# Lecture 14 Instruction Selection: Tree-pattern matching

#### (EaC-11.3)

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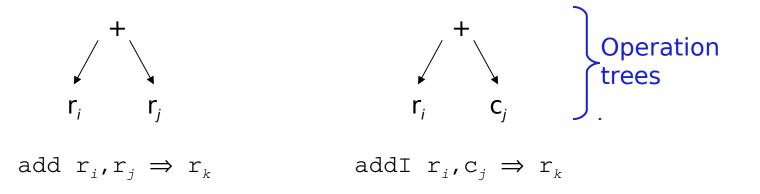
### The Concept

Many compilers use tree-structured IRs

- Abstract syntax trees generated in the parser
- Trees or DAGs for expressions

These systems might well use trees to represent target ISA

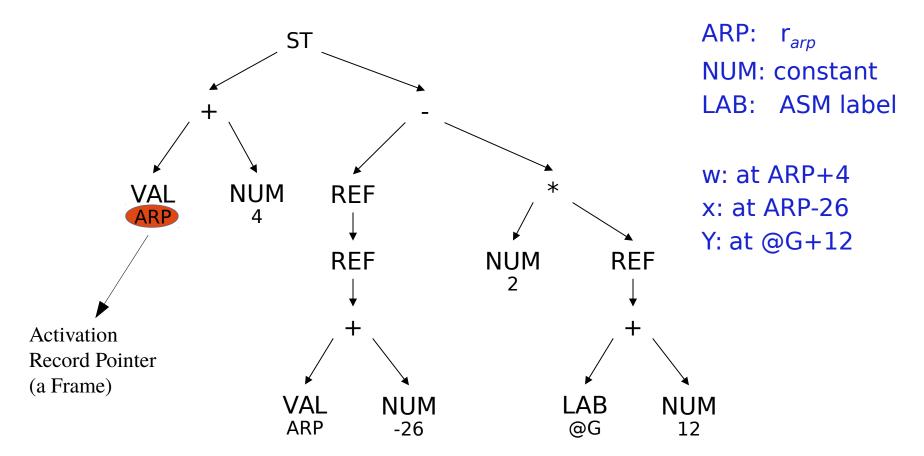
Consider the ILOC add operators



If we can match these "pattern trees" against IR trees, ...

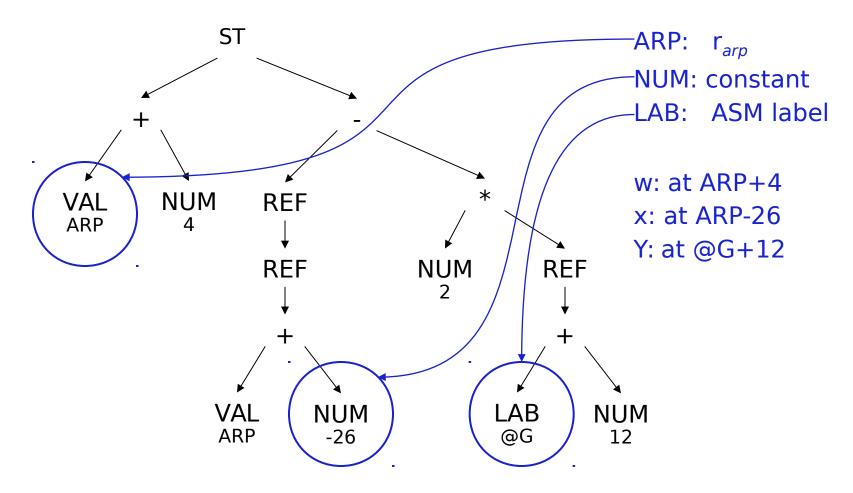
#### The Concept

Low-level AST for  $w \leftarrow x - 2 * y$ 



#### The Concept

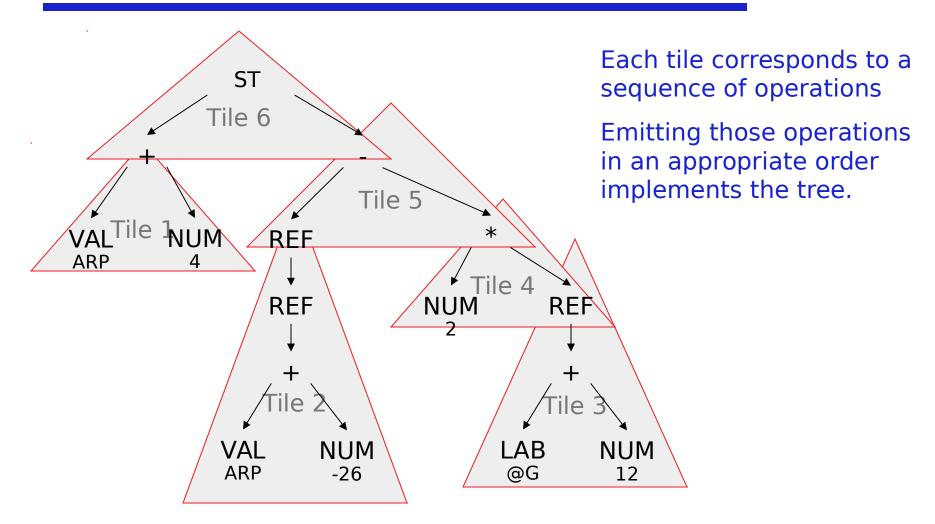
Low-level AST for  $w \leftarrow x - 2 * y$ 



Tree-pattern matching

Goal is to "tile" AST with operation trees

- A tiling is collection of <*ast,op* > pairs
  - $\rightarrow$  ast is a node in the AST
  - $\rightarrow$  op is an operation tree
  - $\rightarrow$  *<ast, op >* means that *op* could implement the subtree at *ast*
- A tiling 'implements" an AST if it covers every node in the AST and the overlap between any two trees is limited to a single node
  - $\rightarrow$  <ast, op>  $\in$  tiling means ast is also covered by a leaf in another operation tree in the tiling, unless it is the root
  - → Where two operation trees meet, they must be compatible (expect the value in the same location)



## Generating Code

Given a tiled tree

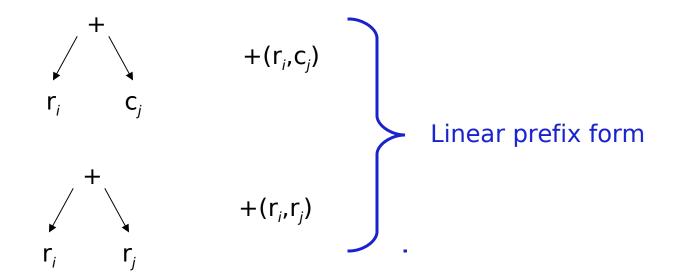
- Postorder treewalk, with node-dependent order for children
  - $\rightarrow$  Right child of  $\leftarrow$  before its left child
  - $\rightarrow$  Might impose "most demanding first" rule ...
- Emit code sequence for tiles, in order
- Tie boundaries together with register names
  - $\rightarrow$  Tile 6 uses registers produced by tiles 1 & 5
  - $\rightarrow$  Tile 6 emits "store  $r_{tile 5} \Rightarrow r_{tile 1}$ "
  - $\rightarrow$  Can incorporate a "real" allocator or can use "NextRegister++"

Finding the matches to tile the tree

- Compiler writer connects operation trees to AST subtrees
  - $\rightarrow$  Encode tree syntax, in linear form
  - $\rightarrow$  Provides a set of rewrite rules
  - $\rightarrow$  Associated with each is a code template

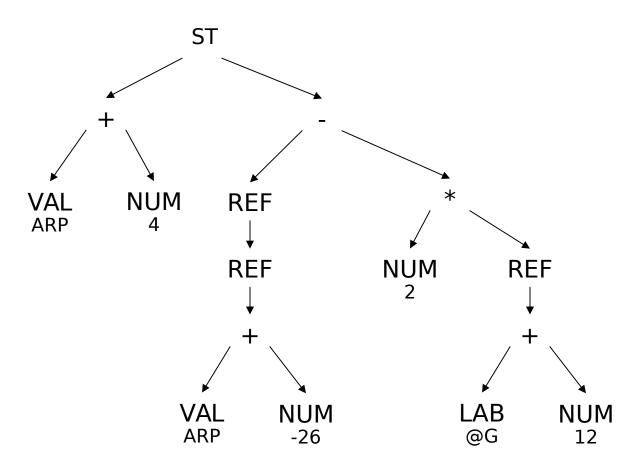
#### Notation

To describe these trees, we need a concise notation



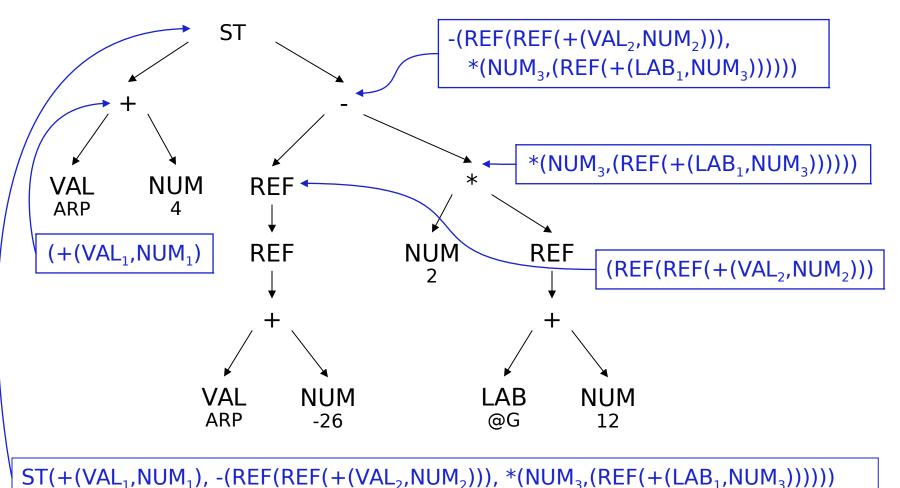
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#### Rewrite rules: LL Integer AST into ILOC

	Rule	Cost	Template
1	Goal $\rightarrow$ Assign	0	
2	Assign $\rightarrow$ ST(Reg <sub>1</sub> ,Reg <sub>2</sub> )	1	store $r_2 \Rightarrow r_1$
3	Assign $\rightarrow$ ST(+(Reg <sub>1</sub> ,Reg <sub>2</sub> ),Reg <sub>3</sub> )	1	storeA0 $r_3 \Rightarrow r_1, r_2$
4	Assign $\rightarrow$ ST(+(Reg <sub>1</sub> ,NUM <sub>2</sub> ),Reg <sub>3</sub> )	1	storeAI $r_3 \Rightarrow r_1, n_2$
5	Assign $\rightarrow$ ST(+(NUM <sub>1</sub> ,Reg <sub>2</sub> ),Reg <sub>3</sub> )	1	storeAI $r_3 \Rightarrow r_2, n_1$
6	$\text{Reg} \rightarrow \text{LAB}_1$	1	loadI $l_1 \Rightarrow r_{new}$
7	$Reg \to VAL_1$	0	
8	$Reg \to NUM_1$	1	loadI $n_1 \Rightarrow r_{new}$
9	$Reg \to REF(Reg_1)$	1	load $r_1 \Rightarrow r_{new}$
10	$Reg \to REF(+ (Reg_1, Reg_2))$	1	loadAO $r_1, r_2 \Rightarrow r_{new}$
11	$Reg \to REF(+ (Reg_1, NUM_2))$	1	loadAI $r_1, n_2 \Rightarrow r_{new}$
12	$Reg \rightarrow REF(+ (NUM_1, Reg_2))$	1	loadAI $r_2, n_1 \Rightarrow r_{new}$

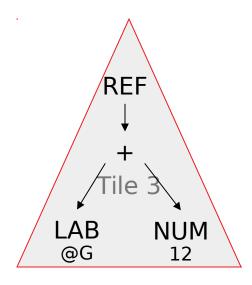
#### Rewrite rules: LL Integer AST into ILOC (part II)

	Rule	Cost	Template
13	$\text{Reg} \rightarrow \text{REF}(+ (\text{Reg}_1, \text{Lab}_2))$	1	loadAI $r_1, l_2 \Rightarrow r_{new}$
14	$Reg \to REF(+ (Lab_1, Reg_2))$	1	loadAI $r_2, l_1 \Rightarrow r_{new}$
15	$Reg \to + (Reg_1, Reg_2)$	1	addI $r_1, r_2 \Rightarrow r_{new}$
16	$\text{Reg} \rightarrow + (\text{Reg}_1, \text{NUM}_2)$	1	addI $r_1, n_2 \Rightarrow r_{new}$
17	$Reg \to + (NUM_1, Reg_2)$	1	addI $r_2, n_1 \Rightarrow r_{new}$
18	$Reg \to + (Reg_1, Lab_2)$	1	addI $r_1, l_2 \Rightarrow r_{new}$
19	$Reg \to + (Lab_1, Reg_2)$	1	addI $r_2, l_1 \Rightarrow r_{new}$
20	$\text{Reg} \rightarrow - (\text{NUM}_1, \text{Reg}_2)$	1	rsubl $r_2, n_1 \Rightarrow r_{new}$

A real set of rules would cover more than signed integers ...

Need an algorithm to AST subtrees with the rules

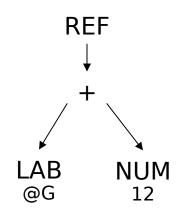
Consider tile 3 in our example



Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example

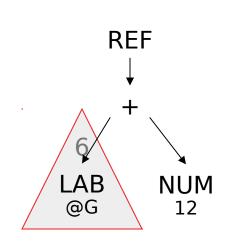
What rules match tile 3?



Need an algorithm to AST subtrees with the rules

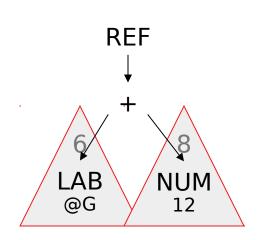
Consider tile 3 in our example

What rules match tile 3?
6: Reg → LAB<sub>1</sub> tiles the lower left node



Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example

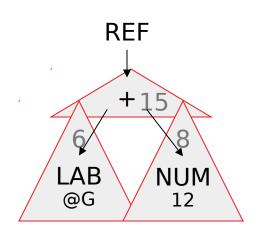


What rules match tile 3? 6: Reg  $\rightarrow$  LAB<sub>1</sub> tiles the lower left node

8: Reg  $\rightarrow$  NUM<sub>1</sub> tiles the bottom right node

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example



What rules match tile 3?

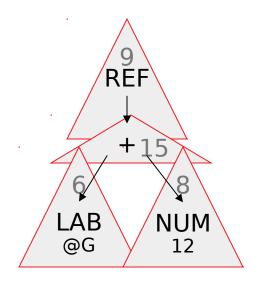
6: Reg  $\rightarrow$  LAB<sub>1</sub> tiles the lower left node

8: Reg  $\rightarrow$  NUM<sub>1</sub> tiles the bottom right node

15:  $\text{Reg} \rightarrow + (\text{Reg}_1, \text{Reg}_2)$  tiles the + node

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example

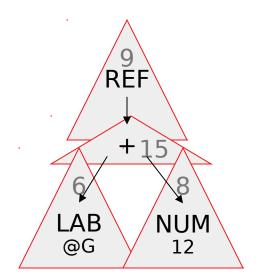


#### What rules match tile 3?

- 6: Reg  $\rightarrow$  LAB<sub>1</sub> tiles the lower left node
- 8: Reg  $\rightarrow$  NUM<sub>1</sub> tiles the bottom right node
- 15:  $\text{Reg} \rightarrow + (\text{Reg}_1, \text{Reg}_2)$  tiles the + node
- 9:  $\text{Reg} \rightarrow \text{REF}(\text{Reg}_1)$  tiles the REF

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example



#### What rules match tile 3?

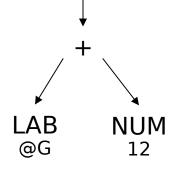
- 6: Reg  $\rightarrow$  LAB<sub>1</sub> tiles the lower left node
- 8: Reg  $\rightarrow$  NUM<sub>1</sub> tiles the bottom right node
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- 9:  $\text{Reg} \rightarrow \text{REF}(\text{Reg}_1)$  tiles the REF

We denote this match as <6,8,15,9> Of course, it implies <8,6,15,9> Both have a cost of 4

## Finding matches

#### Many Sequences Match Our Subtree

Cost	Sequences			
2	6,11	8,12		
3	6,8,10	8,6,10	6,16,9	8,19,9
4	6,8,15,9	8,6,15,9		



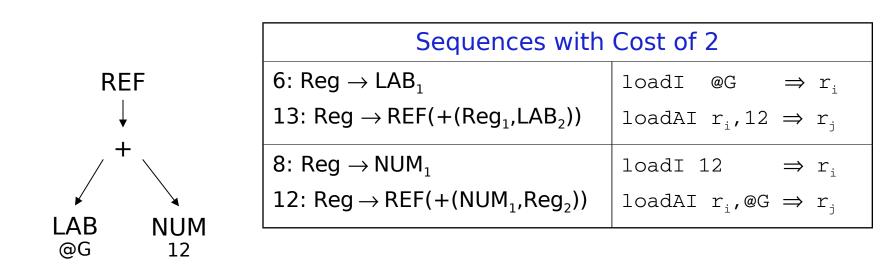
REF

In general, we want the low cost sequence

- Each unit of cost is an operation (1 cycle)
- We should favour short sequences

## Finding matches

Low Cost Matches

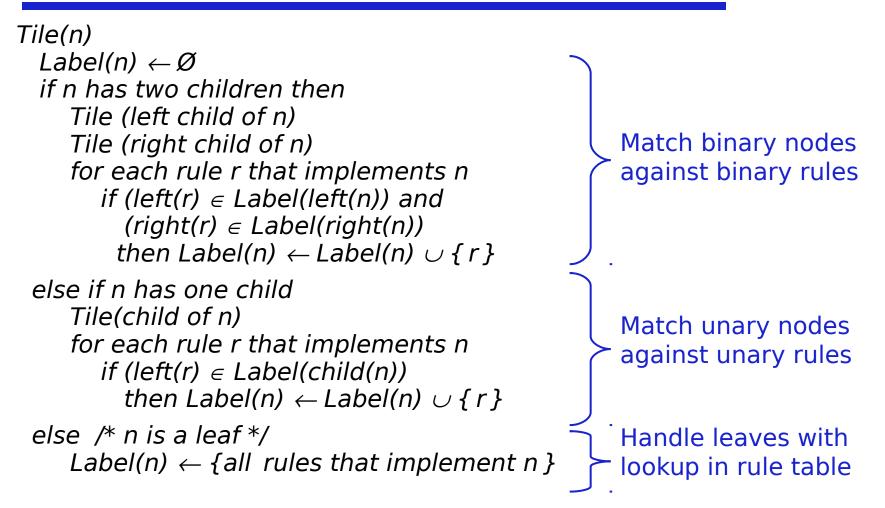


These two are equivalent in cost

6,13 might be better, because @G may be longer than the immediate field

Still need an algorithm

- Assume each rule implements one operator
- Assume operator takes 0, 1, or 2 operands Now, ...



#### Tile(n) Label(n) $\leftarrow \emptyset$ if n has two children then Tile (left child of n) Tile (right child of n) for each rule r that implements n if $(left(r) \in Label(left(n)))$ and $(right(r) \in Label(right(n)))$ then Label(n) $\leftarrow$ Label(n) $\cup$ { r } else if n has one child Tile(child of n) for each rule r that implements n if (left(r) $\in$ Label(child(n)) then Label(n) $\leftarrow$ Label(n) $\cup$ { r } else /\* n is a leaf \*/

Label(n)  $\leftarrow$  {all rules that implement n }

#### This algorithm

- Finds all matches in rule set
- Labels node n with that set
- Can keep lowest cost match at each point
- Leads to a notion of local optimality — lowest cost at each point
- Spends its time in the two matching loops

## The Big Picture

- Tree patterns represent AST and ASM
- Can use matching algorithms to find low-cost tiling of AST
- Can turn a tiling into code using templates for matched rules
- Techniques (& tools) exist to do this efficiently

Hand-coded matcher like <i>Tile</i>	Avoids large sparse table Lots of work
Encode matching as an automaton	O(1) cost per node Tools like BURS (bottom-up rewriting system), BURG
Use parsing techniques	Uses known technology Very ambiguous grammars
Linearize tree into string and use string searching algorithm (Aho-Corasick)	Finds all matches

• Register Allocation