

## LISSOM Orientation Maps

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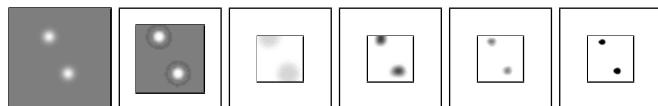
## Modeling Orientation

- Starting point: Retinotopy model
- Same architecture, different input pattern
- Three dimensions of variance: x, y, orientation
- How will that fit into a 2D map?

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## Retinotopy input and response



Retinal activation	LGN response	Iteration 0: Initial V1 response	Iteration 0: Settled V1 response	10,000: Initial V1 response	10,000: Settled V1 response
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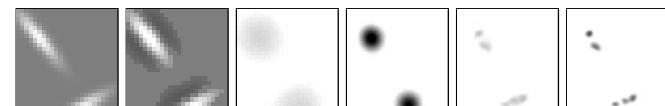
CMVC figure 4.4

(Reminder from last time)

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## Orientation input and response



Retinal activation	LGN response	Iteration 0: Initial V1 response	Iteration 0: Settled V1 response	10,000: Initial V1 response	10,000: Settled V1 response
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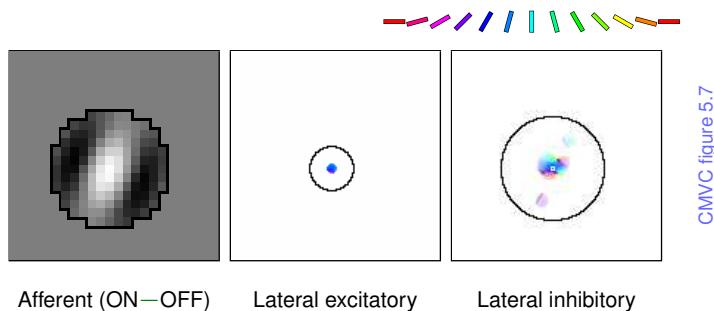
CMVC figure 5.6

- Multiple activity blobs per input pattern:  
orientation-specific

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## Self-organized V1 weights



CMVC figure 5.7

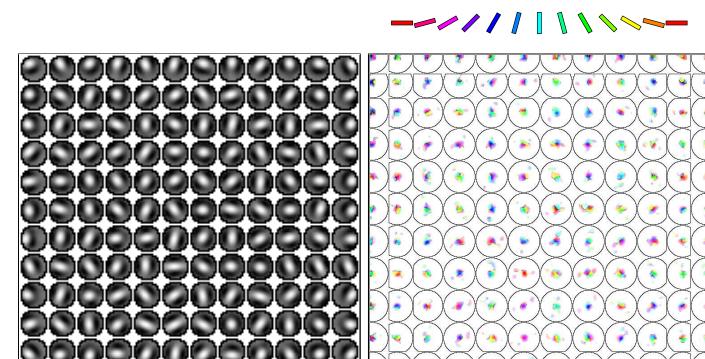
Typical:

- Gabor-like afferent CF
- Nearly uniform short-range lateral excitatory
- Patchy, orientation-specific long-range lateral inhibitory

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## Self-organized weights across V1

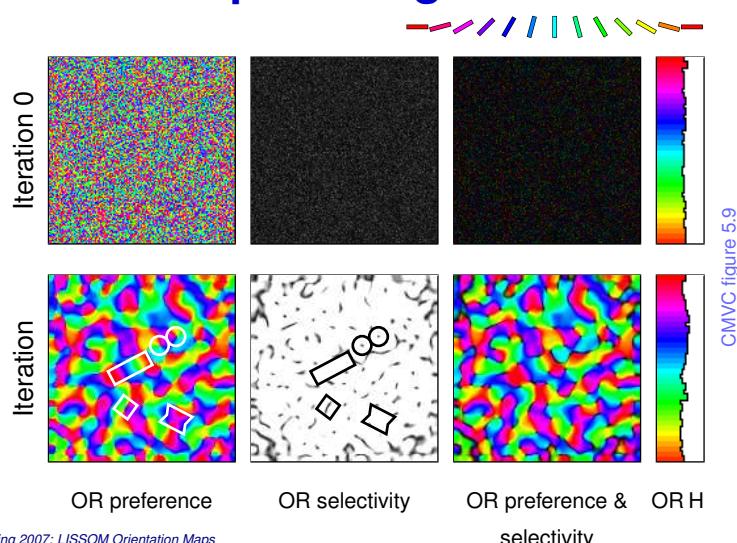


CMVC figure 5.8

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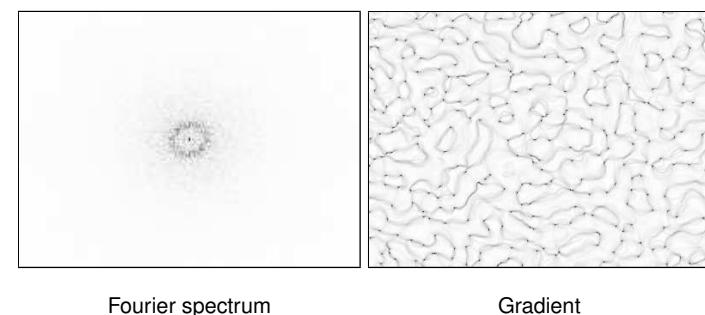
## OR map self-organization



CMVC figure 5.9

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## Macaque ORmap: Fourier,gradient



CMVC figure 5.1

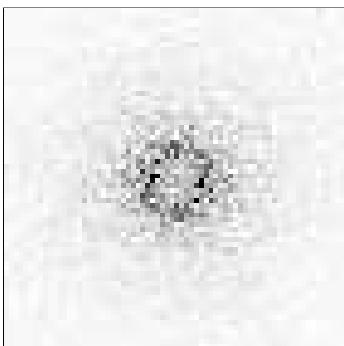
In monkeys:

- Ring-shaped spectrum: repeats regularly in all directions
- High gradient at fractures, pinwheels.

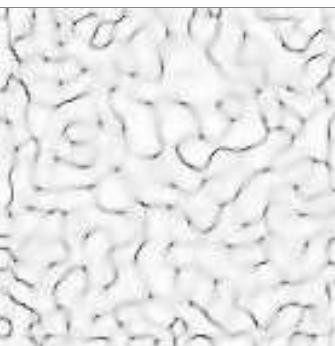
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## OR Map: Fourier, gradient



Fourier spectrum

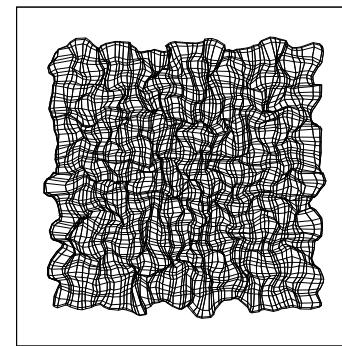


Gradient

LISSOM model has similar spectrum, gradient

CMVC figure 5.10

## OR Map: Retinotopic organization



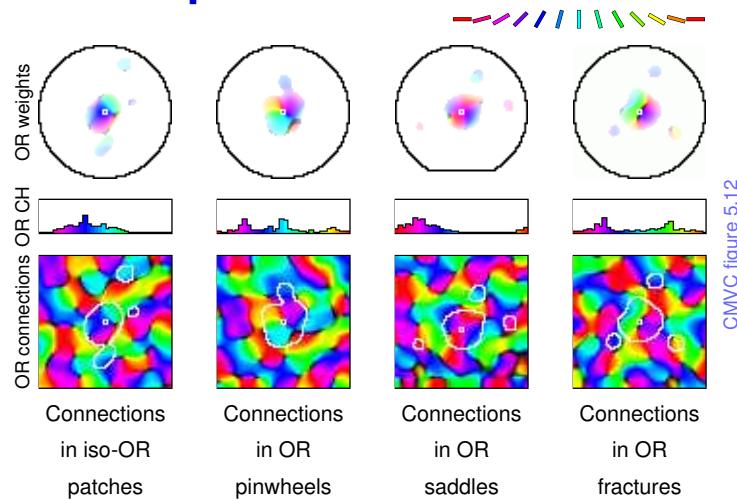
CMVC figure 5.11

- Retinotopy is distorted locally by orientation prefs
- Matches distortions found in animal maps?

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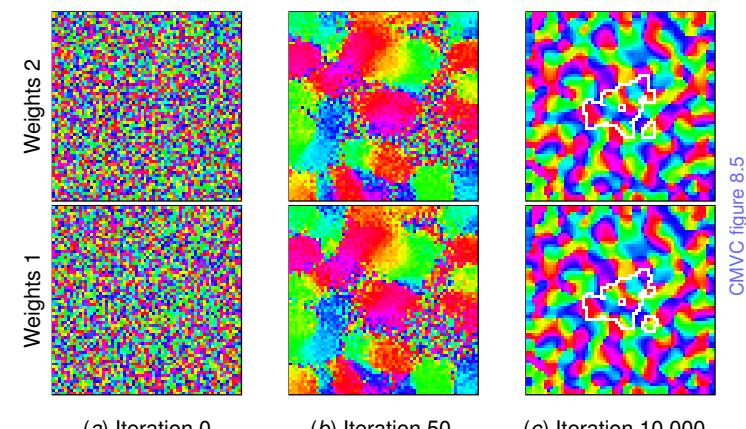
## OR Map: Lateral connections



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## Effect of initial weights

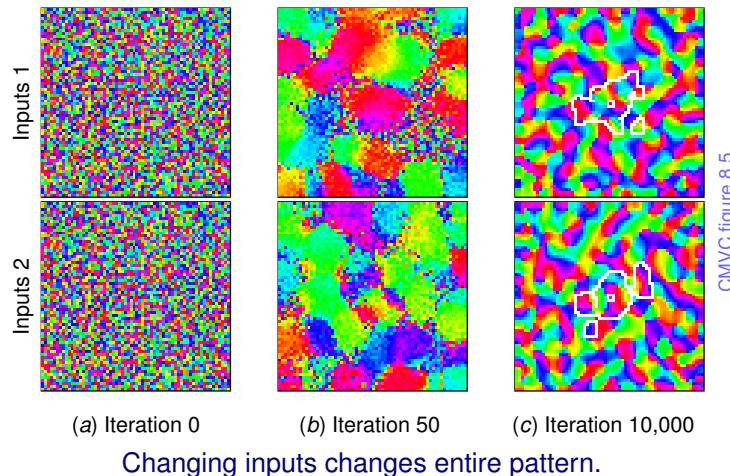


Changing weights doesn't change map folding pattern.

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## Effect of input streams

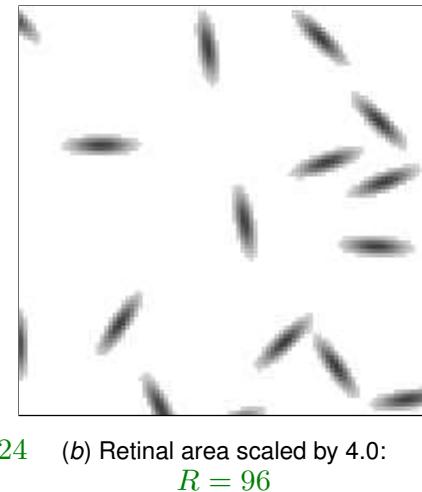


CMVC figure 8.5

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## Scaling retinal and cortical area

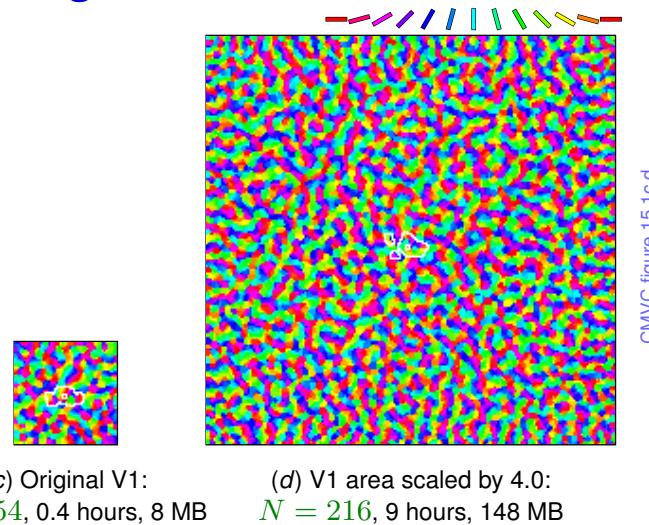


CMVC figure 15.1a,b

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## Scaling retinal and cortical area

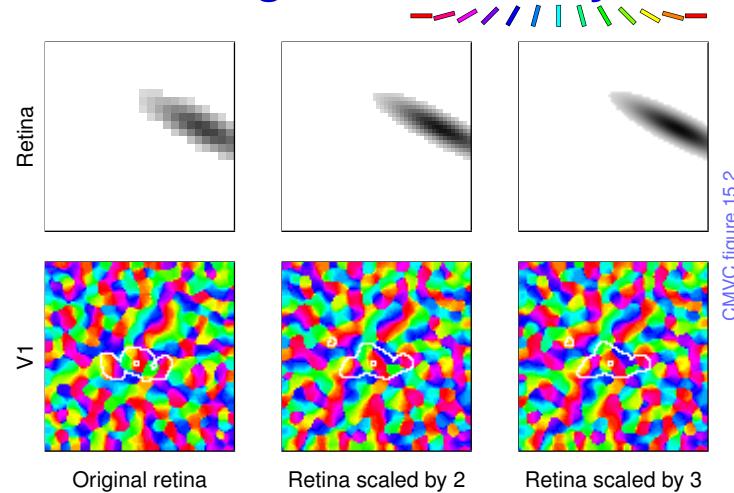


CMVC figure 15.1c,d

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## Scaling retinal density

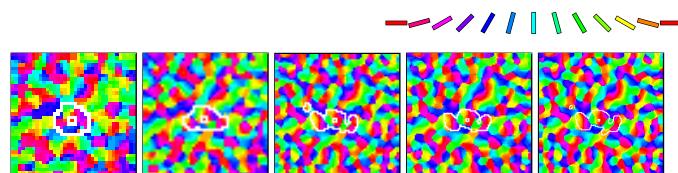


CMVC figure 15.2

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## Scaling cortical density

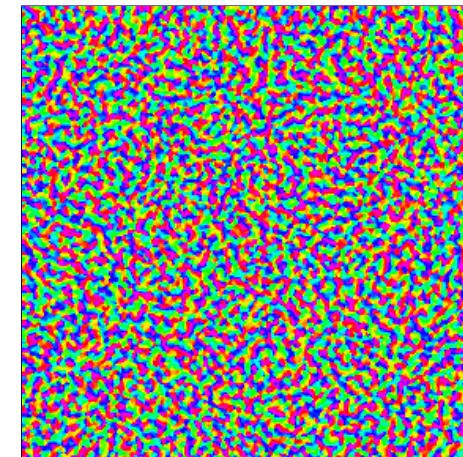


(a)  $36 \times 36$ : 0.17 hours, 2.0 MB  
(b)  $48 \times 48$ : 0.32 hours, 5.2 MB  
(c)  $72 \times 72$ : 0.77 hours, 22 MB  
(d)  $96 \times 96$ : 1.73 hours, 65 MB  
(e)  $144 \times 144$ : 5.13 hours, 317 MB

Above minimum density (due to lateral radii),  
density not crucial for organization

CMVC figure 15.3

## Full-size V1 Map

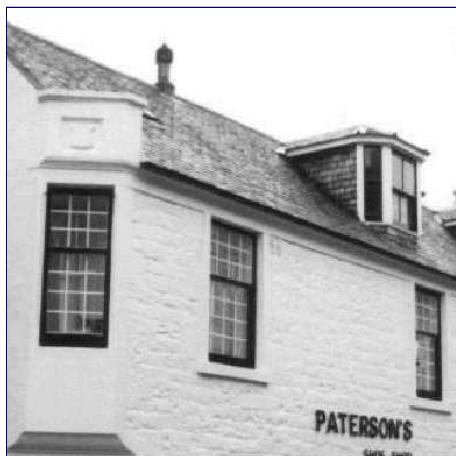


- Map scaled to cover most of visual field
- Allows testing with full-size images
- 30 million connections

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## Sample Image



## LGN Response



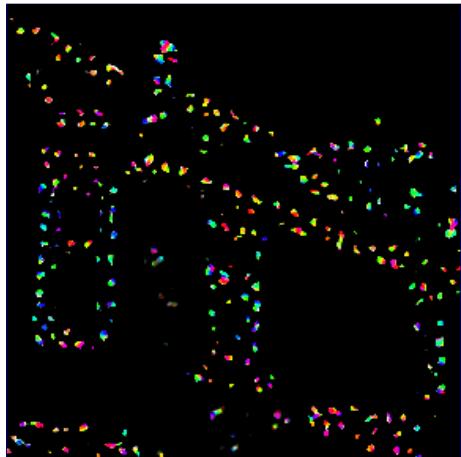
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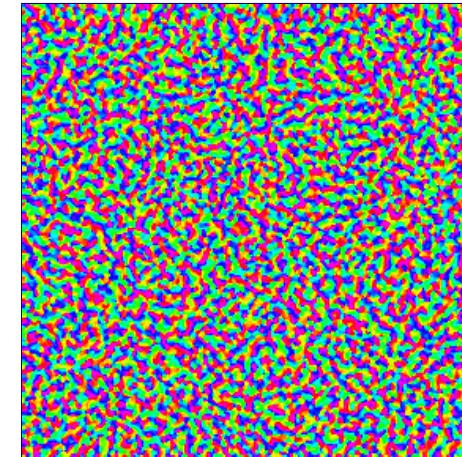
## V1 Response with $\gamma_n$



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## V1 Orientation Map



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## Afferent normalization

Mechanism for contrast invariant tuning:

$$s_{ij} = \frac{\gamma_A \left( \sum_{\rho ab} \xi_{\rho ab} A_{\rho ab, ij} \right)}{1 + \gamma_n \left( \sum_{\rho ab} \xi_{\rho ab} \right)}, \quad (1)$$

$\xi_{\rho ab}$ : activation of unit  $(a, b)$  in afferent RF  $\rho$  of neuron  $(i, j)$

$A_{ab,ij}$  is the corresponding afferent weight

$\gamma_A, \gamma_n$  are constant scaling factors

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## LGN response to large image



Retinal activation



LGN response

LGN responds to most of the visible contours

CMVC figure 8.2a,b

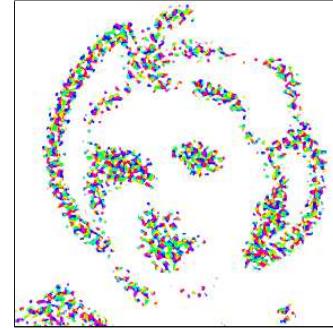
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## V1 without afferent normalization



V1 response:  
 $\gamma_n = 0, \gamma_A = 3.25$



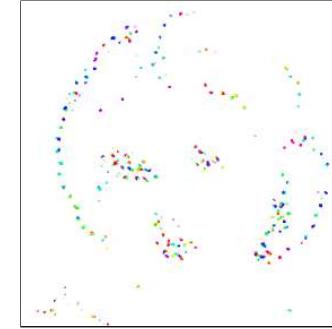
V1 response:  
 $\gamma_n = 0, \gamma_A = 7.5$

Cannot get selective response to all contours

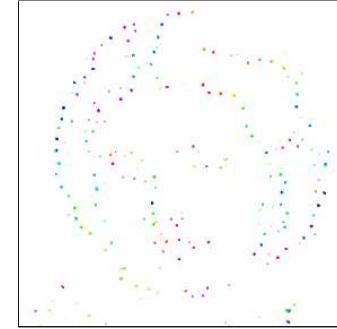
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## V1 with afferent normalization



V1 response:  
 $\gamma_n = 0, \gamma_A = 3.25$



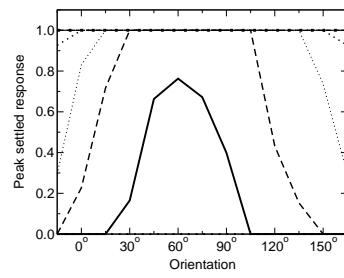
V1 response:  
 $\gamma_n = 80, \gamma_A = 30$

Responds based on contour, not contrast

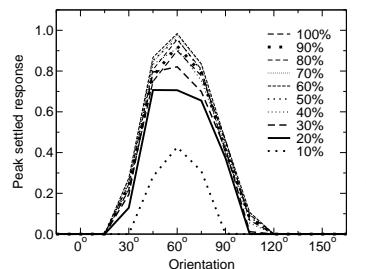
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## Tuning with afferent normalization



$\gamma_n = 0, \gamma_A = 3.25$



$\gamma_n = 80, \gamma_A = 30$

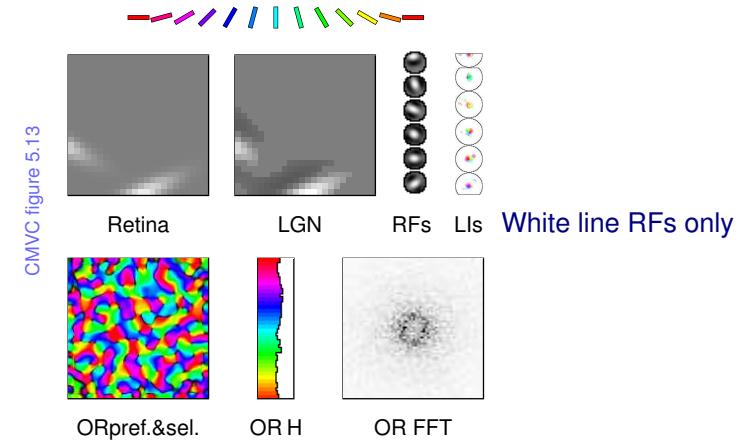
Sine grating tuning curve:

- Without  $\gamma_n$ : selectivity lost as contrast increases
- With  $\gamma_n$ : always orientation-specific

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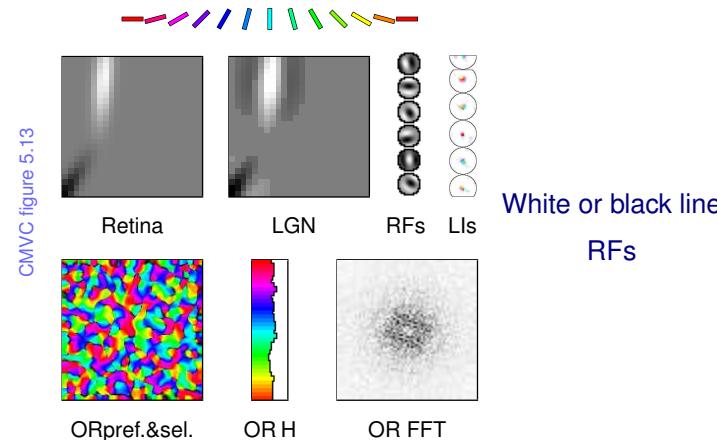
## OR Map: Gaussian



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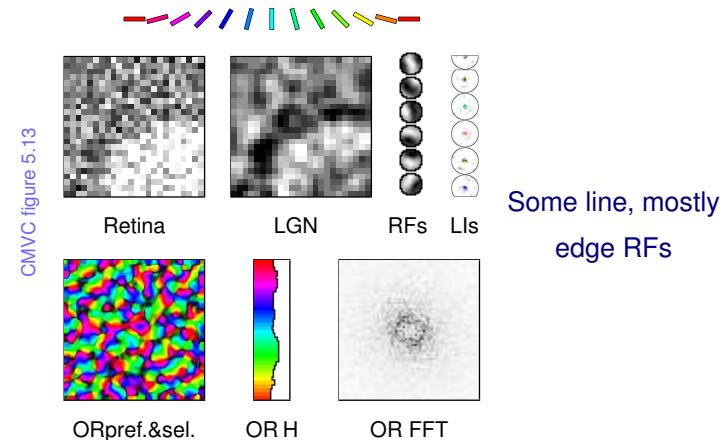
## OR Map: +/- Gaussian



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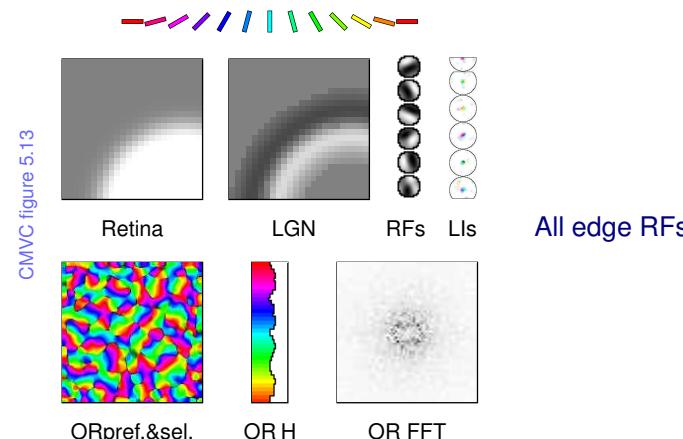
## OR Map: Retinal wave model



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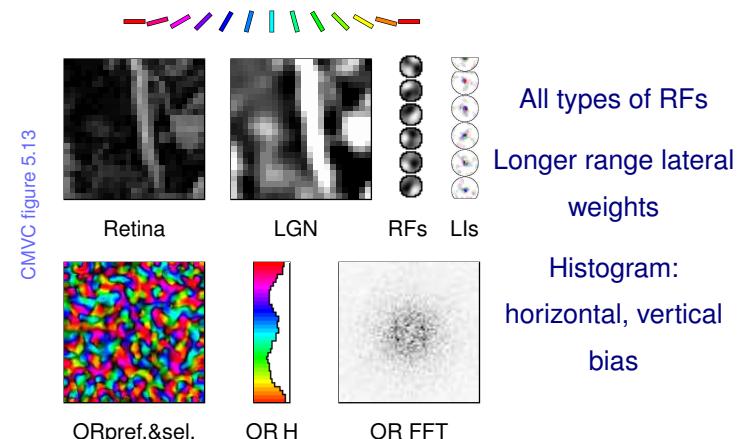
## OR Map: Smooth disks



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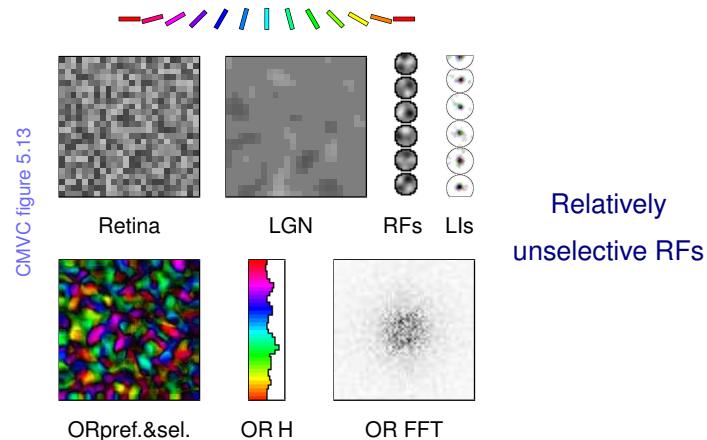
## OR Map: Natural images



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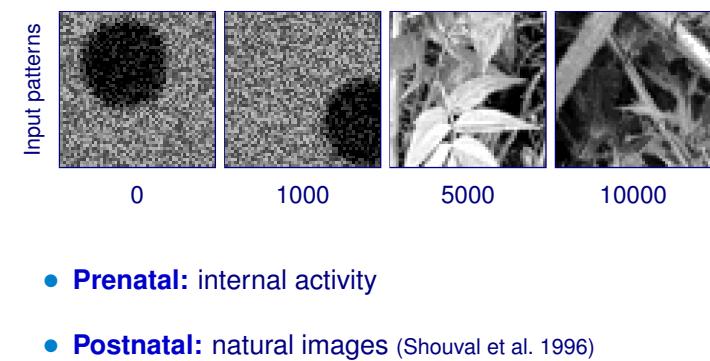
## OR Map: Uniform noise



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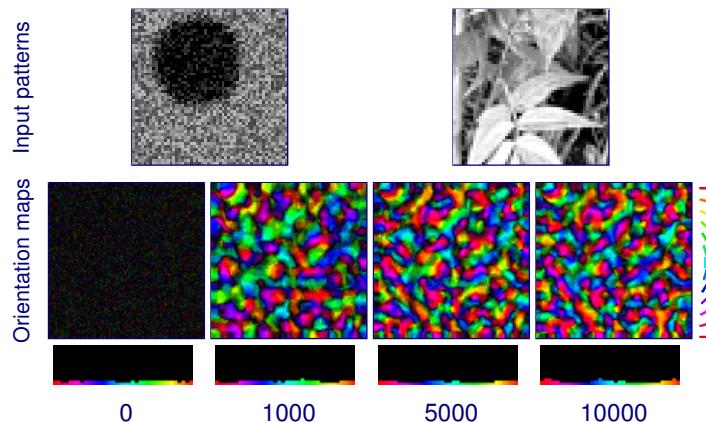
## Modeling pre/post-natal phases



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## Pre/post-natal V1 development

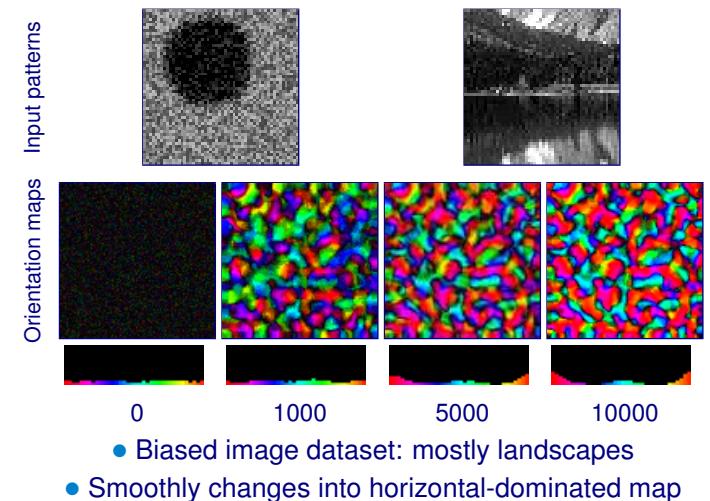


- Neonatal map smoothly becomes more selective

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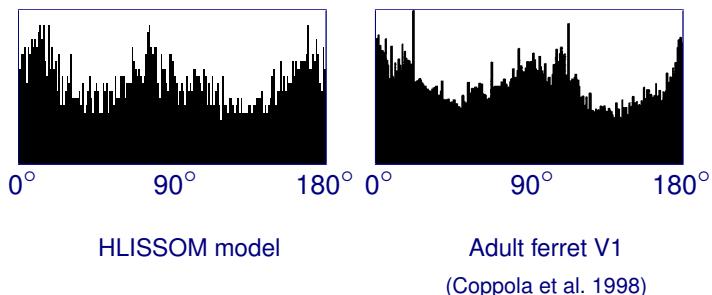
## Statistics drive development



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## OR Histograms



- After postnatal training on Shouval natural images, orientation histogram matches results from ferrets
- Model adapts to statistical structure of images

## Summary

- Development depends on the features of the input pattern
- Orientation maps develop with many different input patterns
- Develops Gabor-type RFs with most inputs
- Breaks up image into oriented patches
- Response must be scaled by local contrast to work well for large images
- Matching biology requires prenatal, postnatal phases

## References

- Coppola, D. M., White, L. E., Fitzpatrick, D., & Purves, D. (1998). Unequal representation of cardinal and oblique contours in ferret visual cortex. *Proceedings of the National Academy of Sciences, USA*, 95 (5), 2621–2623.
- Miikkulainen, R., Bednar, J. A., Choe, Y., & Sirosh, J. (2005). *Computational Maps in the Visual Cortex*. Berlin: Springer.
- Shouval, H. Z., Intrator, N., Law, C. C., & Cooper, L. N. (1996). Effect of binocular cortical misalignment on ocular dominance and orientation selectivity. *Neural Computation*, 8 (5), 1021–1040.