## Compiling Techniques Lecture 4: Automatic Lexer Generation (EaC§2.4)

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## Reminder

### Action

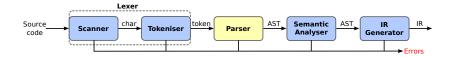
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## Automatic Lexer Generation



- Starting from a collection of regular expressions (RE) we automatically generate a Lexer.
- We use finite state automata (FSA) for the construction

#### Definition: finite state automata

A finite state automata is defined by:

- *S*, a finite set of states
- $\bullet~\Sigma,$  an alphabet, or character set used by the recogniser
- δ(s, c), a transition function (takes a state and a character and returns new state)
- s<sub>0</sub>, the initial or start state
- $S_F$ , a set of final states (a stream of characters is accepted iif the automata ends up in a final state)

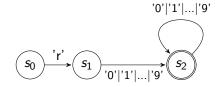
Finite State Automata Non-determinism

### Finite State Automata for Regular Expression

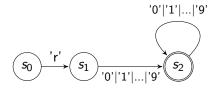
#### Example: register names

```
register ::= 'r' ('0'|'1'|...|'9') ('0'|'1'|...|'9')*
```

The RE (Regular Expression) corresponds to a recogniser (or finite state automata):



Finite State Automata Non-determinism



Finite State Automata (FSA) operation:

• Start in state s<sub>0</sub> and take transitions on each input character

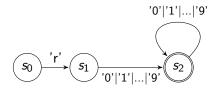
• The FSA accepts a word **x** iff **x** leaves it in a final state (*s*<sub>2</sub>) Examples:

- **r17** takes it through  $s_0, s_1, s_2$  and accepts
- **r** takes it through  $s_0, s_1$  and fails
- a starts in s<sub>0</sub> and leads straight to failure

Finite State Automata Non-determinism

### Table encoding and skeleton code

To be useful a recogniser must be turned into code



#### Table encoding RE

δ	'r'	'0 '  '1 '   '9 '	others
<i>s</i> <sub>0</sub>	<i>s</i> <sub>1</sub>	error	error
<i>s</i> <sub>1</sub>	error	<i>s</i> <sub>2</sub>	error
<i>s</i> <sub>2</sub>	error	<i>s</i> <sub>2</sub>	error

### Skeleton recogniser

```
c = next character

state = s_0

while (c \neq EOF)

state = \delta(state, c)

c = next character

if (state final)

return success

else

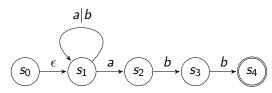
return error
```

Finite State Automata Non-determinism

#### Deterministic Finite Automaton

Each RE corresponds to a Deterministic Finite Automaton (DFA). However, it might be hard to construct directly.

What about an RE such as  $(a|b)^*abb$ ?



This is a little different:

- $s_0$  has a transition on  $\epsilon$ , which can be followed without consuming an input character
- s<sub>1</sub> has two transitions on a
- This is a Non-determinisitic Finite Automaton (NFA)

## Non-deterministic vs deterministic finite automata

Deterministic finite state automata (DFA):

- All edges leaving the same node have distinct labels
- There is no  $\epsilon$  transition

Non-deterministic finite state automata (NFA):

- Can have multiple edges with the same label leaving from the same node
- Can have  $\epsilon$  transition
- This means we might have to backtrack

Regular Expression to NFA From NFA to DFA

## Automatic Lexer Generation

It is possible to systematically generate a lexer for any regular expression.

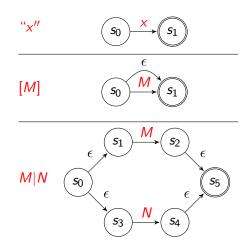
This can be done in three steps:

- regular expression (RE)  $\rightarrow$  non-deterministic finite automata (NFA)
- **2** NFA  $\rightarrow$  deterministic finite automata (DFA)
- $\textbf{3} \ \mathsf{DFA} \to \mathsf{generated} \ \mathsf{lexer}$

**Regular Expression to NFA** From NFA to DFA

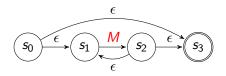
## 1st step: $RE \rightarrow NFA$ (Ken Thompson, CACM, 1968)

ΜN

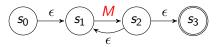


 $(s_0 \xrightarrow{\mathsf{M}} (s_1 \xrightarrow{\epsilon} (s_2 \xrightarrow{\mathsf{N}} (s_3)$ 

 $M^*$ 

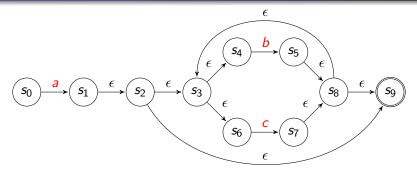


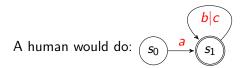




**Regular Expression to NFA** From NFA to DFA

## Example: $a(b|c)^*$





Regular Expression to NFA From NFA to DFA

## Step 2: NFA $\rightarrow$ DFA

Executing a non-deterministic finite automata requires backtracking, which is inefficient. To overcome this, we need to construct a DFA from the NFA. The main idea:

- We build a DFA which has one state for each set of states the NFA could end up in.
- A set of state is final in the DFA if it contains the final state from the NFA.
- Since the number of states in the NFA is finite (*n*), the number of possible sets of states is also finite (maximum 2<sup>n</sup>).

Assuming the state of the NFA are labelled  $s_i$  and the states of the DFA we are building are labelled  $q_i$ .

We have two key functions:

- reachable( $s_i$ ,  $\alpha$ ) returns the set of states reachable from  $s_i$  by consuming character  $\alpha$
- *ϵ*-closure(s<sub>i</sub>) returns the set of states reachable from s<sub>i</sub> by ϵ
   (*e.g.* without consuming a character)

Regular Expression to NFA From NFA to DFA

### The Subset Construction algorithm (Fixed point iteration)

```
\begin{array}{l} q_0 = \epsilon\text{-closure}(s_0); \ Q = \{q_0\}; \ \text{add} \ q_0 \ \text{to} \ \text{WorkList} \\ \text{while} \ (\text{WorkList} \ \text{not} \ \text{empty}) \\ \text{remove} \ q \ \text{from} \ \text{WorkList} \\ \text{for} \ \text{each} \ \alpha \in \Sigma \\ subset = \epsilon\text{-closure}(reachable(q, \alpha)) \\ \delta(q, \alpha) = subset \\ \text{if} \ (subset \notin Q) \ \text{then} \\ \text{add} \ subset} \ \text{to} \ Q \ \text{and} \ \text{to} \ \text{WorkList} \end{array}
```

### The algorithm (in English)

- Start from start state  $s_0$  of the NFA, compute its  $\epsilon$ -closure
- Build subset from all states reachable from  $q_0$  for character lpha
- Add this subset to the transition table/function  $\delta$
- If the subset has not been seen before, add it to the worklist
- Iterate until no new subset are created

Regular Expression to NFA From NFA to DFA

### Informal proof of termination

- Q contains no duplicates (test before adding)
- similarly we will never add twice the same subset to the worklist
- bounded number of states; maximum 2<sup>n</sup> subsets, where n is number of state in NFA
- $\Rightarrow$  the loop halts

#### End result

- S contains all the reachable NFA states
- It tries each symbol in each s<sub>i</sub>
- It builds every possible NFA configuration
- $\Rightarrow$  **Q** and  $\delta$  form the DFA

Regular Expression to NFA From NFA to DFA

## $\mathsf{NFA}\to\mathsf{DFA}$

$a(b c)^*$	$s_0 \xrightarrow{\epsilon} s_1 \xrightarrow{\epsilon} s_2 \xrightarrow{\epsilon} s_3 \xrightarrow{\epsilon} s_6 \xrightarrow{\epsilon} s_7 \xrightarrow{\epsilon} s$							
			$\epsilon$ -closure(reachable( $q, \alpha$ ))					
		NFA states	а	b	С			
	$q_0$	<i>s</i> <sub>0</sub>	$q_1$	none	none			
	$q_1$	$s_1, s_2, s_3,$	none	<i>q</i> <sub>2</sub>	<i>q</i> <sub>3</sub>			
		$s_4, s_6, s_9$						
	$q_2$	<i>s</i> <sub>5</sub> , <i>s</i> <sub>8</sub> , <i>s</i> <sub>9</sub> ,	none	<i>q</i> <sub>2</sub>	<i>q</i> <sub>3</sub>			
		<i>s</i> <sub>3</sub> , <i>s</i> <sub>4</sub> , <i>s</i> <sub>6</sub>						
	<i>q</i> <sub>3</sub>	<i>s</i> <sub>7</sub> , <i>s</i> <sub>8</sub> , <i>s</i> <sub>9</sub> ,	none	<i>q</i> <sub>2</sub>	<i>q</i> <sub>3</sub>			
		<i>s</i> <sub>7</sub> , <i>s</i> <sub>8</sub> , <i>s</i> <sub>9</sub> , <i>s</i> <sub>3</sub> , <i>s</i> <sub>4</sub> , <i>s</i> <sub>6</sub>						

Regular Expression to NFA From NFA to DFA

# Resulting DFA for $a(b|c)^*$

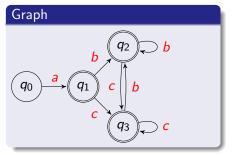


Table encoding								
	а	b	С					
$q_0$	$q_1$	error	error					
$q_1$	error	$q_2$	<i>q</i> 3					
$q_2$	error	$q_2$	<i>q</i> 3					
<b>q</b> 3	error	<i>q</i> <sub>2</sub>	<i>q</i> 3					

- Smaller than the NFA
- All transitions are deterministic (no need to backtrack!)
- Could be even smaller (see EaC§2.4.4 Hopcroft's Algorithm for minimal DFA)
- Can generate the lexer using skeleton recogniser seen earlier

### What can be so hard?

Poor language design can complicate lexing

• PL/I does not have reserved words (keywords):

if then then then = else; else else = then

- In Fortran & Algol68 blanks (whitespaces) are insignificant: do 10 i = 1,25 ≅ do 10 i = 1,25 (loop) do 10 i = 1.25 ≅ do10i = 1.25 (assignment)
- In C,C++,Java string constants can have special characters: newline, tab, quote, comment delimiters, ...

# Building Lexer

The important point:

- All this technology lets us automate lexer construction
- Implementer writes down regular expressions
- Lexer generator builds NFA, DFA and then writes out code
- This reliable process produces fast and robust lexers

For most modern language features, this works:

- As a language designer you should think twice before introducing a feature that defeats a DFA-based lexer
- The ones we have seen (*e.g.* insignificant blanks, non-reserved keywords) have not proven particularly useful or long lasting

## Next lecture

### Parsing:

- Context-Free Grammars
- Dealing with ambiguity
- Recursive descent parser