

# Block ciphers

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A block cipher with parameters  $k$  and  $\ell$  is a pair of deterministic algorithms  $(E, D)$  such that

- ▶ Encryption  $E : \{0, 1\}^k \times \{0, 1\}^\ell \rightarrow \{0, 1\}^\ell$
- ▶ Decryption  $D : \{0, 1\}^k \times \{0, 1\}^\ell \rightarrow \{0, 1\}^\ell$

Examples:

3DES:  $\ell = 64$ ,  $k = 168$

AES:  $\ell = 128$ ,  $k = 128, 192, 256$

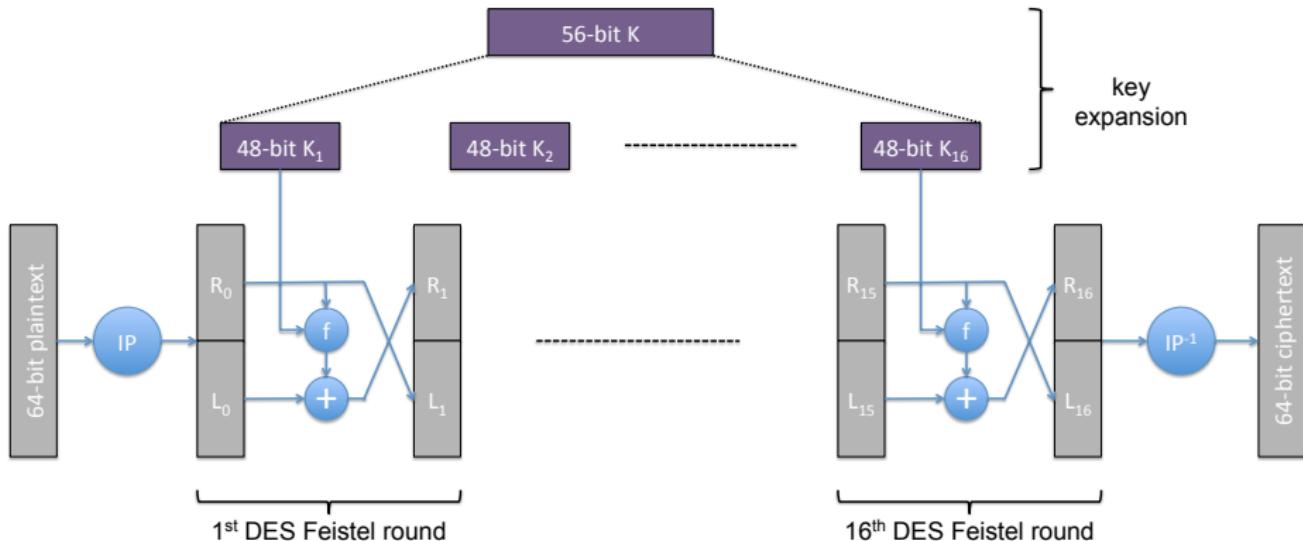
# Data Encryption Standard (DES)

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- ▶ Early 1970s: Horst Feistel designs Lucifer at IBM  
 $k = 128$  bits,  $\ell = 128$  bits
- ▶ 1973: NBS calls for block cipher proposals.  
→ IBM submits a variant of Lucifer.
- ▶ 1976: NBS adopts DES as a federal standard  
 $k = 56$  bits,  $\ell = 64$  bits
- ▶ 1997: DES broken by exhaustive search
- ▶ 2001: NIST adopts AES to replace DES  
 $k = 128, 192, 256$  bits,  $\ell = 128$  bits

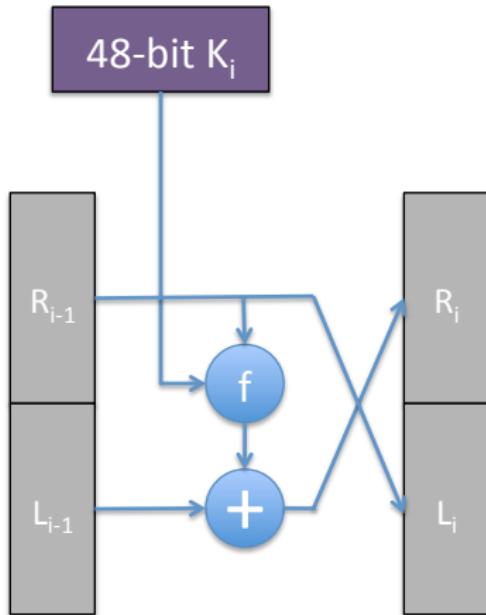
Widely deployed in banking (ATM machines) and commerce

# DES: encryption circuit



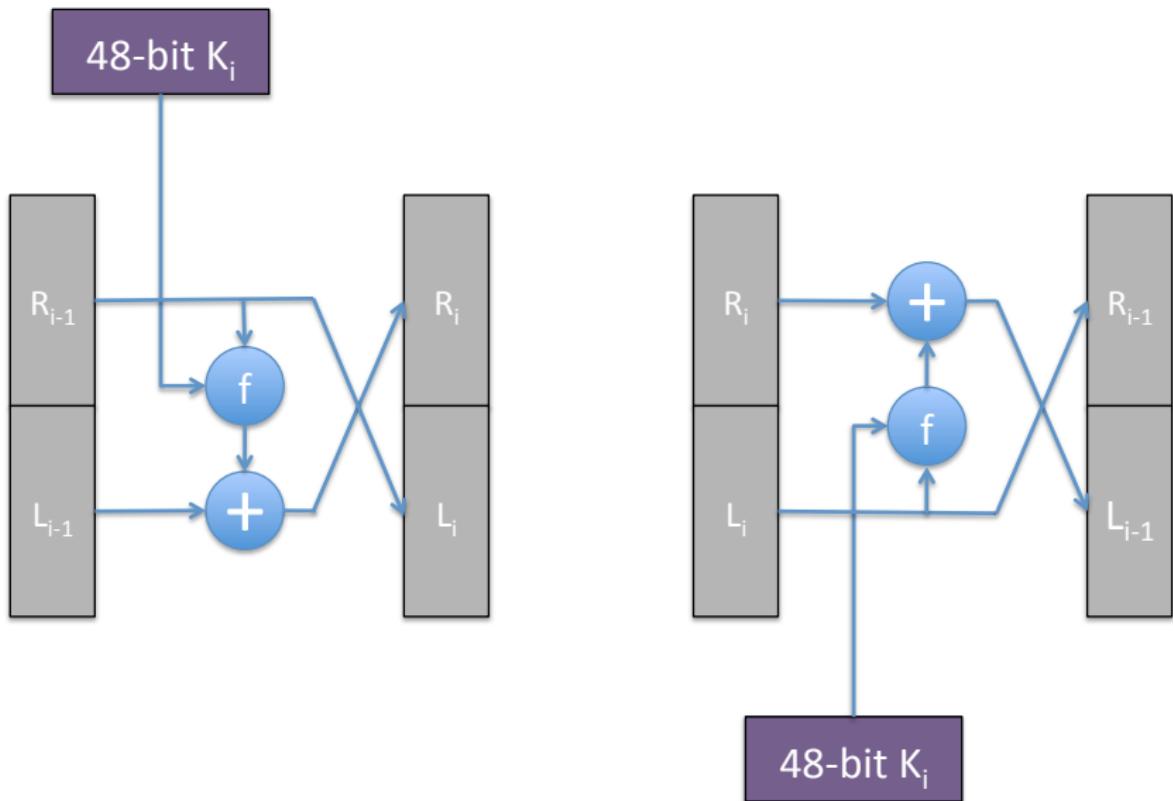
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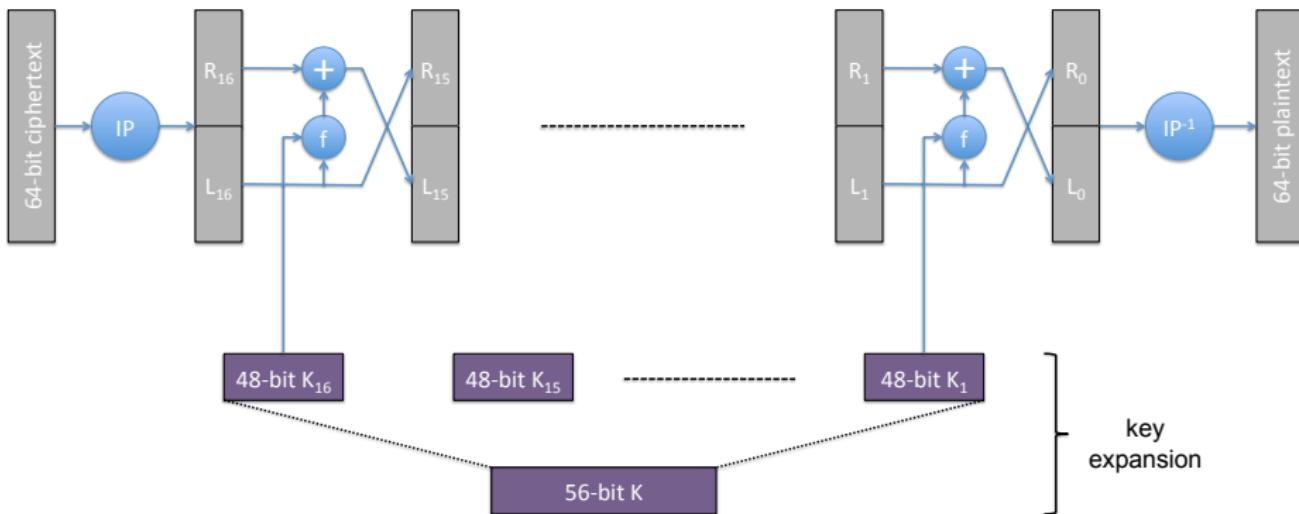


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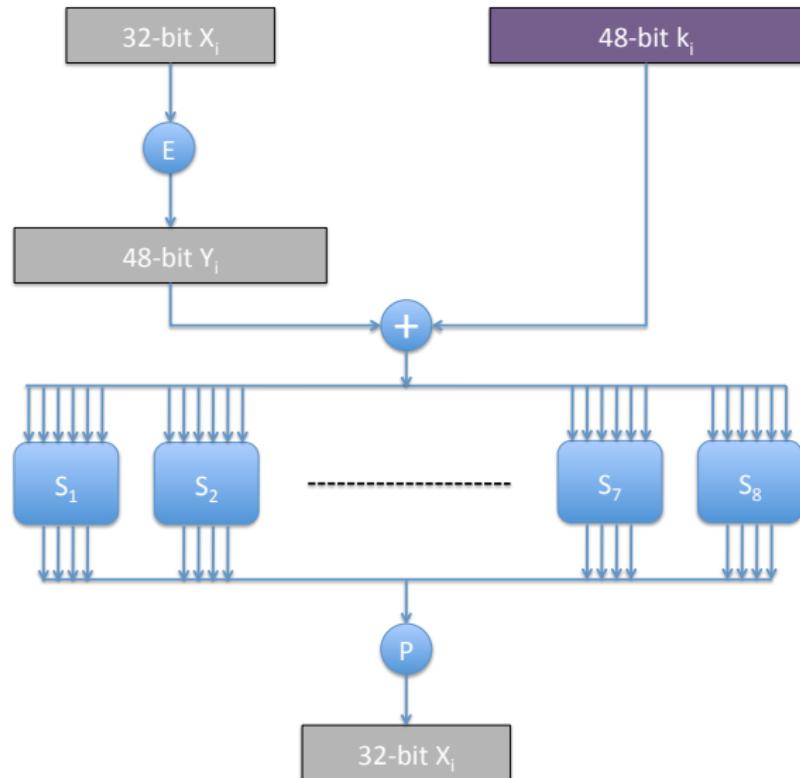


# DES: decryption circuit



# DES: the function $f$

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# DES: $S_5$ -box

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$S_5$		Middle 4 bits of input															
		0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Outer bits	00	0010	1100	0100	0001	0111	1010	1011	0110	1000	0101	0011	1111	1101	0000	1110	1001
	01	1110	1011	0010	1100	0100	0111	1101	0001	0101	0000	1111	1010	0011	1001	1000	0110
	10	0100	0010	0001	1011	1010	1101	0111	1000	1111	1001	1100	0101	0110	0011	0000	1110
	11	1011	1000	1100	0111	0001	1110	0010	1101	0110	1111	0000	1001	1010	0100	0101	0011

$$S_5 : \{0, 1\}^6 \rightarrow \{0, 1\}^4$$

(source: Wikipedia)

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→ Note that  $S_5$  is not reversible as it maps 6 bits to 4 bits.

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⇒ DES is badly broken! Do not use it in new projects!!

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- ▶ simple (meet-in-the-middle) attack in time  $2^{118}$

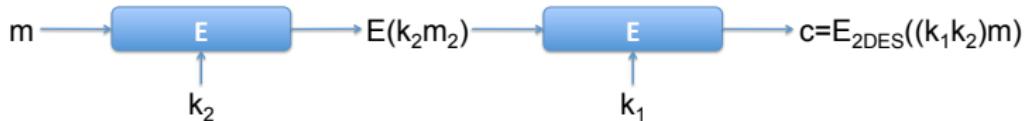
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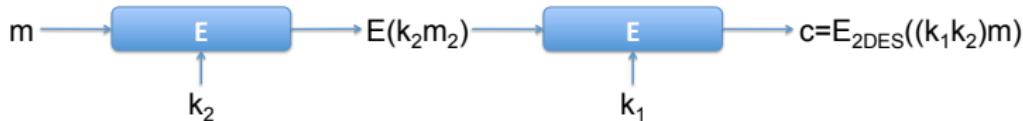
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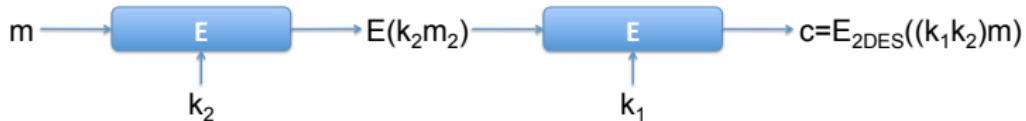


⇒ For  $m$  and  $c$  such that  $E_{2DES}((k_1, k_2), m) = c$  we have that  $E_{DES}(k_2, m) = D_{DES}(k_1, c)$

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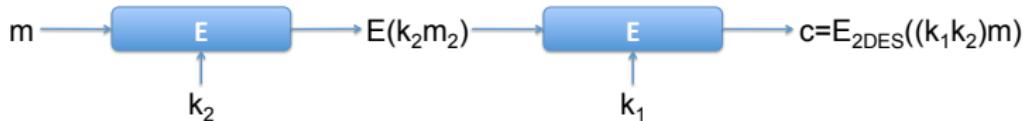
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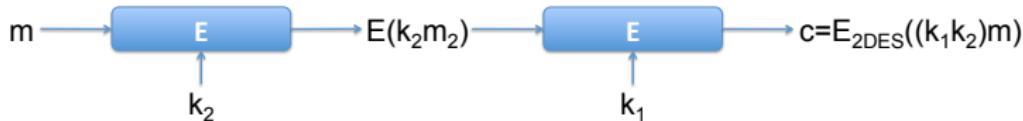


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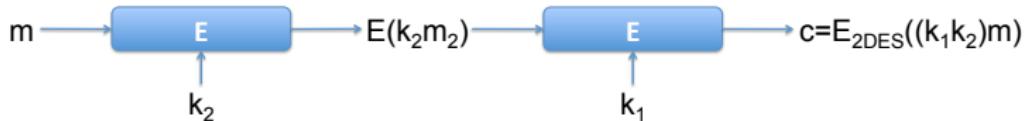
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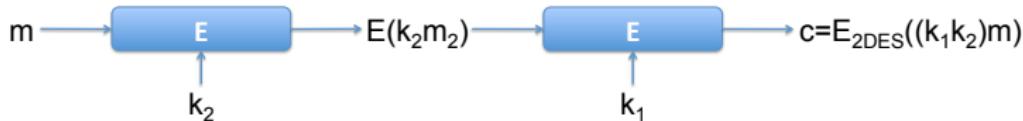
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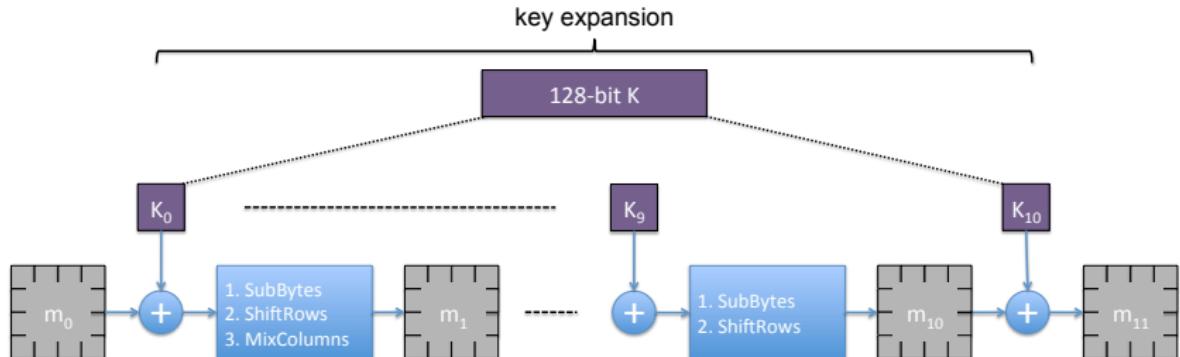
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- ▶ Similar attack on 3DES in time  $2^{118}$

# The Advanced Encryption Standard (AES)

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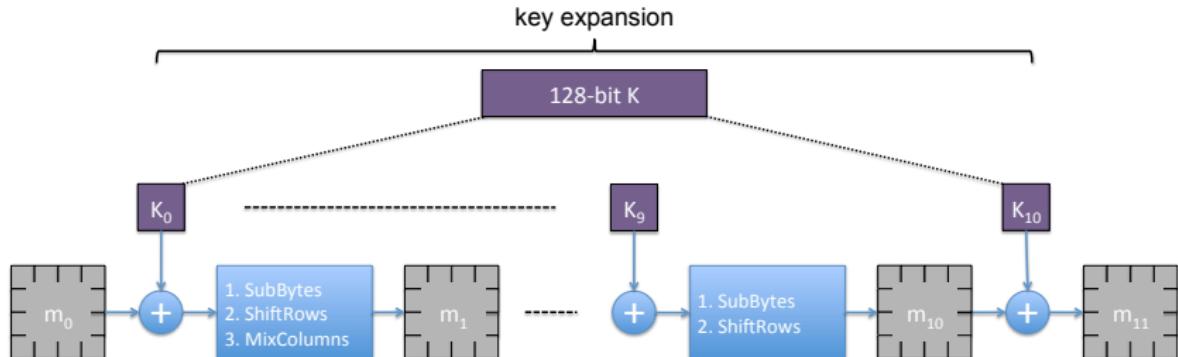
- ▶ Goal: replace 3DES which is too slow (3DES is 3 times as slow as DES)
- ▶ 2001: NIST adopts Rijndael as AES
- ▶ Block size  $\ell = 128$  bits, Key size  $k = 128, 192, 256$  bits
- ▶ AES is Substitution-Permutation network (not a Feistel network)

# AES: encryption circuit



- ▶  $m_i$  :  $4 \times 4$  byte matrix,  $K_i$ : 128-bit key
- ▶  $m_0$ : plaintext,  $m_{11}$ : ciphertext
- ▶ at the last round MixColumns is not applied

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→ As AES is not a Feistel network, each step needs to be reversible!

# AES: SubBytes

---

	x0	x1	x2	x3	x4	x5	x6	x7	x8	x9	xa	xb	xc	xd	xe	xf
0x	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
1x	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
2x	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
3x	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
4x	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
5x	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
6x	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
7x	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
8x	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
9x	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
ax	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
bx	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a	
dx	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
ex	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
fx	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

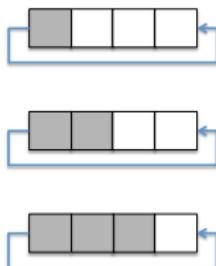
- ▶  $\forall j, k. m'_i[j, k] = S[m_i[j, k]]$
  - ▶ rows: most significant 4 bits
  - ▶ columns: least significant 4 bits
- Note that SubBytes is reversible

# AES: ShiftRows

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$m'_i$

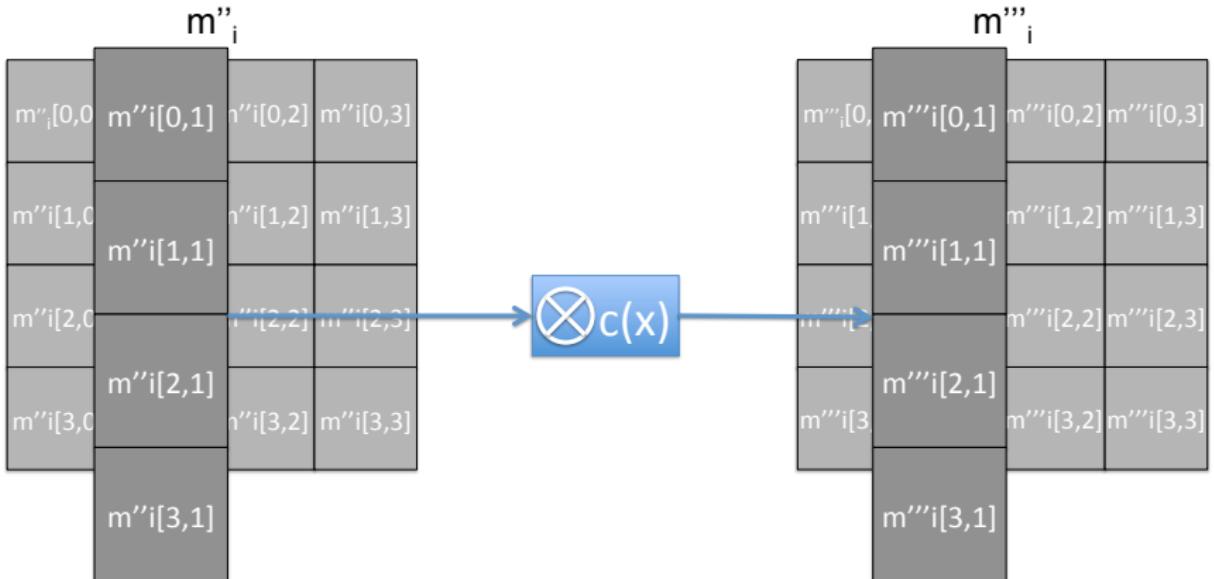
$m'_i[0,0]$	$m'_i[0,1]$	$m'_i[0,2]$	$m'_i[0,3]$
$m'_i[1,0]$	$m'_i[1,1]$	$m'_i[1,2]$	$m'_i[1,3]$
$m'_i[2,0]$	$m'_i[2,1]$	$m'_i[2,2]$	$m'_i[2,3]$
$m'_i[3,0]$	$m'_i[3,1]$	$m'_i[3,2]$	$m'_i[3,3]$



$m''_i$

$m''_i[0,0]$	$m''_i[0,1]$	$m''_i[0,2]$	$m''_i[0,3]$
$m''_i[1,1]$	$m''_i[1,2]$	$m''_i[1,3]$	$m''_i[1,0]$
$m''_i[2,2]$	$m''_i[2,3]$	$m''_i[2,0]$	$m''_i[2,1]$
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# AES: MixColumns



# Attacks on AES

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- ▶ **Related-key attack** on the 192-bit and 256-bit versions of AES: exploits the AES key schedule [A. Biryukov, D. Khovratovich (2009)]  
→ key recovery in time  $\sim 2^{99}$
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→ 4 times faster than exhaustive search
- ⇒ Existing attacks on AES-128 are still not practical, but should use AES-192 and AES-256 in new projects!

# Using block ciphers

**Myrto Arapinis**

School of Informatics  
University of Edinburgh

# Goal

---

Encrypt  $M$  using a block cipher operating on blocks of length  $\ell$   
when  $|M| \neq \ell$

# Padding - $|M| \leq \ell$

---

- ▶ Bit padding - append a *set bit* ('1') at the end of message, and then append as many *reset bits* ('0') required

Example: padding a 52-bits message for a 64-bits block:

11010011 01010110 10010000 00111010 10110101 01011010 11111000 00000000

padding a 64-bits message  $M$  for 64-bits blocks requires adding a padding block:

M|10000000 00000000 00000000 00000000 00000000 00000000 00000000 00000000

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padding a  $8k$ -bytes messages for 8-bytes blocks requires adding a padding block:

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- ▶ PKCS#7 - byte padding - the value of each added byte is the total number of padding bytes. The padding will be 01, or 02 02, or 03 03 03, or 04 04 04 04, etc.

Example: padding a 4-bytes message for 8-bytes blocks:

DD DD DD DD 04 04 04 04

padding a 8-bytes message for 8-bytes blocks requires adding a padding block:

DD DD DD DD DD DD DD DD | 08 08 08 08 08 08 08 08



# Electronic Code Book (ECB) mode

---

$(E, D)$  a block cipher.

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- ▶ Each block  $M_i$  is encrypted under the key  $K$  using the block cipher  
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- ▶ The ciphertext corresponding to  $M$  is the concatenation of the  $C_i$ s  
 $\Rightarrow C = C_1 || C_2 || \dots || C_m$

# Weakness of ECB

---

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---

$m:$    $m_1$   $m_2$   $\dots$   $m_n$

$E_{ECB}(k,m):$    $c_1$   $c_2$   $\dots$   $c_n$

# Weakness of ECB

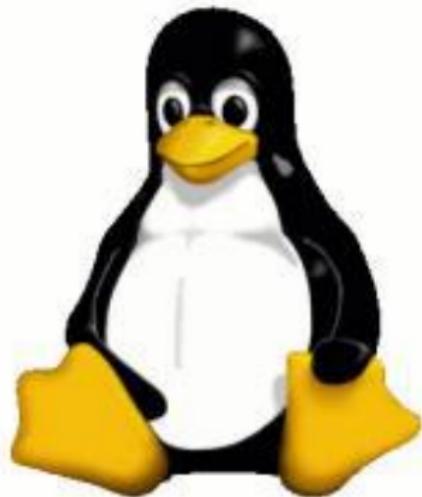
---



Problem:  $\forall i, j. m_i = m_j \Rightarrow c_i = E(k, m_i) = E(k, m_j) = c_j$   
 $\Rightarrow$  Weak to frequency analysis!

# Weakness of ECB in pictures

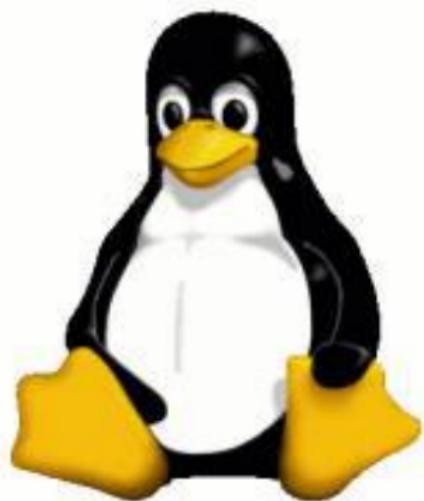
---



Original image

## Weakness of ECB in pictures

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Original image

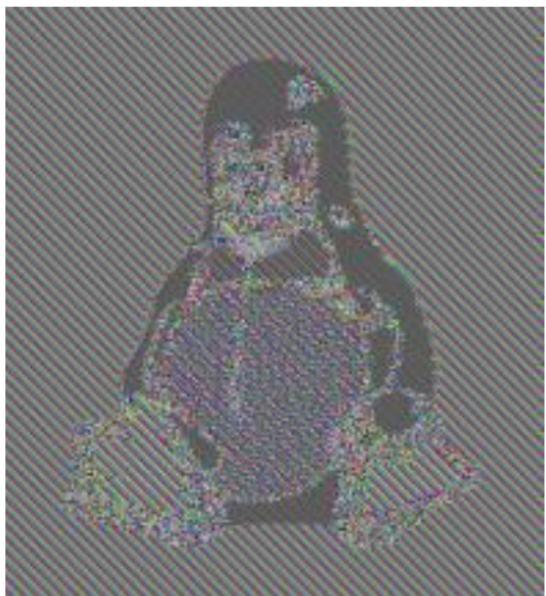


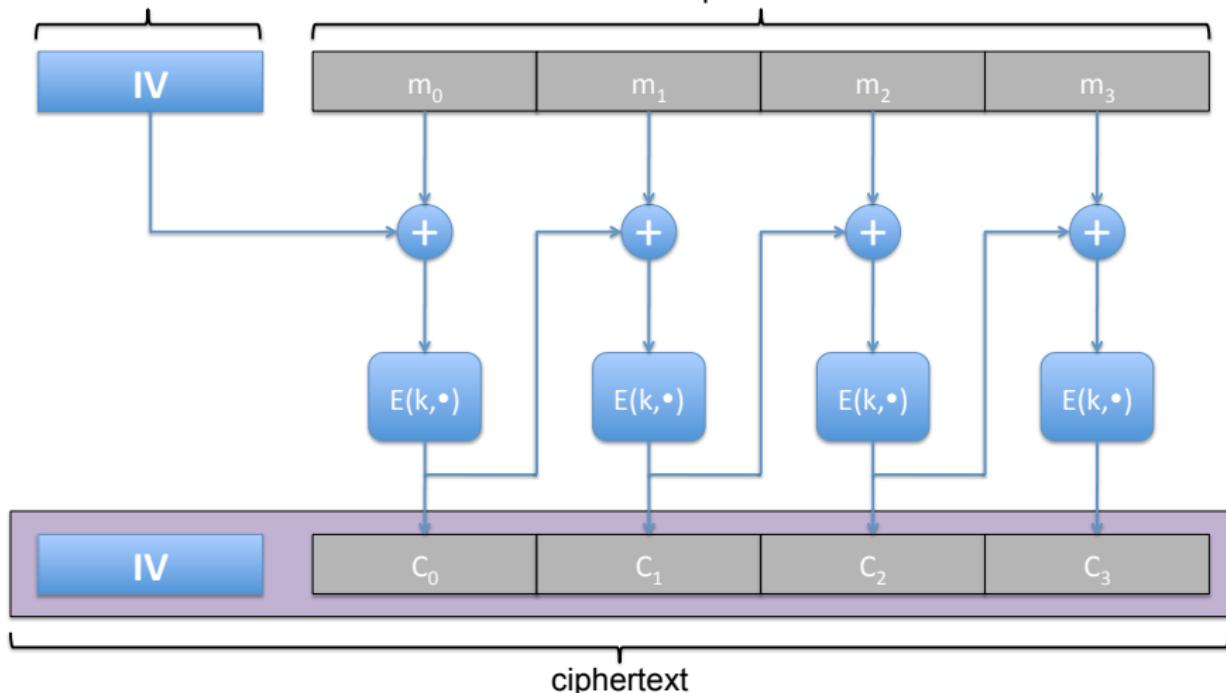
Image encrypted using ECB mode

# Cipher-block chaining (CBC) mode: encryption

$(E, D)$  a block cipher that manipulates blocks of size  $\ell$ .

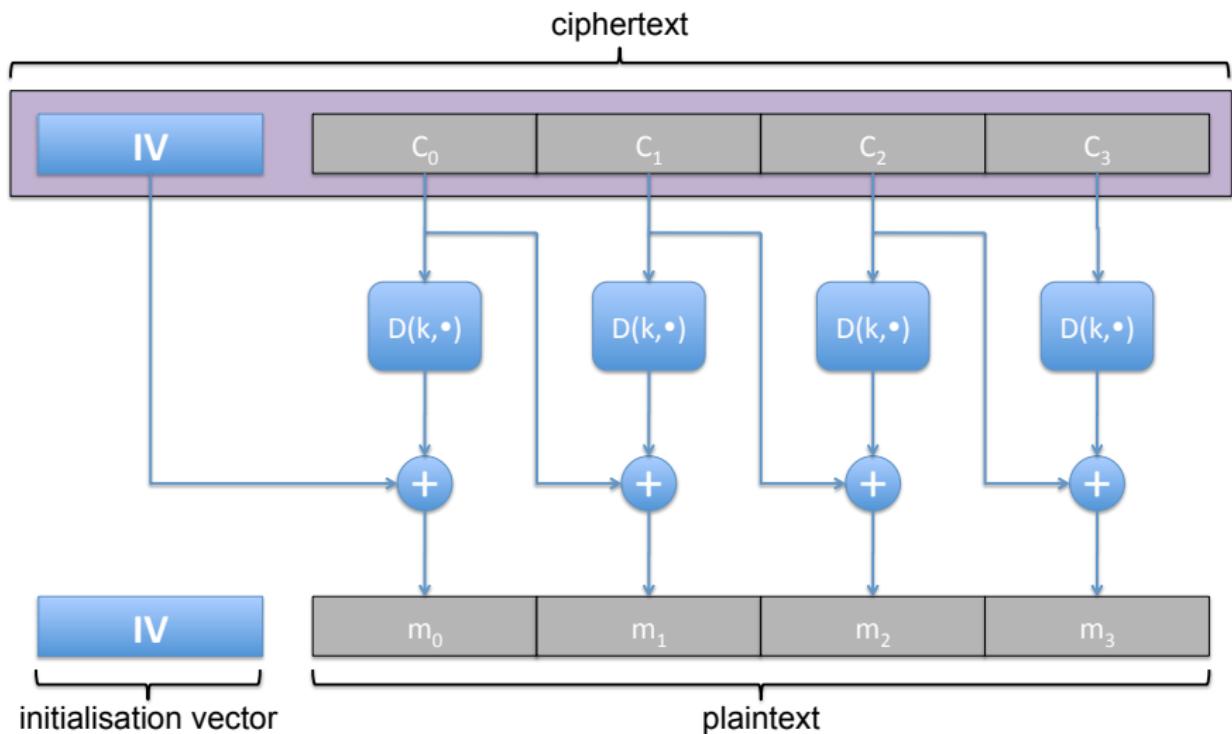
initialisation vector

plaintext



IV chosen at random in  $\{0, 1\}^\ell$

# Cipher-block chaining (CBC) mode: decryption



# Sony PlayStation

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# Sony PlayStation

---

- ▶ Prevent games being copied



# Sony PlayStation

---

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- ▶ CD & full disk encryption



# Sony PlayStation

---

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- ▶ Sony PS used ECB full-disk encryption
- ▶ Hardware controlled user access to data



# Sony PlayStation disk encryption attack

---

- ▶ Remove disk and make copy

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- ▶ Copy a file to the disk
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- ▶ Copy target data to the user area
- ▶ Put disk back in PlayStation and ask for user data
- ▶ PlayStation decrypts the file and gives it to user

# Sweet32: birthday attacks on 64-bit block ciphers in TLS and openVPN

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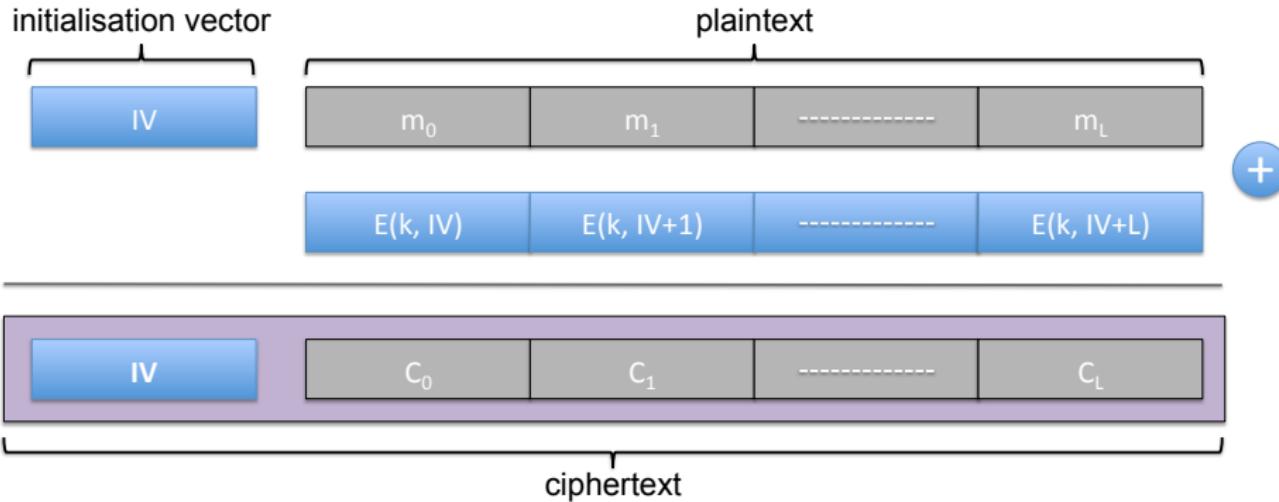
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# Counter (CTR) mode

$(E, D)$  a block cipher that manipulates blocks of size  $\ell$ .



IV chosen at random in  $\{0, 1\}^\ell$