

Cross-validation

- Optimize network performance given a fixed training set
- Hold out a set of data (validation set) and predict generalization performance on this set
 - Train network in usual way on training data Estimate performance of network on validation set
- If several networks trained on the same data, choose the one that performs best on the validation set (**not** the training set)
- *n-fold* Cross-validation: divide the data into *n* partitions; select each partition in turn to be the validation set, and train on the remaining (n-1) partitions. Estimate generalization error by averaging over all validation sets.

Overtraining

- Overtraining corresponds to a network function too closely fit to the training set (too much flexibility)
- Undertraining corresponds to a network function not well fit to the training set (too little flexibility)
- Solutions
 - If possible increasing both network complexity in line with the training set size
 - Use prior information to constrain the network function
 - Control the flexibility: Structural Stabilization • Control the effective flexibility: early stopping and
 - regularization

Structural Stabilization

- Directly control the number of weights:

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- Compare models with different numbers of hidden units • Start with a large network and reduce the number of weights
- by pruning individual weights or hidden units
- Weight sharing use prior knowledge to constrain the weights on a set of connections to be equal. → Convolutional Neural Networks

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Early Stopping

• Use validation set to decide when to stop training

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- Training Set Error monotonically decreases as training progresses
- Validation Set Error will reach a minimum then start to increase

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Early Stopping

Use validation set to decide when to stop training

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- Training Set Error monotonically decreases as training progresses
- Validation Set Error will reach a minimum then start to increase
- Best generalization predicted to be at point of minimum validation set error
- "Effective Flexibility" increases as training progresses
- Network has an increasing number of "effective degrees of freedom" as training progresses
- Network weights become more tuned to training data

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• Very effective — used in many practical applications such as speech recognition and optical character recognition

Weight Decay

- Weight decay puts a "spring" on weights
- If training data puts a consistent force on a weight, it will outweigh weight decay
- If training does not consistently push weight in a direction, then weight decay will dominate and weight will decay to 0
- Without weight decay, weight would walk randomly without being well determined by the data
- Weight decay can allow the data to determine how to reduce the effective number of parameters

Penalizing Complexity

• Consider adding a *complexity term* E_w to the network error function, to encourage smoother mappings:

$$E = \underbrace{E_{\text{train}}}_{\text{data term}} + \underbrace{\beta E_W}_{\text{prior term}}$$

• *E*_{train} is the usual error function:

$$E_{\text{train}}^n = -\sum_{k=1}^K t_k^n \ln y_k'$$

• If we choose the complexity term to be:

$$E_W = \frac{1}{2} \sum_i w_i^2$$

Then we have a simple partial derivative:

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$$\frac{\partial E_W}{\partial w_i} = w_i$$

Backprop Training with Weight Decay

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$$\frac{\partial E^{n}}{\partial w_{i}} = \frac{\partial (E_{\text{train}}^{n} + E_{W})}{\partial w_{i}}$$
$$= \left(\frac{\partial E_{\text{train}}^{n}}{\partial w_{i}} + \beta \frac{\partial E_{W}}{\partial w_{i}}\right)$$
$$= \left(\frac{\partial E_{\text{train}}^{n}}{\partial w_{i}} + \beta w_{i}\right)$$
$$\Delta w_{i} = -\eta \left(\frac{\partial E_{\text{train}}^{n}}{\partial w_{i}} + \beta w_{i}\right)$$

- Weight decay corresponds to adding $E_w = 1/2 \sum_i w_i^2$ to the error function
- Addition of complexity terms is called regularization
- Weight decay is sometimes called L2 regularization
- *E_W* should be easily differentiable (for backprop) and should be some sort of flexibility measure
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Summary

- The first coursework
- Generalisation
- Training / test / validation
- Early stopping and cross-validation
- Weight decay and regularization
- Reading: Michael Nielsen, chapters 2 & 3 of Neural Networks and Deep Learning

http://neuralnetworksanddeeplearning.com/

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Chris Bishop, Chapters 6 & 9 of *Neural Networks for Pattern Recognition* (although a lot more detail than needed for now)