### Learning from Data

#### Amos Storkey, School of Informatics

Semester 1

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http://www.anc.ed.ac.uk/~amos/lfd/

Amos Storkey, School of Informatics Learning from Data

#### Welcome

- Administration
  - Online notes
  - Books: See website
  - Assignments
  - Tutorials
  - Exams

Acknowledgement: I would like to that David Barber and Chris Williams for permission to use course material from previous years.

- 18 lectures 5.10 to 6.00pm Mon and Thurs
- ▶ 7 tutorials (compulsory). Start Thurs week 3.
- 2 assignments (20%) (week 4 and week 8)
- 1 exam (80%)
- Course notes.

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- LfD Learning from Data. Basic introductory course on supervised and unsupervised learning
- RL Reinforcement Learning.
- MLSC Machine Learning and Sensorimotor Control.
  - PMR Probabilistic modelling and reasoning. Focus on probabilistic modelling. Learning and inference for probabilistic models, e.g. Probabilistic expert systems, latent variable models, Hidden Markov models, Kalman filters, Boltzmann machines.
  - DME Data mining and Exploration. Using methods from PMR to deal with practical issues in learning from large datasets.

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# Maths and Learning from Data

- Learning from Data will involve a significant number of mathematical ideas and a significant amount of mathematical manipulation.
- For those wanting to pursue research in any of the areas covered, you better understand all (or almost all) the maths.
- Others should understand the *ideas* behind the maths. It is obviously preferable to understand the detail too, but understanding in a procedural way (i.e. how to program an algorithm) will usually be sufficient.

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## Course Outline (not necessarily in order)

- Introduction. Thinking about data.
- Preliminaries: supplementary maths, MATLAB.
- Understanding data, and models of data: generative versus discriminative, supervised or unsupervised.
- Gaussian density estimation, dimensionality reduction.
- Visualisation.
- Naive Bayes.
- Regression and classification, linear and logistic regression, generalised linear models.
- Mixture models, class conditional classification, visualisation 2.
- Generalisation, perceptron, layered neural networks, radial basis functions, nearest neighbour classifiers.

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- Growing flood of online data.
- People already learn from data. Automated methods increase the scope.
- Recent progress in algorithms and theory.
- Computational power is available.
- Budding industry.
- Because we can.

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## Examples

- Science (Astronomy, neuroscience, medical imaging, bio-informatics).
- Retail (Intelligent stock control, demographic store placement)
- Manufacturing (Intelligent control, automated monitoring, detection methods)
- Security (Intelligent smoke alarms, fraud detection).
- Marketing
- Management (Scheduling, time tabling, competitor analysis warning systems).
- Finance (risk analysis, micro-elasticity analysis).
- Over to you...

- This course is not computer science as you know it.
- Computer science and algorithms:
  - Computer science as algorithm generation.
  - If the algorithm works it is good. If it doesn't it is bad.
- Machine Learning: the algorithm and the model.
  - Model encodes understanding about the data.
  - Algorithm comes from the model (and a bit of maths).

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Algorithms give different approximations.

- Learning from data is not magic.
- Prior beliefs/assumptions + data  $\rightarrow$  posterior beliefs.
- The model encodes beliefs about the generative process of the data.
- or... The model encodes beliefs about the features/characteristics in the data.
- Can do nothing without some prior input no connection between data and question.

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- Logvinenko illusion
- Meteor internet ray tracing entry.

# Logvinenko Illusion



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3 Boolean variables. Data set:

 $\begin{array}{ccccc} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & x \end{array}$ 

- ▶ What is *x*?
- We cannot say. We have no information at all about how any of these data items is connected.

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"No free lunch"

## No Free Lunch

- Try to predict  $C \in \{0, 1\}$  from  $A, B \in \{0, 1\}$ .
- ▶ No noise given A,B then C is always the same.
- Possible hypotheses. C = 1 if and only if values for A,B are in a particular set. One example hypothesis is:
- ► {(1, 1), (0, 1), (1, 0)} (i.e. C = A OR B). Here (0, 1) means A = 0, B = 1.
- ▶ If no bias, then there are  ${}^{4}C_{0} + {}^{4}C_{1} + {}^{4}C_{2} + {}^{4}C_{3} + {}^{4}C_{4} = 16$  equally possible hypotheses - the hypothesis space.
- Each data point reduces the size of the hypothesis space, but when we attempted to predict C given an unseen set of values of A,B the number of hypotheses predicting C = 1 is the same as the number predicting C = 0.

## No Free Lunch contd.

- Eg suppose we have data (a = 1, b = 1, c = 0), (a = 0, b = 1, c = 1), then the remaining C = 1 hypothesis space for (AB) is
- ► {(0,1)}, {(0,1), (1,0)}, {(0,1), (0,0)}, {(0,1), (1,0), (0,0)}.
- Suppose we now query (a = 1, b = 0). Two of the possible hypotheses predict C = 1, and two predict C = 0.
- Suppose we now see data (a = 0, b = 0, c = 0). Hypothesis space is {(0,1)}, {(0,1), (1,0)}.
- One of the remaining hypotheses predict C = 1, and the other predicts C = 0.
- No matter what data you receive the number of hypotheses predicting one values for unseen data will equal the number predicting the other value.

- Prior assumption: say something about the ways C is allowed to relate to A, B.
- ► e.g. (C = A OR B) OR (C = A AND B) OR (C = A XOR B).
- ► (*a* = 1, *b* = 0, *c* = 1), (*a* = 0, *b* = 1, *c* = 1):
- So either OR or XOR. Can predict (a = 0, b = 0, c =?).

- Model Free.
- Bias Free. Unbiased.
- No prior information.
- Generally applicable.

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- Probability theory is key: probabilistic understanding of uncertainty.
- Bayesian methods: machine learning is really just statistics?
- Bayesian methods are non-trivial:
  - Hard to really understand the full implications of a probability distribution.
  - Hard to accurately represent your prior beliefs, and represent them in a way that is amenable to computation.

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- Fairly mathematical course. Try to keep on top of it.
- No free lunch.
- Plethora of practical needs.
- Models not algorithms.
- Probability theory is key.

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