# Cryptography III: Symmetric Ciphers <br> Computer Security Lecture 4 

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26th January 2012

## Outline

Stream ciphers

Block ciphers

DES and Rijndael

Summary

## Stream ciphers and block ciphers

Symmetric-key encryption schemes are often characterised as stream ciphers or block ciphers, but the distinction can be fuzzy.

- A stream cipher is an encryption scheme which treats the plaintext symbol-by-symbol (e.g., by bit or byte);
- security in a stream cipher lies in a changing keystream rather than the encryption function, which may be simple.
- A block cipher is an encryption scheme which breaks up the plaintext message into blocks of a fixed length (e.g., 128 bits), and encrypts one block at a time;
- the block encryption function is a complex function parameterised on a fixed size key.


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## Stream ciphers

Typically, $\mathcal{M}=\mathcal{C}=\mathcal{A}$ and a stream of symbols

$$
m_{1} m_{2} m_{3} \cdots
$$

is encrypted using a keystream

$$
e_{1} e_{2} e_{3} \cdots
$$

to generate

$$
E_{e_{1}}\left(m_{1}\right) E_{e_{2}}\left(m_{2}\right) E_{e_{3}}\left(m_{3}\right) \cdots
$$

Stream ciphers may be

- synchronous (keystream generated independently of the plaintext and ciphertext), or
- self-synchronizing (the keystream is generated as a function of the key and a fixed amount of previous ciphertext).


## Vernam cipher and one-time pad

- The Vernam cipher is a stream cipher defined on the alphabet $\mathcal{A}=\{0,1\}$, with a key stream also of binary digits.
- Each symbol $m_{i}$ in the message is encoded using the corresponding symbol $k_{i}$ of the key stream, using exclusive-or:

$$
c_{i}=m_{i} \oplus k_{i} .
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- Because $(a \oplus b) \oplus b=a$, the decryption operation is identical:

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If the key string is randomly chosen, and never reused, then this cipher is called a one-time pad. Claude Shannon proved that this cipher is unconditionally secure. Unfortunately, to guarantee this, it requires a true random source for key bits (hard to come by), and a key stream as long as the message. This makes it impractical for most applications. It used to be used for high security communications between Washington and Moscow.

## Feedback Shift Registers

- More practical than the one-time pad would be to use a pseudorandom keystream, which is seeded with a much shorter key. Feedback shift registers (FSRs) are the basic component of many keystream generators, used to produce pseudorandom bit streams.
- An FSR of length $n$ consists of $n$ 1-bit register stages connected together, whose contents $\vec{s}$ are inputs to a boolean function $f$. At each tick, the contents are shifted right, and $f$ calculates the feedback digit.

- If the initial state is $\left[s_{n-1}, \ldots, s_{0}\right]$, then the output sequence $s_{0}, s_{1}, \ldots$ is determined by the equation:

$$
s_{j}=f\left(s_{j-1}, s_{j-2}, \ldots s_{j-n}\right) \text { for } j \geq n
$$

## Linear Feedback Shift Registers

- In a $n$-length LFSR, the feedback function $f$ is set by a n-degree connection polynomial $C$ with binary coefficients $c_{i}$

$$
C(X)=1+c_{1} X+c_{2} X^{2} \ldots+c_{n} X^{n}
$$

this determines the feedback function, as:

$$
s_{j}=\left(c_{1} s_{j-1}+c_{2} s_{j-2}+\cdots+c_{n} s_{j-n}\right) \bmod 2 \quad \text { for } j \geq n
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- However, LFSRs are insecure. To break, find the length $n$, and then use a known-plaintext attack of length $2 n$.
- In practice, some controlled non-linearity is added by either non-linear filtering or composition of LFSRs, or LFSR-controlled clocking.


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## Old Time Cryptanalysis

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If I saw anything that looked like a German word I had to stop the machine; someone would come and note the position where I had stopped and transfer the section of script to their machines for further investigation. I did this work from July 1943 to May 1945 and earned \$3 week. I heard people say that they thought it must be very interesting work but in fact I found it extremely boring.

## Simple substitution ciphers

A simple substitution cipher is a block cipher for arbitrary block length $t$. It swaps each letter for another letter, using a permutation of the alphabet.

- Let $\mathcal{A}$ be an alphabet, $\mathcal{M}$ be the set of strings over $\mathcal{A}$ of length $t$, and $\mathcal{K}$ be the set of all permutations on $\mathcal{A}$.


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$$
E_{e}(m)=e\left(m_{1}\right) e\left(m_{2}\right) \cdots e\left(m_{t}\right)=c
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where $m \in \mathcal{M}$ and $m=m_{1} m_{2} \cdots m_{t}$.

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where $m \in \mathcal{M}$ and $m=m_{1} m_{2} \cdots m_{t}$.
For each $d \in \mathcal{K}$ we define $E_{d}$ in exactly the same way,

$$
D_{d}(c)=d\left(c_{1}\right) d\left(c_{2}\right) \cdots d\left(c_{t}\right)
$$

- Key pairs are permutations and their inverses, so $d=e^{-1}$, and

$$
D_{d}(c)=e^{-1}\left(c_{1}\right) e^{-1}\left(c_{2}\right) \cdots e^{-1}\left(c_{t}\right)=m_{1} m_{2} \cdots m_{t}=m .
$$

## Simple substitution ciphers, cont'd

- The Caesar cipher is a simple substitution cipher which replaces $\mathrm{A} \rightarrow \mathrm{D}, \mathrm{B} \rightarrow \mathrm{E}, \mathrm{C} \rightarrow \mathrm{F}, \ldots, \mathrm{X} \rightarrow \mathrm{A}, \mathrm{Y} \rightarrow \mathrm{B}, \mathrm{Z} \rightarrow \mathrm{C}$.


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Simple substitution ciphers are insecure, even when the key space is large. The reason is that the distribution of letter frequencies is preserved in the ciphertext, which allows easy cryptanalysis with a fairly small amount of ciphertext and known properties of plain text (e.g., the relative frequencies of letters in English text).

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## Polyalphabetic substitution ciphers

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where $m=m_{1} m_{2} \cdots m_{t}$.

- The corresponding decryption key is $d=\left(p_{1}^{-1}, \ldots, p_{t}^{-1}\right)$.


## Polyalphabetic substitution ciphers, cont'd

- The Vigenère cipher has a block-length of 3 , and uses the permutations $e=\left(p_{1}, p_{2}, p_{3}\right)$ where $p_{1}$ rotates each letter of the alphabet three places to the right, $p_{2}$ rotates seven positions, and $p_{3}$ ten positions
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\begin{array}{ll}
m & =C O M \text { EON EVE RYB ODY } \\
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Polyalphabetic substitution ciphers have the advantage over simple substitution ciphers that symbol frequencies are not preserved: a single letter may be encrypted to several different letters, in different positions. However, cryptanalysis is still straightforward, by first determining the block size, and then applying frequency analysis by splitting the letters into groups which are encrypted with the same permutation. So polyalphabetic substitutions are certainly not secure.

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This cipher again preserves letter frequencies, which allows easy cryptanalysis. So it is not secure. These block ciphers so far are not useful by themselves, but get interesting when combined. A good cipher should add both confusion by substitution transformations and diffusion by transpositions. Confusion obscures the relationship between the key and the ciphertext. Diffusion spreads out redundancy in the plaintext across the ciphertext. Modern block ciphers apply rounds consisting of substitution and transposition steps.

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- Involutions (functions that are their own inverse) are particularly useful in constructing product ciphers. The favourite is XOR: $f(x)=x \oplus c$.


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- The Feistel principle gives a way of constructing a cipher so that the same circuit is used for both encryption and decryption. A round in a Feistel cipher treats the input block in two halfs, $L_{i}$ and $R_{i}$. It uses the right-hand half to modify the left, and then swaps:

$$
L_{i+1}=R_{i} \quad R_{i+1}=L_{i} \oplus f\left(K_{i}, R_{i}\right)
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## Modes for block ciphers: ECB

- Block ciphers can be used in various modes. Important reading exercise: compare the security, efficiency, inbuilt data integrity, and error recovery of these different modes.
- ECB: electronic codebook mode. Each block of plaintext $x_{j}$ is enciphered independently.

- This is the simplest mode, but it has obvious failings.


## Modes for block ciphers: CBC

- CBC: cipherblock chaining mode. Each plaintext block $x_{j}$ is XORed with the previous ciphertext $c_{j-1}$ block before encryption. An initialization vector (IV) (optionally secret, fresh for each message) is used for $c_{0}$.

$$
c_{j}=E_{k}\left(x_{j} \oplus c_{j-1}\right) \quad x_{j}=c_{j-1} \oplus E_{k}^{-1}\left(c_{j}\right)
$$


(i) encipherment

(ii) decipherment

## Modes for block ciphers: OFB

- OFB: output-feedback mode. Block cipher encryption function used as synchronous stream cipher (internal feedback).

$$
c_{j}=x_{j} \oplus s_{j} ; s_{j}=E_{k}\left(s_{j-1}\right) \quad x_{j}=c_{j} \oplus s_{j} ; s_{j}=E_{k}\left(s_{j-1}\right)
$$



## Modes for block ciphers: CFB

- CFB cipher-feedback mode. Encryption function of block cipher used as self-synchronizing stream cipher for symbols of size up to block size.

$$
c_{j}=x_{j} \oplus E_{k}\left(c_{j-1}\right) \quad x_{j}=c_{j} \oplus E_{k}\left(c_{j-1}\right)
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- Main threat isn't cryptanalytic, but (slightly optimised) exhaustive search in small key-space. Remedied by 3DES (triple DES), 3 keys:

$$
C=E_{k_{3}}\left(D_{k_{2}}\left(E_{k_{1}}(P)\right)\right) \quad P=D_{k_{1}}\left(E_{k_{2}}\left(D_{k_{3}}(C)\right)\right) .
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- Several other DES variants, including DESX, using whitenening keys $k_{1}, k_{2}$ as $C=E_{k}\left(P \oplus k_{1}\right) \oplus k_{2}$. (Used in Win2K encrypting FS).


## Overview of DES internals [FIPS 46-3]



## The Advanced Encryption Standard

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- Rijndael is built as a network of linear transformations and substitutions, with 10,12 or 14 rounds, depending on key size.


## Outline

## Stream ciphers

## Block ciphers

## DES and Rijndael

Summary

## Recent symmetric crypto algorithms

 Stream ciphers
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- Skipjack. NSA designed, once classified (key escrow and LEAF issue) and patented under a secrecy order; now public domain. Block size 64 bits, 80-bit key. Used in tamperproof Clipper and Capstone chips.


## References

The DES diagram is from Smart, Chapter 8 and the block cipher diagrams are from Figure 7.1 in the HAC.

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## Recommended Reading

Chapters 7 and 8 of Smart.

