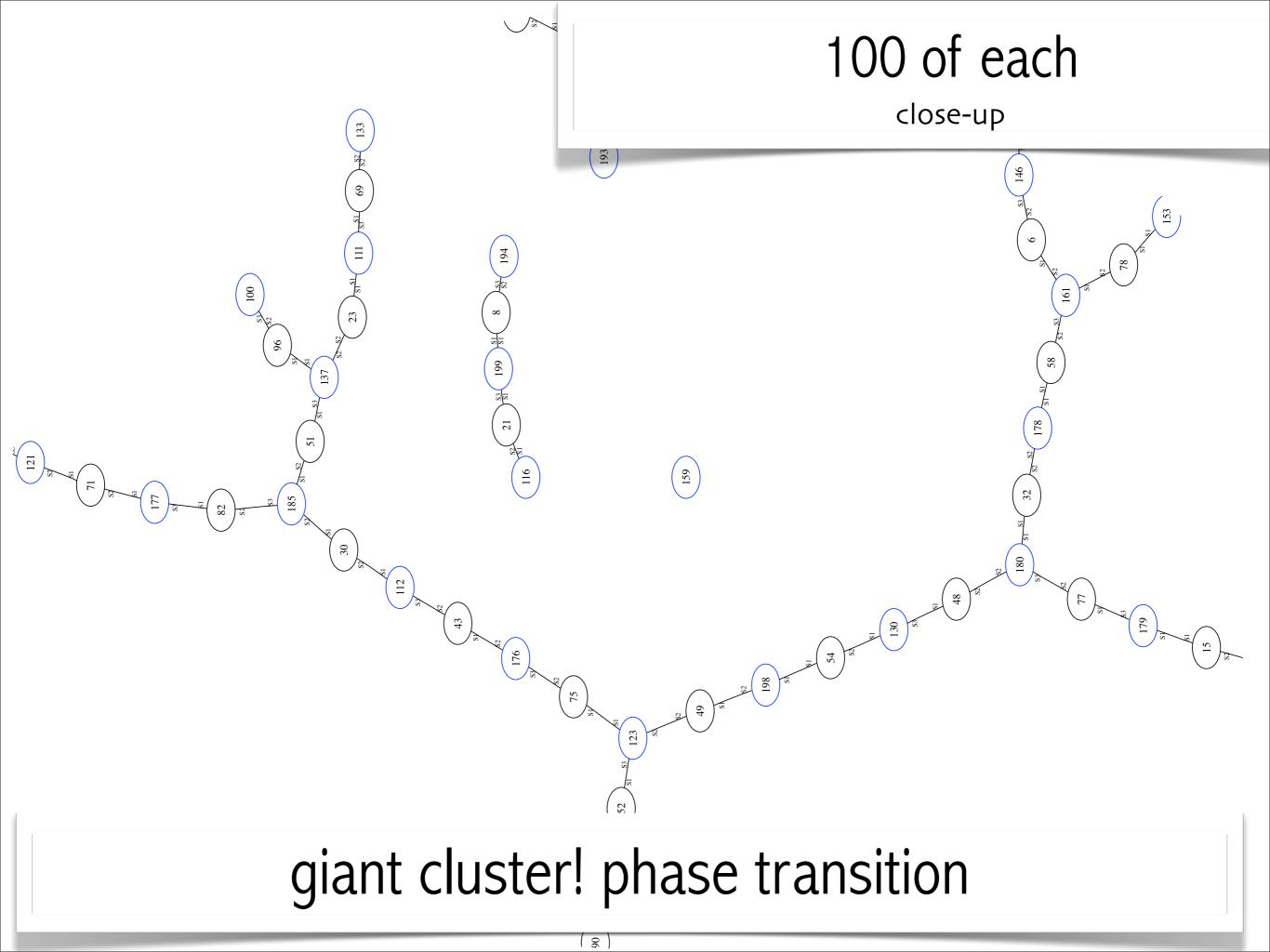
One ab binding rule with low dissociation T (viscous)

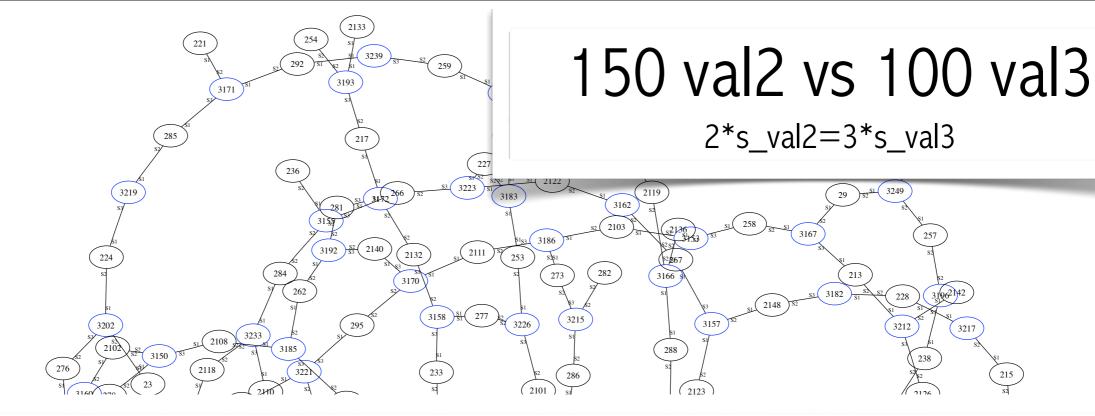








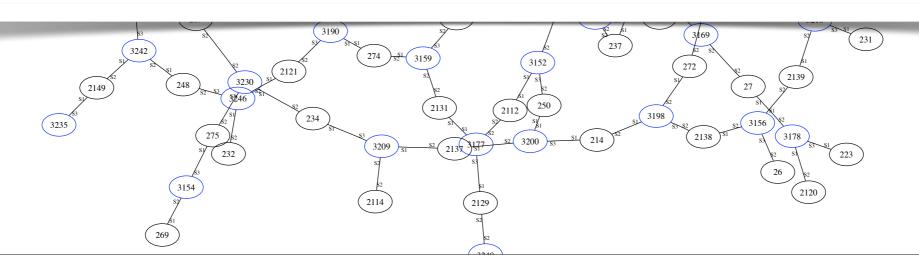




criticality happens easily and early (not just at ∞ !)

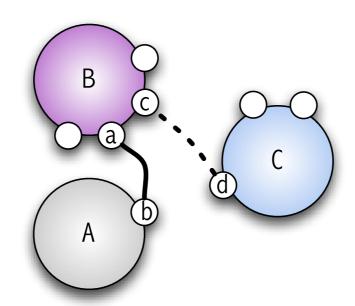
sensitive to T structure = dissociation rate

sensitive to E structure := local stub correlations



liquidity index

the dRG model

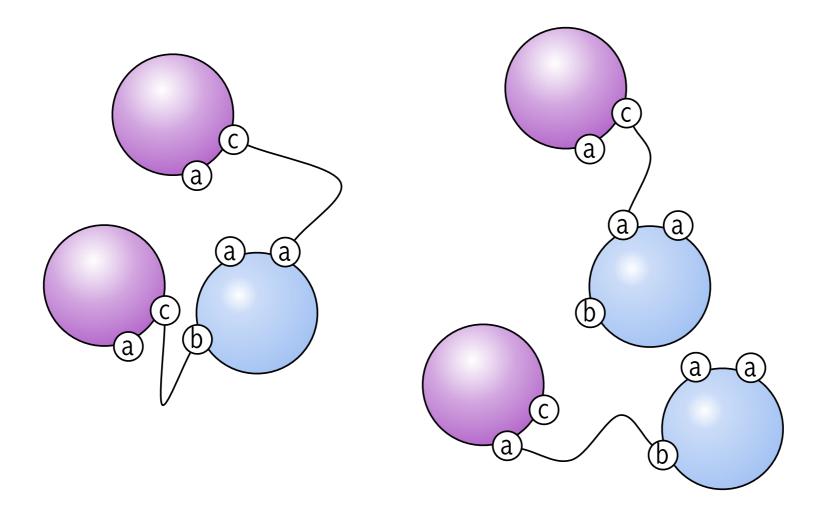


A random graph with sites consists of the following data:

- n the set of nodes
- K the (finite) set of colours
- Z the node random variable with values in \mathbb{N}^K
- for each $a, b \in K$ a dissociation constant $\Gamma_{ab} \in [0, \infty]$

the dRG model II

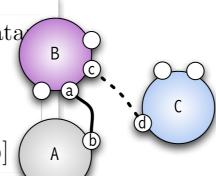
- [binding] two free sites x, y of respective colours a, b bind each other with a probability proportional to γ_{ab}^+ ;
- [unbinding] two sites x, y of respective colours a, b, and already bound together, unbind with a probability proportional to γ_{ab}^- .



the dRG model steady state

A random graph with sites consists of the following data

- n the set of nodes
- K the (finite) set of colours
- Z the node random variable with values in \mathbb{N}^K
- for each $a, b \in K$ a dissociation constant $\Gamma_{ab} \in [0, \infty]$



$$n_a = n_a^f + \sum_b e_{ab}$$
$$\Gamma_{ab}e_{ab} = n_a^f n_b^f$$

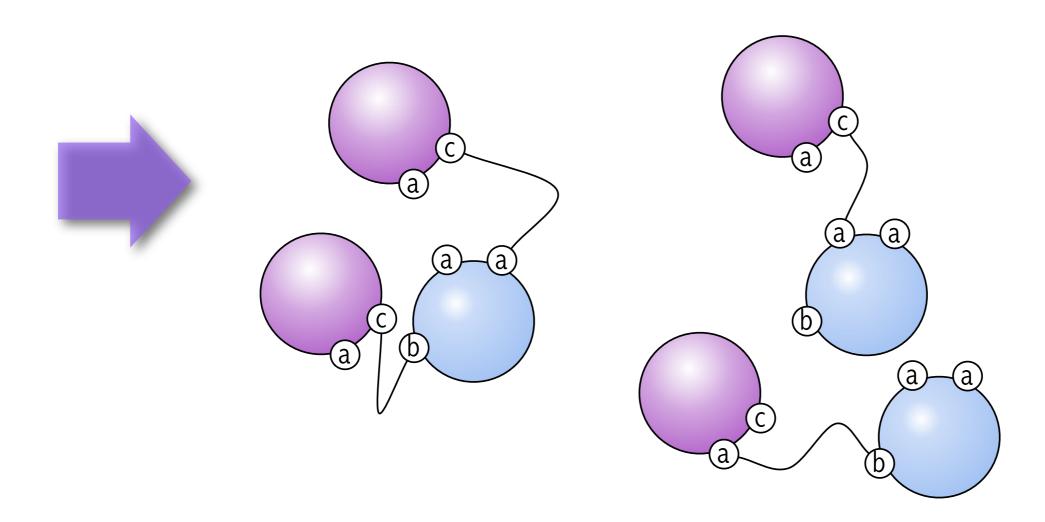
steady state equation is node independent (E structure), scale-less too!

$$\Gamma_{ab} \cdot e_{ab} = (n_a - \sum_c e_{ac})(n_b - \sum_d e_{db})$$

$$K_{ab}\epsilon_{ab} = (\langle m_a \rangle - \sum_c \epsilon_{ac})(\langle m_b \rangle - \sum_d \epsilon_{bd})$$

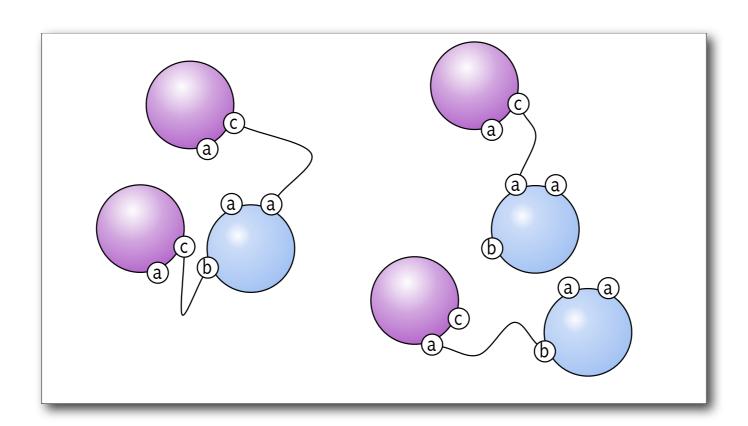
an sRG model -after Soderberg Act. Phys. Polonica (2003)

- n the set of nodes
- K the set of colours together with * a special value not in K
- Z the node random variable with values in \mathbb{N}^K
- for each $a \in K$, Y_a the edge random variable with values in $K + \{*\}$



from dRG to sRG

limit distribution of dRG gives Y_a/T_{ab} as a function of e_{ab}



$$p(Y_a = b) := \epsilon_{ab} / \langle m_a \rangle$$

$$T_{ab} := \epsilon_{ab}/\langle m_a \rangle \langle m_b \rangle$$

size and gf-ology

$$|\epsilon_{ab}/\langle m_a \rangle \cdot m_b p_m/\langle m_b \rangle$$

$$T_{ab}m_bp_m$$

$$S_p^a(z) := \sum_n p(S_p^a = n) z^n$$

 $Z(x_c; c \in K) := \sum_{m \in \mathbb{N}^K} p(Z = m) \prod_{c \in K} x_c^{m_c}$

inductive size gf

$$S_{p}^{a}(z) - p(Y^{a} = *)$$

$$= z \sum_{n>0} p(S_{p}^{a} = n) z^{n-1}$$

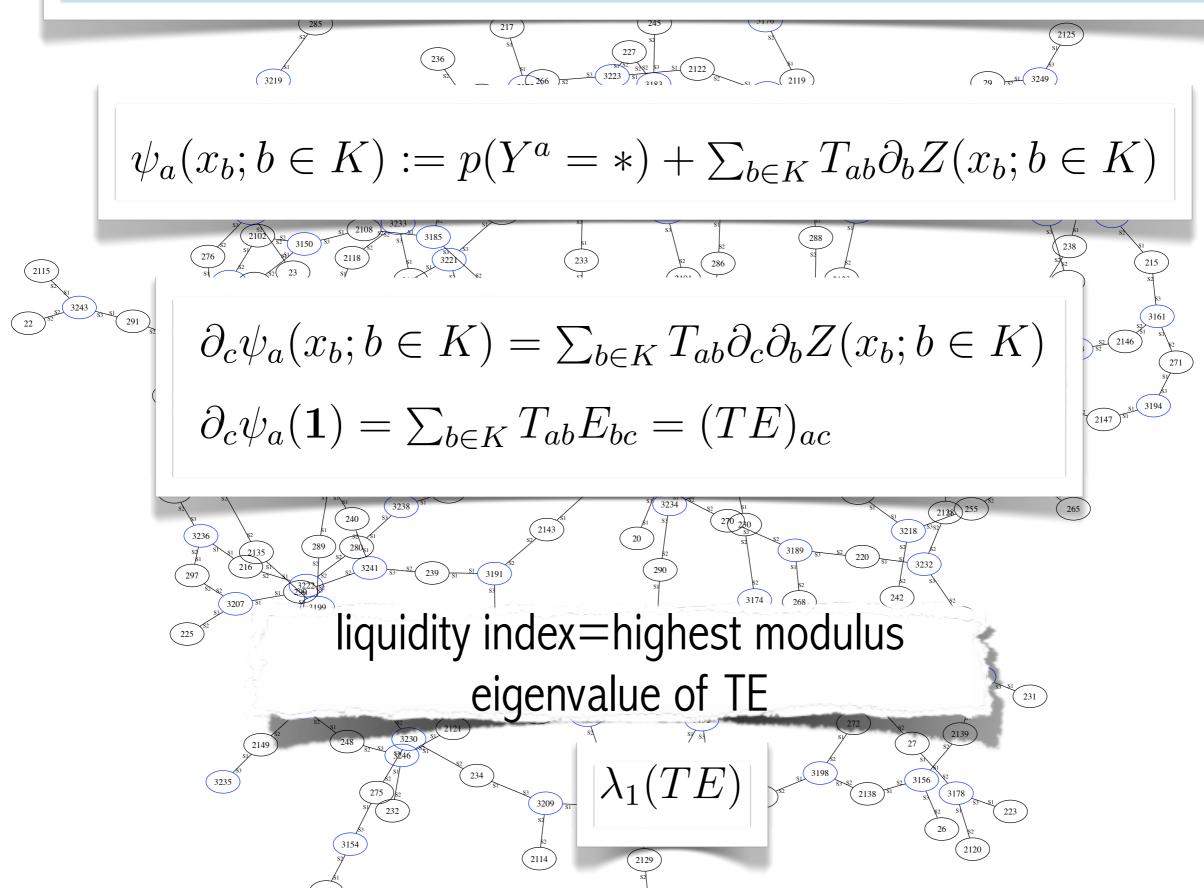
$$= z \sum_{n>0,m} \sum_{b \in K} T_{ab} m_{b} p_{m} p(\sum_{c \in m-b} S_{p-1}^{c} = n-1) z^{n-1}$$

$$= z \sum_{b \in K} T_{ab} \sum_{m} m_{b} p_{m} (\sum_{n>0} p(\sum_{c \in m-b} S_{p-1}^{c} = n-1) z^{n-1})$$

$$= z \sum_{b \in K} T_{ab} \sum_{m} m_{b} p_{m} \prod_{c \in m-b} S_{p-1}^{c}(z)$$

$$= z \sum_{b \in K} T_{ab} \partial_{b} Z(S_{p-1}^{c}(z); c \in K)$$

liquidity index



a2ba1 b1 b2 ab ab b1 b1

bicolor case

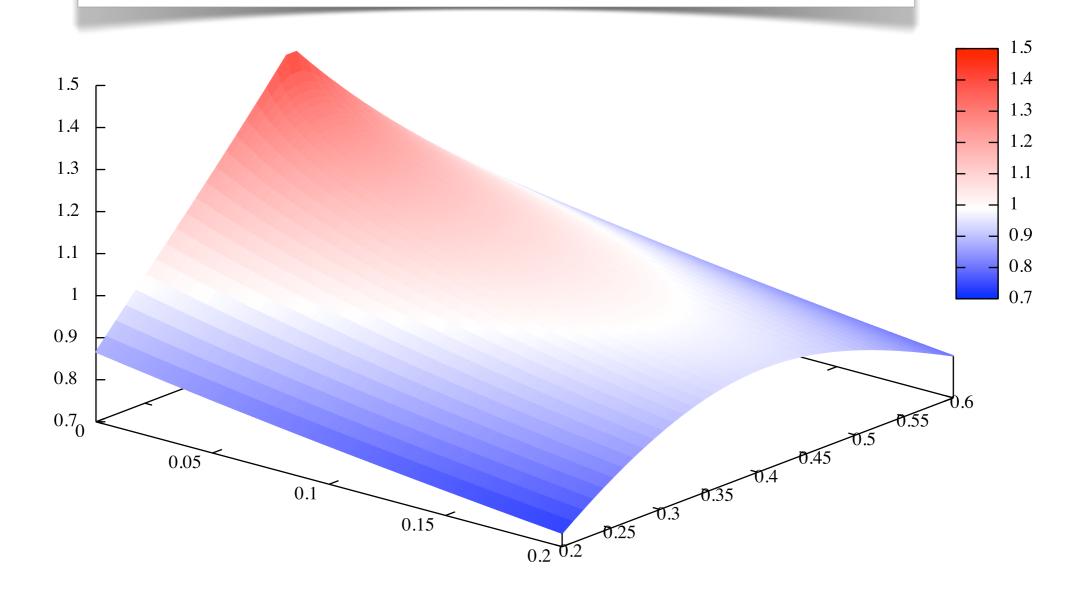
$$N := \frac{\langle m_a m_b \rangle + \sqrt{\langle m_a (m_a - 1) \rangle \langle m_b (m_b - 1) \rangle}}{\langle m_a \rangle \langle m_b \rangle}$$

$$\epsilon := \frac{\langle m_a \rangle + \langle m_b \rangle + K - \sqrt{(\langle m_a \rangle + \langle m_b \rangle + K)^2 - 4\langle m_a \rangle \langle m_b \rangle}}{2}$$

2a vs. 3b

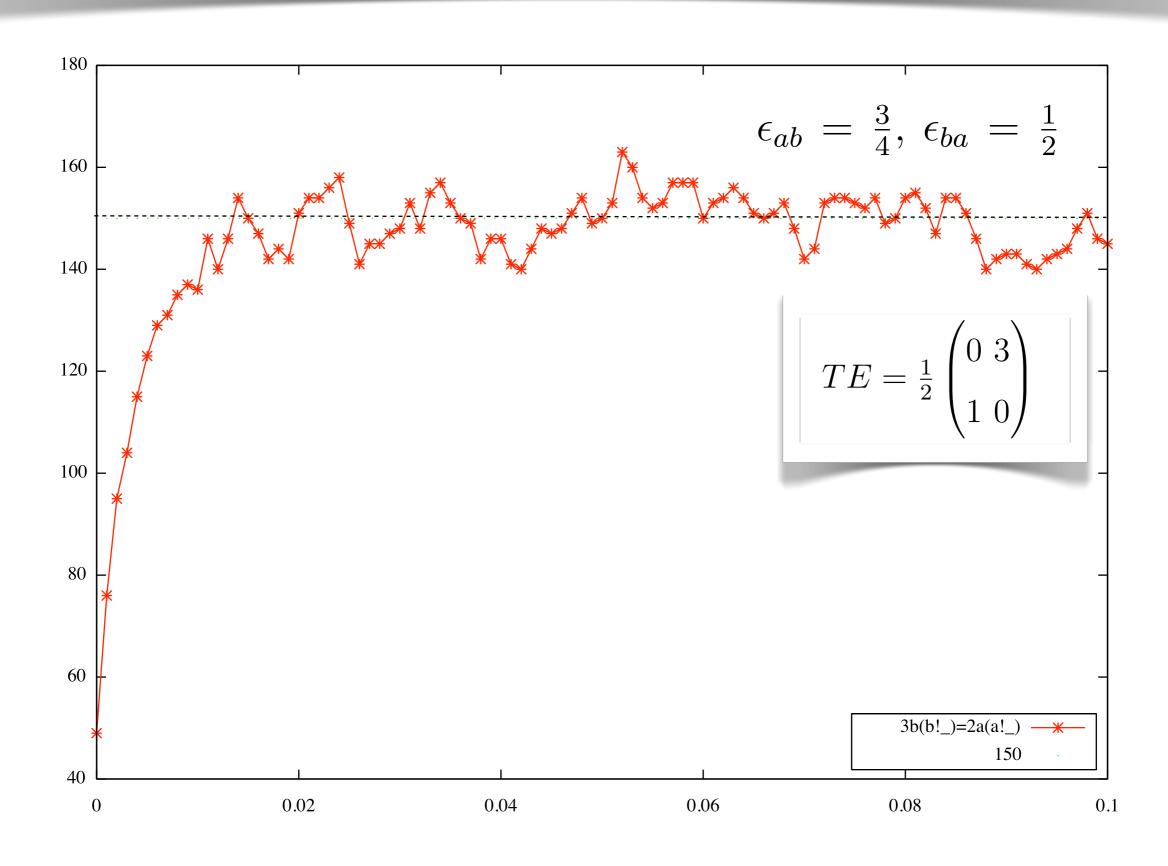
p = proportion of 3b

$$\lambda(p,K) := \frac{2 + p + K - \sqrt{(2 + p + K)^2 - 24p(1 - p)}}{2\sqrt{3p(1 - p)}}$$

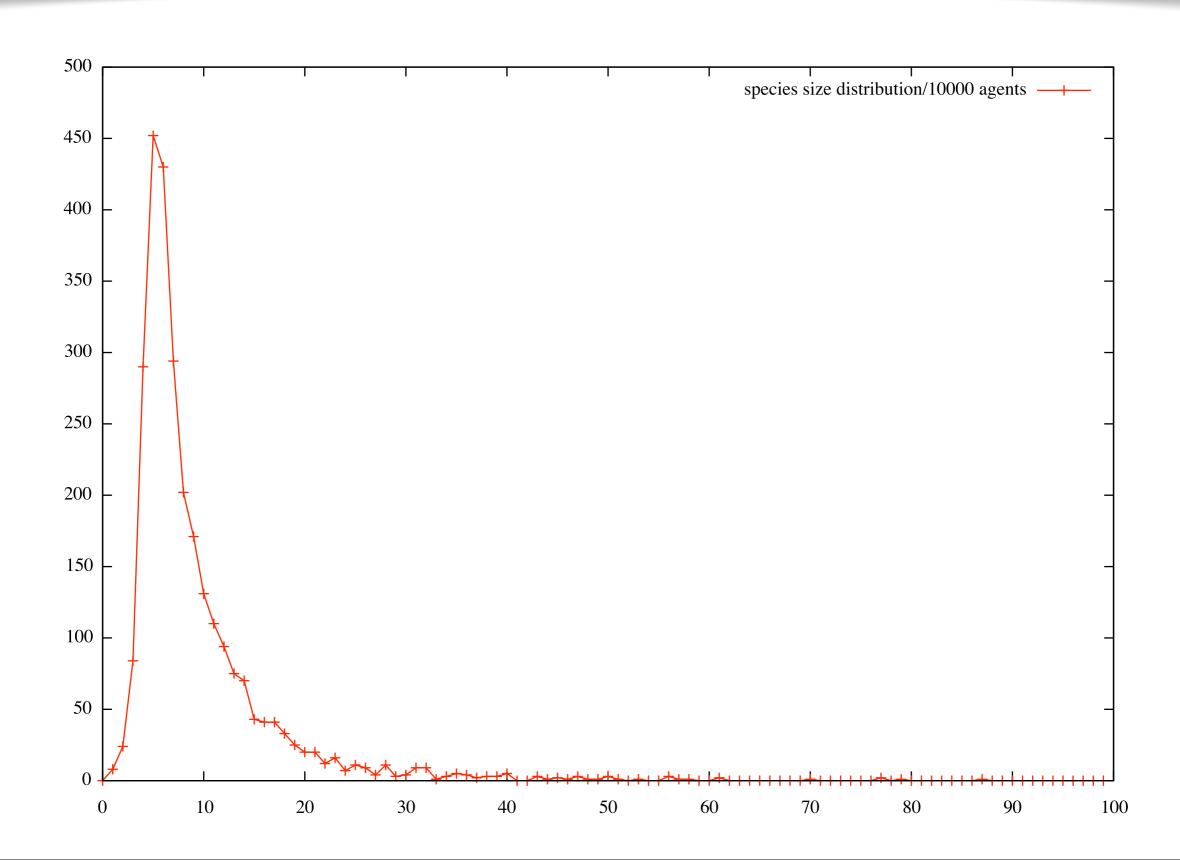


simulations

n=200, $K_{ab=1/4}$,

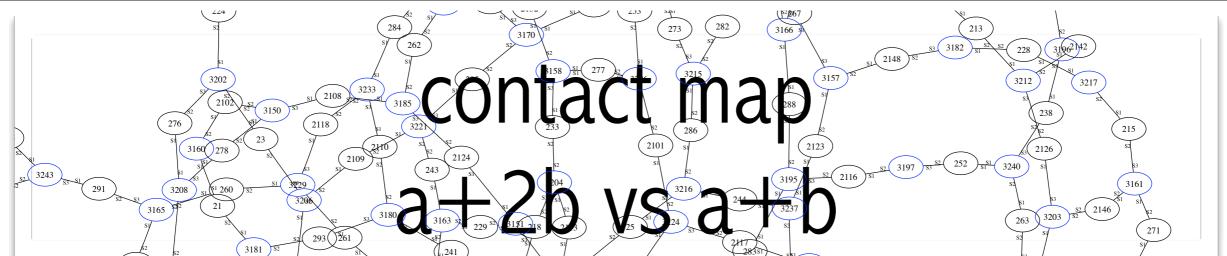


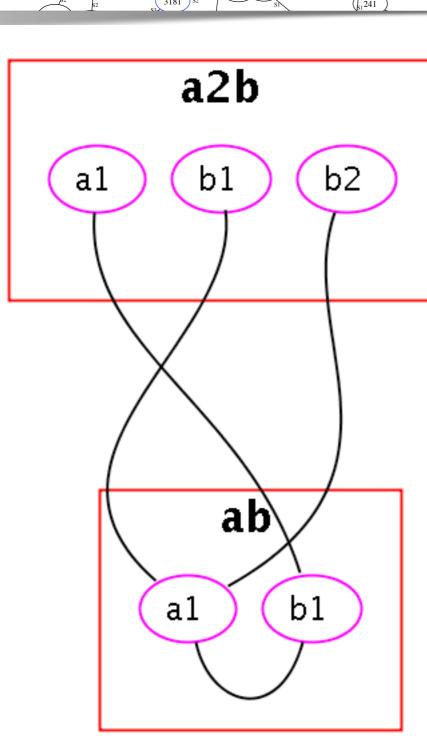
n=1000 size distribution



$n = 0.2 \ 10^6 - \text{max size}$

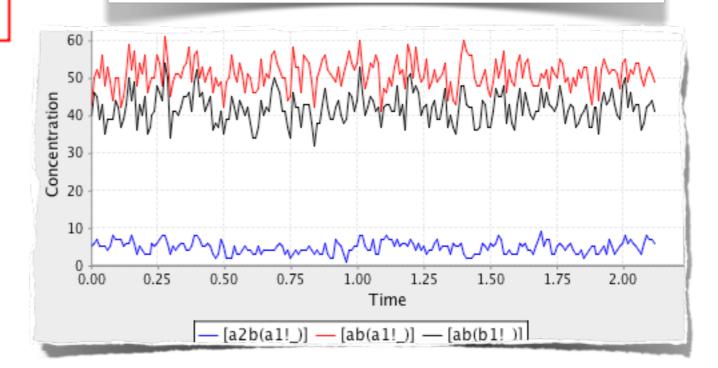
```
simplx --sim 2a_3b.ka --time 0.03 --no-measure --no-maps --output-final-state --rescale 1000
'a1-b1' 3b(b1),2a(a1) <-> 3b(b1!1),2a(a1!1) @ 1.0,50
a1-b2, 3b(b2), 2a(a1) <-> 3b(b2!1), 2a(a1!1) @ 1.0,50
'a1-b3' 3b(b3),2a(a1) <-> 3b(b3!1),2a(a1!1) @ 1.0,50
'a2-b1' 3b(b1),2a(a2) <-> 3b(b1!1),2a(a2!1) @ 1.0,50
a2-b2, 3b(b2), 2a(a2) <-> 3b(b2!1), 2a(a2!1) @ 1.0,50
a2-b3, 3b(b3), 2a(a2) <-> 3b(b3!1), 2a(a2!1) @ 1.0,50
% init: 100 * (2a(a1,a2))
%init: 100 * (3b(b3,b1,b2))
%obs: 2a(a1!_)
%obs: 3b(b1!)
%obs: 3b(b2!_)
%obs: 3b(b3!_)
%obs: 2a(a2!_)
the above takes (n = 0.2 \ 10^6):
- Initialization: 27.5 sec. CPU
- Simulation: 213.5 sec. CPU the final state is 2MB -takes ages to write in a file!- max size is
168, of relative size < 0.1\%.
```





multisets are enumerated

a+2b allows branching



Gamma=50, Z=90*ab+10*a2b

conclusions

- TE have non monotonic effects in the case of conflicting contact maps
- how good is liquidity a proxy for the size distribution
- what is the influence of other forces (extend to view-local systems)
- compute liquidity of yeast!
- where is information (more later)