# Elements of Programming Languages Tutorial 8: References and laziness Week 10 (November 21–25, 2016)

Exercises marked  $\star$  are more advanced. Please try all unstarred exercises before the tutorial meeting.

#### 1. Semantics of references

- (a) Give explicit small-step rules for evaluating the sequential composition expression  $e_1$ ;  $e_2$ . (Remember that it can also be viewed as syntactic sugar for let  $x = e_1$  in  $e_2$  provided x is a fresh variable unused in either expression)
- (b) Evaluate the following expression to completion:

$$let r = ref(ref(42)) in !(!(r))$$

(c) Consider the following expression:

let 
$$r = ref(\lambda x. x)$$
 in  $r := (\lambda x. x + 1); (!r)(true)$ 

Apply small-step evaluation to this expression until it reaches either a value or an error state.

# 2. Interaction of references and evaluation order

Consider the following expression *e*:

let 
$$r = ref(42)$$
 in  $(\lambda x.print(x); print(x))$   $(r := !r + 1; !r)$ 

where print is a side-effecting operation that fully evaluates its argument to a value and then prints it. For each of the following evaluation strategies, explain informally how e would be evaluated and what the printed output will be.

- (a) call-by-value
- (b) call-by-name
- (c) call-by-need / lazy evaluation

### 3. Embedding L<sub>While</sub> in Scala

Recall the statements of L<sub>While</sub>:

$$Stmt \ni s ::=$$
 skip  $\mid s_1; s_2 \mid x := e \mid$  if  $e \text{ then } s_1 \text{ else } s_2 \mid$  while  $e \text{ do } s$ 

In this exercise, we will show how to embed these statements into Scala, viewing  $L_{While}$ 's variables as references using the Ref[T] type discussed in class:

```
class Ref[A] (val x: A) {
  private var a = x
  def get = a
  def set(y: A) = { a = y }
}
```

Statements in  $L_{While}$  will correspond to expressions of type unit in Scala, and variables will correspond to instances of the Ref[T] type. Consider the following interface:

```
val skip : ()
def seq(s1: => Unit, s2: => Unit): Unit
def assign[T](x: Ref[T], e: => T): Unit
def ifthenelse(e: => Boolean, s1: => Unit, s2: => Unit): Unit
def whiledo(e: => Boolean, s: => Unit): Unit
```

Notice in particular that most arguments are passed *by name* (that is, their types are of the form => T).

- (a) Implement the above operations.
- (b) Why do the statements expressions in assign, ifthenelse, and whiledo need to be passed by name? What would happen if they were passed by value?
- (c) ( $\star$ ) We have not considered how to adapt *expressions*. In L<sub>While</sub>, a mutable variable occurring in an expression is evaluated to its value. How should we adjust such expressions in L<sub>Ref</sub>?

## 4. (⋆) Stream programming

Consider the following Stream type:

```
abstract class Stream[+A]
case object Empty extends Stream[Nothing]
case class SCons[+A](h: A, t: () => Stream[A]) extends Stream[A]
```

This defines a type of *streams*, which are similar to lists, but the evaluation of the tail of a stream is delayed.

Define Scala functions on streams as follows:

- (a) const[A]: A => Stream[A] so that const(a) which produces an infinite stream of a's.
- (b) take[A]: (Int, Stream[A]) => List[A] so that take(n, s) lists the
   first n elements from s.
- (c) repeat[A]: (A => A) => A => Stream[A] such that

  repeat(a)(f) = Stream(a,f(a),f(f(a)),..)

For example, repeat (0) (incr) should produce the stream 0, 1, 2, 3, ..., if incr is the increment function.

(d) map[A]: Stream[A] => (A => B) => Stream[B] that applies the function f: A => B to each element of the stream s: Stream[A] yielding a stream of Bs.