## Cryptography II: Hash Functions Computer Security Lecture 5

#### Mike Just<sup>1</sup>

School of Informatics University of Edinburgh

25th January 2010

<sup>&</sup>lt;sup>1</sup>Based on original lecture notes by David Aspinall

### Outline

Varieties of hash function

Properties of hash functions

**Building hash functions** 

Standard hash functions

Conclusion

## Outline

#### Varieties of hash function

Properties of hash functions

Building hash functions

Standard hash functions

Conclusion

## Hash function basics

A hash function is a computationally efficient function h: {0, 1}\* → {0, 1}<sup>k</sup> which compresses any arbitrary length binary string to a fixed size k-length binary hash value (or hash for short).

## Hash function basics

- ▶ A hash function is a computationally efficient function  $h : \{0, 1\}^* \rightarrow \{0, 1\}^k$  which compresses any arbitrary length binary string to a fixed size *k*-length binary hash value (or hash for short).
- ► A good hash function distributes values uniformly: the probability that a randomly chosen string s gets mapped to a particular hash y is <sup>1</sup>/<sub>2<sup>k</sup></sub>

# Hash function basics

- ▶ A hash function is a computationally efficient function  $h : \{0, 1\}^* \rightarrow \{0, 1\}^k$  which compresses any arbitrary length binary string to a fixed size *k*-length binary hash value (or hash for short).
- ► A good hash function distributes values uniformly: the probability that a randomly chosen string s gets mapped to a particular hash y is <sup>1</sup>/<sub>2<sup>k</sup></sub>
- A cryptographic hash function must satisfy some further properties, e.g.:
  - 1. it should be difficult to invert;
  - 2. it should be difficult to find a second input that hashes to the same value as another input;
  - 3. it should be difficult to find any two inputs that hash to the same value.

depending on the application.

# Hash function basics . . .

- There are several applications of hash functios
  - Integrity: Alice sends m, h(m) (or alternatively, E<sub>k</sub>(m||h(m))) to Bob. (NB: Don't assume that encryption, on its own, provides confidentiality).
  - Confidentiality: An Authentication Server stores a user's password p as h(p).
  - And others: confirmation of knowledge (e.g., password), key derivation, pseudo-random number generation, ...
- On their own, hash functions don't protect against
  - Malicious repetition of data, e.g., repeating a £100 bank deposit
  - Dishonestly repudiation, e.g., denying sending a hashed email message using a hash function
- Nor do they support message recovery, i.e., recovering the original message after tampering
- Hash functions are intended to protect against malicious modification

# Properties of cryptographic hash functions

#### Preimage Resistance (One-way)

*h* is **preimage resistant** if given a hash value *y*, it is computationally infeasible to find an *x* such that h(x) = y.

# Properties of cryptographic hash functions

#### Preimage Resistance (One-way)

*h* is **preimage resistant** if given a hash value *y*, it is computationally infeasible to find an *x* such that h(x) = y.

#### 2nd Preimage Resistance (Weak Collision Resistance)

*h* is **2nd preimage resistant** if given a value  $x_1$  and its hash  $h(x_1)$ , it is computationally infeasible to find another  $x_2$  such that  $h(x_2) = h(x_1)$ .

# Properties of cryptographic hash functions

#### Preimage Resistance (One-way)

*h* is **preimage resistant** if given a hash value *y*, it is computationally infeasible to find an *x* such that h(x) = y.

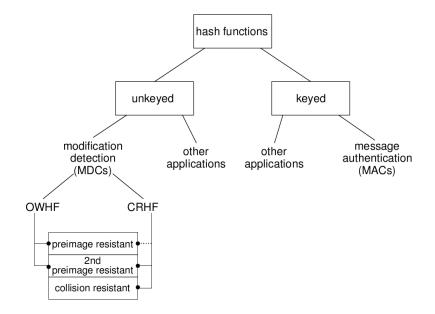
2nd Preimage Resistance (Weak Collision Resistance)

*h* is **2nd preimage resistant** if given a value  $x_1$  and its hash  $h(x_1)$ , it is computationally infeasible to find another  $x_2$  such that  $h(x_2) = h(x_1)$ .

#### (Strong) Collision Resistance

*h* is **collision resistant** if it is computationally infeasible to find *any* two inputs  $x_1$  and  $x_2$  such that  $h(x_1) = h(x_2)$ .

# Hash function Classification [HAC]



# **Modification Detection Codes**

- The main application of hash functions is as Modification Detection Codes to provide data integrity.
- A hash h(x) provides a short message digest, a "fingerprint" of some possibly large data x. If the data is altered, the digest should become invalid.
  - This allows the data (but not the hash!) to be stored in an unsecured place.
  - If x is altered to x', we hope h(x) ≠ h(x'), so it can be detected.
- This is useful especially where malicious alteration is a concern, e.g., software distribution.
- Ordinary hash functions such as CRC-checkers produce *checksums* which are not 2nd preimage resistant: an attacker could produce a hacked version of a software product and ensure the checksum remained the same.

A one-way hash function (OWHF) is a hash function that satisfies preimage resistance and 2nd-preimage resistance.

- A one-way hash function (OWHF) is a hash function that satisfies preimage resistance and 2nd-preimage resistance.
- A collision resistant hash function (CRHF) is a hash function that satisfies 2nd-preimage resistance and collision resistance.

- A one-way hash function (OWHF) is a hash function that satisfies preimage resistance and 2nd-preimage resistance.
- A collision resistant hash function (CRHF) is a hash function that satisfies 2nd-preimage resistance and collision resistance.
- In practice, CRHF usually satisfies preimage resistance.

- A one-way hash function (OWHF) is a hash function that satisfies preimage resistance and 2nd-preimage resistance.
- A collision resistant hash function (CRHF) is a hash function that satisfies 2nd-preimage resistance and collision resistance.
- In practice, CRHF usually satisfies preimage resistance.
- CRHFs are harder to construct than OWHFs and have longer length hash values.

- A one-way hash function (OWHF) is a hash function that satisfies preimage resistance and 2nd-preimage resistance.
- A collision resistant hash function (CRHF) is a hash function that satisfies 2nd-preimage resistance and collision resistance.
- In practice, CRHF usually satisfies preimage resistance.
- CRHFs are harder to construct than OWHFs and have longer length hash values.
- Choice between OWHF and CRHF depends on application:

- A one-way hash function (OWHF) is a hash function that satisfies preimage resistance and 2nd-preimage resistance.
- A collision resistant hash function (CRHF) is a hash function that satisfies 2nd-preimage resistance and collision resistance.
- In practice, CRHF usually satisfies preimage resistance.
- CRHFs are harder to construct than OWHFs and have longer length hash values.
- Choice between OWHF and CRHF depends on application:
  - If attacker can control input, CRHF required.

- A one-way hash function (OWHF) is a hash function that satisfies preimage resistance and 2nd-preimage resistance.
- A collision resistant hash function (CRHF) is a hash function that satisfies 2nd-preimage resistance and collision resistance.
- In practice, CRHF usually satisfies preimage resistance.
- CRHFs are harder to construct than OWHFs and have longer length hash values.
- Choice between OWHF and CRHF depends on application:
  - If attacker can control input, CRHF required.
  - Otherwise OWHF suffices

- A one-way hash function (OWHF) is a hash function that satisfies preimage resistance and 2nd-preimage resistance.
- A collision resistant hash function (CRHF) is a hash function that satisfies 2nd-preimage resistance and collision resistance.
- In practice, CRHF usually satisfies preimage resistance.
- CRHFs are harder to construct than OWHFs and have longer length hash values.
- Choice between OWHF and CRHF depends on application:
  - If attacker can control input, CRHF required.
  - Otherwise OWHF suffices
- **Ex**: which is needed for password file security?

### Message Authentication Codes

- Message Authentication Codes are keyed hash functions, indexed with a secret key.
  - As well as data integrity, they provide data-origin authentication, because it is assumed that apart from the recipient, only the sender knows the secret key necessary to compute the MAC.
- A MAC is a key-indexed family of hash functions,  $\{h_k \mid k \in \mathcal{K}\}$ . MACs must satisfy a *computation* resistance property.

#### **Computation Resistance**

Given a set of pairs  $(x_i, h_k(x_i))$  it is computationally infeasible to find any other text-MAC pair  $(x, k_k(x))$  for a new input  $x \neq x_i$ .

## Outline

Varieties of hash function

#### Properties of hash functions

**Building hash functions** 

Standard hash functions

Conclusion

 Collision resistance implies 2nd-preimage resistance.

- Collision resistance implies 2nd-preimage resistance.
- Sketch proof [HAC]:

- Collision resistance implies 2nd-preimage resistance.
- Sketch proof [HAC]:
  - Let h be CR, but suppose it is not 2nd Pl.

- Collision resistance implies 2nd-preimage resistance.
- Sketch proof [HAC]:
  - Let h be CR, but suppose it is not 2nd Pl.
  - Fix some input x; compute h(x).

- Collision resistance implies 2nd-preimage resistance.
- Sketch proof [HAC]:
  - Let h be CR, but suppose it is not 2nd Pl.
  - Fix some input x; compute h(x).
  - Since not 2nd PI, we can find an  $x' \neq x$  with h(x') = h(x).

- Collision resistance implies 2nd-preimage resistance.
- Sketch proof [HAC]:
  - Let h be CR, but suppose it is not 2nd Pl.
  - Fix some input x; compute h(x).
  - Since not 2nd PI, we can find an  $x' \neq x$  with h(x') = h(x).
  - But now (x, x') is a collision, so h cannot be CR.

- Collision resistance implies 2nd-preimage resistance.
- Sketch proof [HAC]:
  - Let h be CR, but suppose it is not 2nd PI.
  - Fix some input x; compute h(x).
  - Since not 2nd PI, we can find an  $x' \neq x$  with h(x') = h(x).
  - But now (x, x') is a collision, so h cannot be CR.
- This and similar arguments (e.g., see Smart) can be made precise using the Random Oracle Model.

- Collision resistance implies 2nd-preimage resistance.
- Sketch proof [HAC]:
  - Let h be CR, but suppose it is not 2nd PI.
  - Fix some input x; compute h(x).
  - Since not 2nd PI, we can find an  $x' \neq x$  with h(x') = h(x).
  - But now (x, x') is a collision, so h cannot be CR.
- This and similar arguments (e.g., see Smart) can be made precise using the Random Oracle Model.

#### Collision resistance does not imply preimage resistance

- Collision resistance implies 2nd-preimage resistance.
- Sketch proof [HAC]:
  - Let h be CR, but suppose it is not 2nd Pl.
  - Fix some input x; compute h(x).
  - Since not 2nd PI, we can find an  $x' \neq x$  with h(x') = h(x).
  - But now (x, x') is a collision, so h cannot be CR.
- This and similar arguments (e.g., see Smart) can be made precise using the Random Oracle Model.

#### Collision resistance does not imply preimage resistance

Contrived counterexample:

$$h(x) = \begin{cases} 1 \mid \mid x & \text{if } x \text{ has length } n \\ 0 \mid \mid g(x) & \text{otherwise} \end{cases}$$

To satisfy (strong) collision resistance, a hash function must be large enough to withstand a birthday attack. (or square root attack).

- To satisfy (strong) collision resistance, a hash function must be large enough to withstand a birthday attack. (or square root attack).
- Drawing random elements with replacement from a set of k elements, a repeat is likely after about  $\sqrt{k}$  selections.

- To satisfy (strong) collision resistance, a hash function must be large enough to withstand a birthday attack. (or square root attack).
- Drawing random elements with replacement from a set of k elements, a repeat is likely after about  $\sqrt{k}$  selections.
- Mallory has two contracts, one for £1000, the other £100,000, to be signed with a 64-bit hash. He makes 2<sup>32</sup> minor variations in each (e.g spaces/control chars), and finds a pair with the same hash. Later claims second document was signed, not first.

- To satisfy (strong) collision resistance, a hash function must be large enough to withstand a birthday attack. (or square root attack).
- Drawing random elements with replacement from a set of k elements, a repeat is likely after about  $\sqrt{k}$  selections.
- Mallory has two contracts, one for £1000, the other £100,000, to be signed with a 64-bit hash. He makes 2<sup>32</sup> minor variations in each (e.g spaces/control chars), and finds a pair with the same hash. Later claims second document was signed, not first.
- An *n*-bit unkeyed hash function has **ideal security** if producing a preimage or 2nd-preimage each requires 2<sup>n</sup> operations, and producing a collision requires 2<sup>n/2</sup> operations.

## Outline

Varieties of hash function

Properties of hash functions

**Building hash functions** 

Standard hash functions

Conclusion

Multiplication of large primes is a OWF

#### Multiplication of large primes is a OWF

 for appropriate choices of p and q, f(p, q) = pq is a one-way function since *integer factorization* [FACTORING] is difficult.

#### Multiplication of large primes is a OWF

- for appropriate choices of p and q, f(p, q) = pq is a one-way function since *integer factorization* [FACTORING] is difficult.
- Not feasible to turn into an MD function, though. (Ex: why?)

#### Multiplication of large primes is a OWF

- for appropriate choices of p and q, f(p, q) = pq is a one-way function since *integer factorization* [FACTORING] is difficult.
- Not feasible to turn into an MD function, though. (Ex: why?)
- Exponentiation in finite fields is a OWF

#### Multiplication of large primes is a OWF

- for appropriate choices of p and q, f(p, q) = pq is a one-way function since integer factorization [FACTORING] is difficult.
- Not feasible to turn into an MD function, though. (Ex: why?)

### Exponentiation in finite fields is a OWF

for appropriate primes p and numbers α,
 f(x) = α<sup>x</sup> mod p is a one-way function, since the discrete logarithm problem [DLP] is difficult.

#### Multiplication of large primes is a OWF

- for appropriate choices of p and q, f(p, q) = pq is a one-way function since *integer factorization* [FACTORING] is difficult.
- Not feasible to turn into an MD function, though. (Ex: why?)

### Exponentiation in finite fields is a OWF

- for appropriate primes p and numbers α,
   f(x) = α<sup>x</sup> mod p is a one-way function, since the discrete logarithm problem [DLP] is difficult.
- Main problem with turning this into a realistic MD function is that it's too slow to calculate.

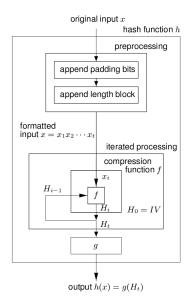
# OWFs from block ciphers

- A block cipher is an encryption scheme which works on fixed length blocks of input text.
- We can construct a OWF from a block cipher such as DES, which is treated essentially as a random function:

$$h(x) = E_k(x) \oplus x$$

for fixed key k. This can be turned into a MD function, by iteration...

## Iterated hash function construction [HAC]



An iterated hash function is constructed using a compression function f which converts a t + n-bit input into an n-bit output.

- An iterated hash function is constructed using a compression function f which converts a t + n-bit input into an n-bit output.
  - The input x is split into blocks x<sub>1</sub>x<sub>2</sub>,...x<sub>k</sub> of size t, appending padding bits and a *length block* indicating the original length.

$$H_0 = IV$$
  $H_i = f(H_{i-1}, x_i), \ 1 \le i \le k$   $h(x) = g(H_k).$ 

- An iterated hash function is constructed using a compression function f which converts a t + n-bit input into an n-bit output.
  - The input x is split into blocks x<sub>1</sub>x<sub>2</sub>,...x<sub>k</sub> of size t, appending padding bits and a *length block* indicating the original length.

$$H_0 = IV$$
  $H_i = f(H_{i-1}, x_i), \ 1 \le i \le k$   $h(x) = g(H_k).$ 

 IV: an initialization vector; g: an output transformation (often identity).

- An iterated hash function is constructed using a compression function f which converts a t + n-bit input into an n-bit output.
  - The input x is split into blocks x<sub>1</sub>x<sub>2</sub>,...x<sub>k</sub> of size t, appending padding bits and a *length block* indicating the original length.

$$H_0 = IV$$
  $H_i = f(H_{i-1}, x_i), \ 1 \le i \le k$   $h(x) = g(H_k).$ 

- IV: an initialization vector; g: an output transformation (often identity).
- This is Merkle's meta-method

- An iterated hash function is constructed using a compression function f which converts a t + n-bit input into an n-bit output.
  - The input x is split into blocks x<sub>1</sub>x<sub>2</sub>,...x<sub>k</sub> of size t, appending padding bits and a *length block* indicating the original length.

 $H_0 = IV$   $H_i = f(H_{i-1}, x_i), \ 1 \le i \le k$   $h(x) = g(H_k).$ 

 IV: an initialization vector; g: an output transformation (often identity).

### This is Merkle's meta-method

 Fact: any CR compression function f can be extended to a CRHF by the above construction, and

- An iterated hash function is constructed using a compression function f which converts a t + n-bit input into an n-bit output.
  - The input x is split into blocks x<sub>1</sub>x<sub>2</sub>,...x<sub>k</sub> of size t, appending padding bits and a *length block* indicating the original length.

 $H_0 = IV$   $H_i = f(H_{i-1}, x_i), \ 1 \le i \le k$   $h(x) = g(H_k).$ 

 IV: an initialization vector; g: an output transformation (often identity).

### This is Merkle's meta-method

- Fact: any CR compression function f can be extended to a CRHF by the above construction, and
- padding: the last block with 0s, adding a final extra block x<sub>k</sub> which holds right-justified binary representation of length(x) (this padding is called **MD strengthening**).

- An iterated hash function is constructed using a compression function f which converts a t + n-bit input into an n-bit output.
  - The input x is split into blocks x<sub>1</sub>x<sub>2</sub>,...x<sub>k</sub> of size t, appending padding bits and a *length block* indicating the original length.

 $H_0 = IV$   $H_i = f(H_{i-1}, x_i), \ 1 \le i \le k$   $h(x) = g(H_k).$ 

 IV: an initialization vector; g: an output transformation (often identity).

#### This is Merkle's meta-method

- Fact: any CR compression function f can be extended to a CRHF by the above construction, and
- padding: the last block with 0s, adding a final extra block x<sub>k</sub> which holds right-justified binary representation of length(x) (this padding is called **MD strengthening**).
- Set  $IV = 0^n$ , g = id, and compute  $H_i = f(H_{i-1}, x_i)$ .

### Outline

Varieties of hash function

Properties of hash functions

**Building hash functions** 

Standard hash functions

Conclusion

# MD5

- Improvement of MD4; MD4 and MD5 designed by Ron Rivest.
  - Text processed in 512-bit blocks, as 16 32-bit sub-blocks. Output is four 32-bit blocks, giving a 128-bit hash. Message padded with 1 and then 0s until last block is 448 bits long, then a 64-bit length.

# MD5

- Improvement of MD4; MD4 and MD5 designed by Ron Rivest.
  - Text processed in 512-bit blocks, as 16 32-bit sub-blocks. Output is four 32-bit blocks, giving a 128-bit hash. Message padded with 1 and then 0s until last block is 448 bits long, then a 64-bit length.
  - Main loop has four rounds, chaining 4 variables a, b, c, d. Each round uses a different operation (with a similar structure) 16 times, which computes a new value of one of the four variables using a non-linear function of the other three, chosen to preserve randomness properties of the input.

# MD5

- Improvement of MD4; MD4 and MD5 designed by Ron Rivest.
  - Text processed in 512-bit blocks, as 16 32-bit sub-blocks. Output is four 32-bit blocks, giving a 128-bit hash. Message padded with 1 and then 0s until last block is 448 bits long, then a 64-bit length.
  - Main loop has four rounds, chaining 4 variables a, b, c, d. Each round uses a different operation (with a similar structure) 16 times, which computes a new value of one of the four variables using a non-linear function of the other three, chosen to preserve randomness properties of the input.
  - For example, the first round uses the operation:

$$a = (F(b, c, d) + x_i + t_j) <<< s$$
  
$$F(b, c, d) = (b \land c) \lor (\neg b \land d)$$

where <<< s is left-circular shift of s bits,  $x_i$  is the *i*th sub-block of the message. Constants  $t_j$  are the integer part of  $2^{32} * abs(sin(i + 1))$  where  $0 \le i \le 63$  is in radians (for the 4 \* 16 steps).

# SHA-1 (160)

 Secure Hash Algorithm (rev 1) is a NIST standard [FIPS 180] also based on MD4. Five 32-bit blocks are chained; output is 160 bits. Message blocks 512 bits. Padding like MD5.

# SHA-1 (160)

- Secure Hash Algorithm (rev 1) is a NIST standard [FIPS 180] also based on MD4. Five 32-bit blocks are chained; output is 160 bits. Message blocks 512 bits. Padding like MD5.
  - Main loop has four rounds of 20 operations, chaining 5 variables a, b, c, d, e, f. Five IVs and four constants are used:
    - $A = 0 \times 67452301$  $B = 0 \times EFCDAB89$  $C = 0 \times 98BADCFE$  $D = 0 \times 10325476$  $E = 0 \times C3D2E1F0$  $K_0 = 0 \times 5A827999$  $K_1 = 0 \times 6ED9EBA1$  $K_2 = 0 \times 8F1BBCDC$  $K_3 = 0 \times CA62C1D6$

# SHA-1 (160)

- Secure Hash Algorithm (rev 1) is a NIST standard [FIPS 180] also based on MD4. Five 32-bit blocks are chained; output is 160 bits. Message blocks 512 bits. Padding like MD5.
  - Main loop has four rounds of 20 operations, chaining 5 variables a, b, c, d, e, f. Five IVs and four constants are used:
    - $\begin{array}{ll} A = 0 \times 67452301 \\ B = 0 \times EFCDAB89 \\ C = 0 \times 98BADCFE \\ D = 0 \times 10325476 \\ E = 0 \times C3D2E1F0 \end{array} \begin{array}{ll} K_0 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_2 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_2 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_2 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_2 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_2 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_2 = 0 \times 5A827999 \\ K_2 = 0 \times 5A827999 \\ K_1 = 0 \times 5A827999 \\ K_2 = 0 \times 5A82799 \\ K_3 = 0 \times 5A8279 \\ K_4 = 0 \times 5A8279 \\ K_5 = 0 \times 5A8279 \\$
  - The message block undergoes an expansion transformation from 16\*32-bit words x<sub>i</sub> to 80\*32-bit words, w<sub>i</sub> by:

$$\begin{array}{ll} w_i &= x_i, & \text{for } 0 \leq i \leq 15. \\ w_i &= (w_{i-3} \oplus w_{i-8} \oplus & \\ & w_{i-14} \oplus w_{i-16}) <<<1, & \text{for } 16 \leq i \leq 79. \end{array}$$

80 steps in main loop, changing Ks and Fs 4 times

80 steps in main loop, changing Ks and Fs 4 times

80 steps in main loop, changing Ks and Fs 4 times

Where 
$$j = i/20$$
:  
**for**( $i = 0$ ;  $i < 80$ ;  $i++$ ) {  
 $tmp = (a <<<5) + F_j(b, c, d) + e + w_i + K_j;$   
 $e = d;$   
 $c = b <<<30;$   
 $b = a;$   
 $a = tmp;$   
}

Each F<sub>j</sub> combines three of the five variables:

$$\begin{array}{rcl} F_0(X,Y,Z) &=& (X \wedge Y) \vee (\neg X \wedge Z) \\ F_1(X,Y,Z) &=& X \oplus Y \oplus Z \\ F_2(X,Y,Z) &=& (X \wedge Y) \vee (X \wedge Z) \vee (Y \wedge Z) \\ F_3(X,Y,Z) &=& X \oplus Y \oplus Z \end{array}$$

80 steps in main loop, changing Ks and Fs 4 times

Each F<sub>j</sub> combines three of the five variables:

$$F_0(X, Y, Z) = (X \land Y) \lor (\neg X \land Z)$$
  

$$F_1(X, Y, Z) = X \oplus Y \oplus Z$$
  

$$F_2(X, Y, Z) = (X \land Y) \lor (X \land Z) \lor (Y \land Z)$$
  

$$F_3(X, Y, Z) = X \oplus Y \oplus Z$$

 Finally a, b, c, d, e are added to tmp (all addition is modulo 2<sup>32</sup>).

80 steps in main loop, changing Ks and Fs 4 times

Each F<sub>j</sub> combines three of the five variables:

$$F_0(X, Y, Z) = (X \land Y) \lor (\neg X \land Z)$$
  

$$F_1(X, Y, Z) = X \oplus Y \oplus Z$$
  

$$F_2(X, Y, Z) = (X \land Y) \lor (X \land Z) \lor (Y \land Z)$$
  

$$F_3(X, Y, Z) = X \oplus Y \oplus Z$$

- Finally a, b, c, d, e are added to tmp (all addition is modulo 2<sup>32</sup>).
- Exercise: implement SHA-1 in your favourite language following this. Test against sha1sum.

### Outline

Varieties of hash function

Properties of hash functions

Building hash functions

Standard hash functions

Conclusion

# **Current Status**

- Hash functions are versatile and powerful primitive.
- However, difficult to construct and less researched than encryption schemes.
  - ideal hash function is a "random mapping" where knowledge of previous results doesn't give knowledge of another.
  - practical fast iterative hash constructions fail this!
  - MD4 (1998), MD5 (1993/2005), SHA-1 (2005) are now all considered broken.
- The US National Institute of Standards and Technology (NIST) has since developed a set of newer hash functions.
  - Formerly called SHA-2, they are denoted by their output size: SHA-256, SHA-384, SHA-512.
  - However, since they are based upon the same SHA construction, they are not long-term solutions
  - NIST is currently running a SHA-3 competition to determine the successor.

### References

嗪 A. J. Menezes, P. C. Van Oorschot, S. A. Vanstone, eds. Handbook of Applied Cryptography. CRC Press, 1997. Online:

http://www.cacr.math.uwaterloo.ca/hac.



Neils Ferguson and Bruce Schneier. Practical Cryptography. John Wiley & Sons, 2003.

Douglas R Stinson. Cryptography Theory and Practice. CRC Press, second edition edition, 2002.

Nigel Smart. Cryptography: An Introduction.

McGraw-Hill, 2003. Third edition online: http://www.cs.bris.ac.uk/~nigel/Crypto\_Book/

#### **Recommended Reading**

One of: Ch 9 of HAC (9.1–9.2); Ch. 10 of Smart 3rd Ed; 11.1–11.3 of Gollmann.