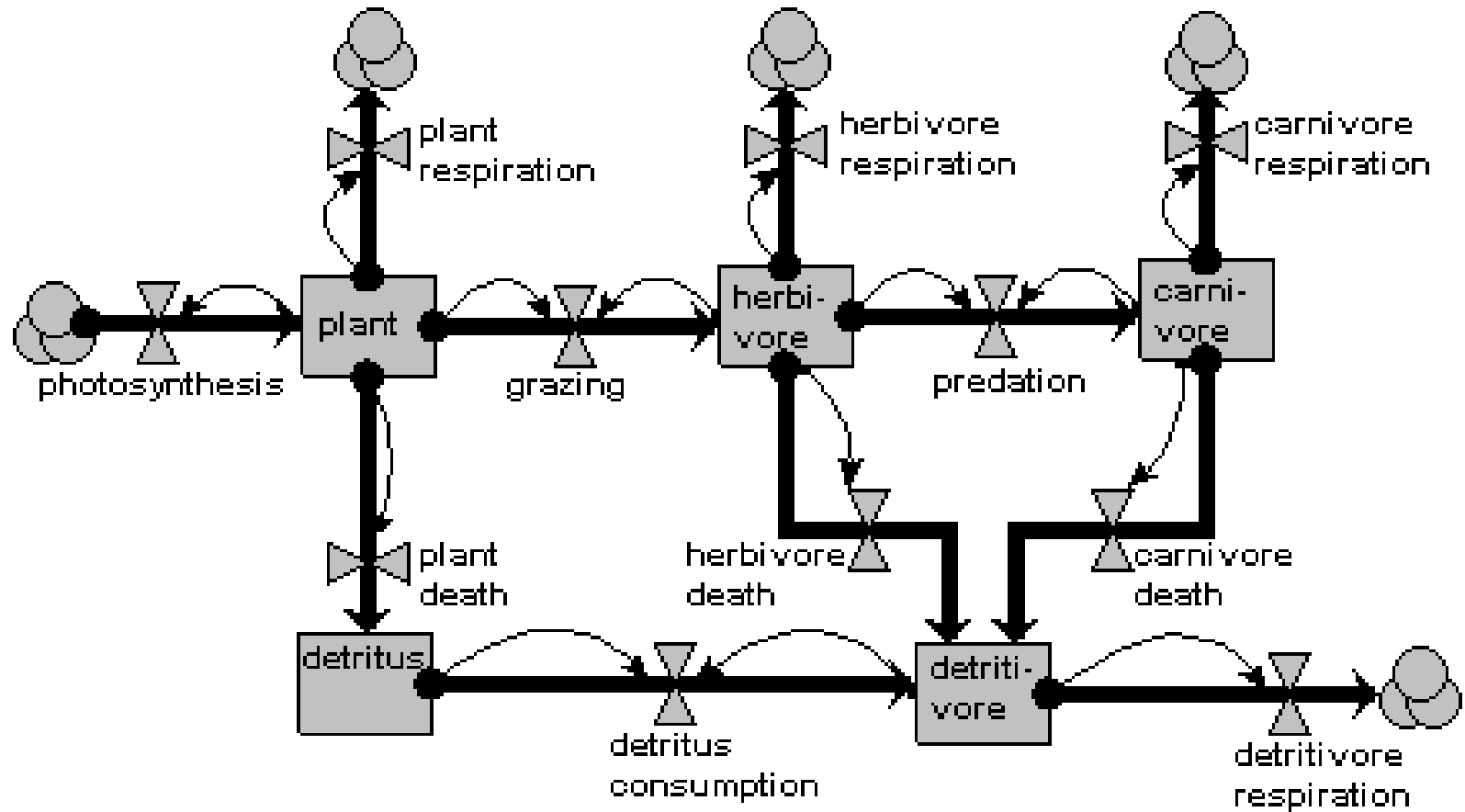


# CMGCR

## Ecosystem Modelling with System Dynamics

# Ecosystem energy flow



# System Dynamics Concepts

- Stocks – modified each timestep by flows
- Flows – rate of change
- Auxiliary variables – used for intermediate calculations

# Population Dynamics

*simple*: statement

- The population is represented by a single state variable (stock), whose dynamics depend on two flows: a reproduction inflow and a mortality outflow. Both occur at a rate proportional to population size.

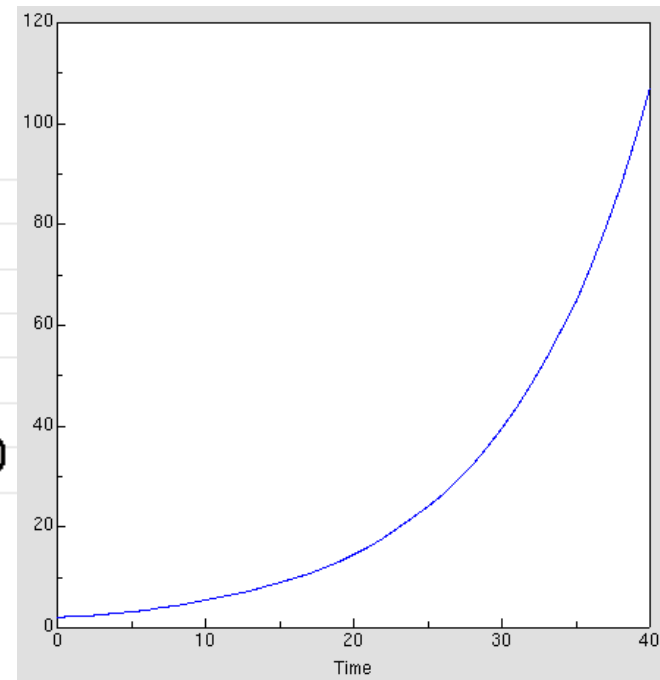
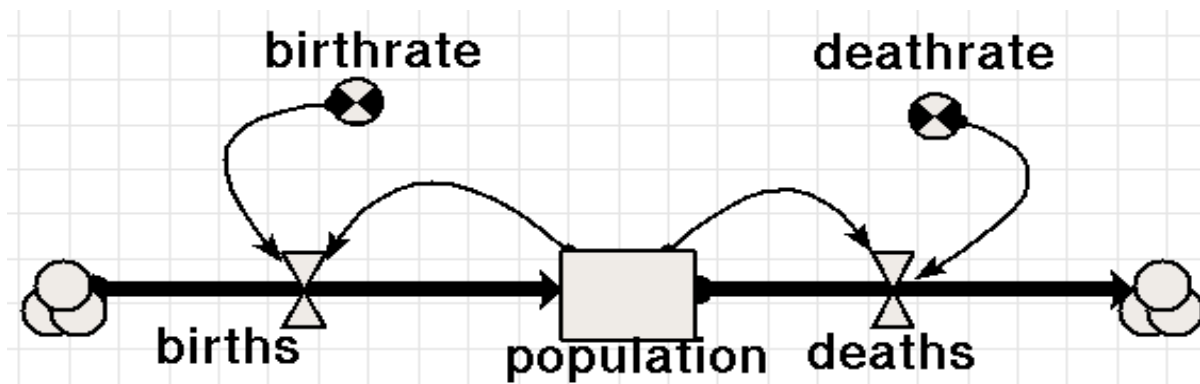
# Population Dynamics

## *simple*: components

- stock: population
- flows: births, deaths
- parameters: birthrate, deathrate
- Equations:
  - $\text{births} = \text{population} \times \text{birthrate}$
  - $\text{deaths} = \text{population} \times \text{deathrate}$
- initial conditions: population, birthrate, deathrate

# Population Dynamics

*simple: model*



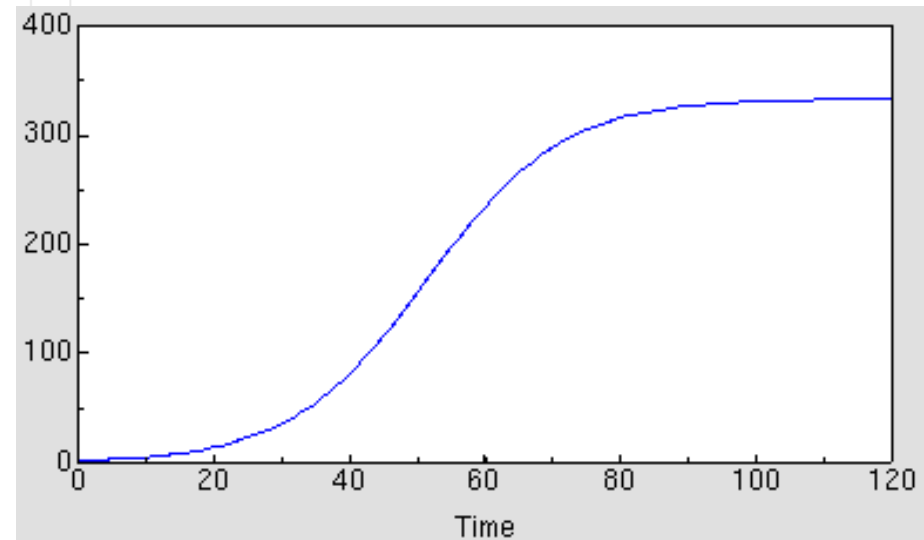
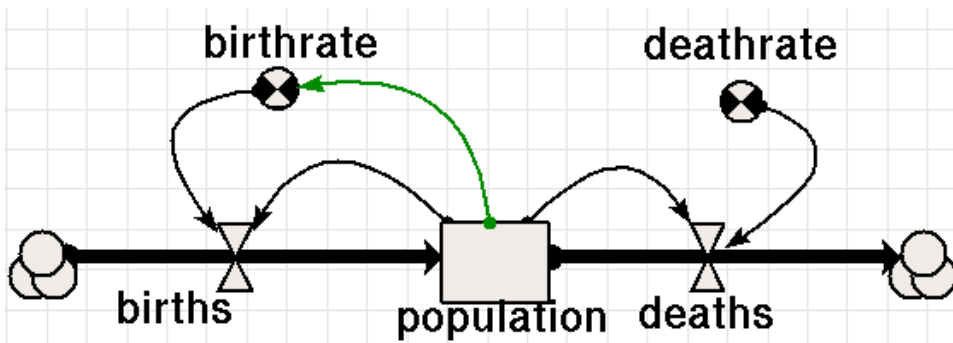
# Population Dynamics

## *declining fertility*: statement

- The simple model is modified by making the reproductive rate per individual depend on population size, decreasing as population increases.
- Birthrate =  
$$0.3 \times (1000 - \text{population})/1000$$

# Population Dynamics

## *declining fertility: model*





# Population Dynamics

## *competition*: statement

- Two-species competition. Each population's growth rate is reduced as its population gets bigger (the *declining-fertility* model). When a competitor is present, then the growth of each population is further reduced by the other. The outcome depends on the relative strength of within- and between-species factors.

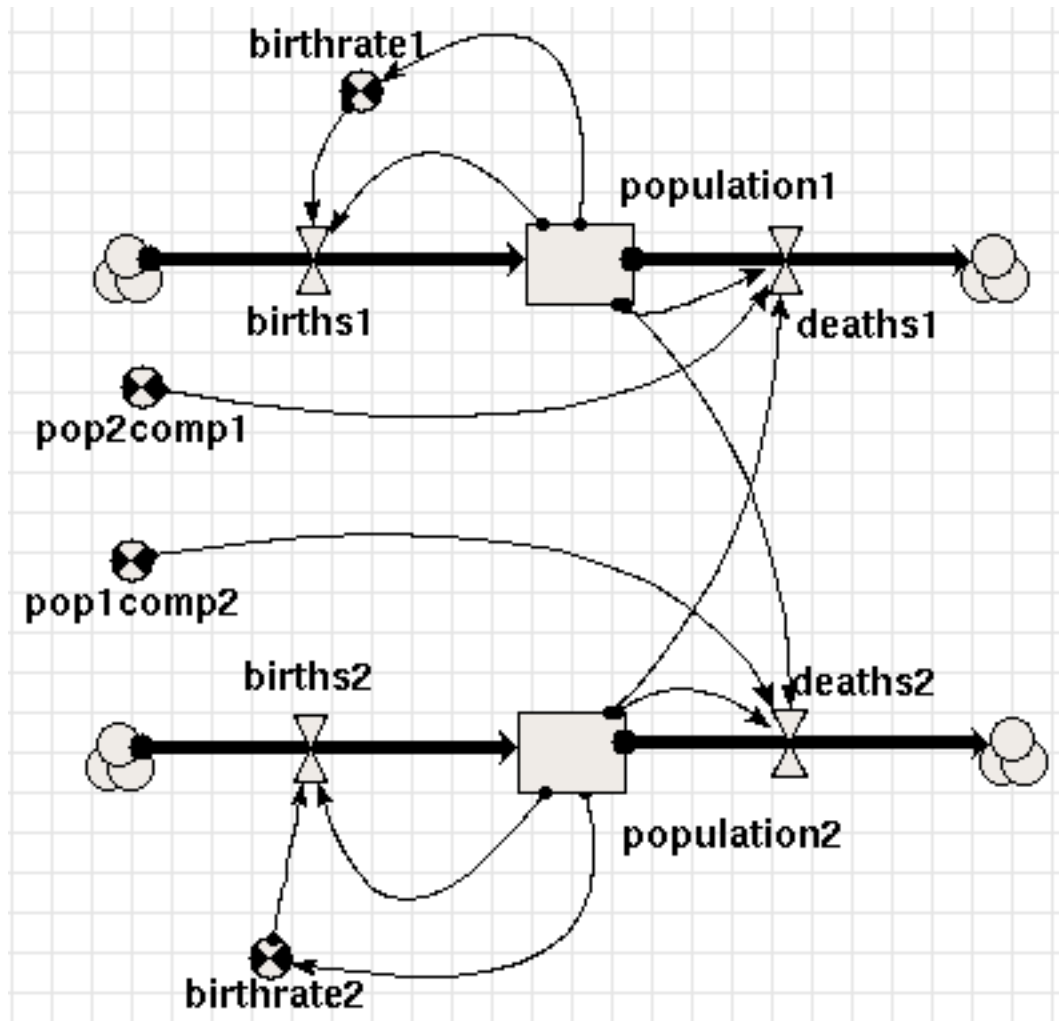
# Population Dynamics

## *competition*: components

- Stocks: population1, population2
- Flows
  - each population as for *declining-fertility*
- Parameters
  - Additional parameters to reflect the increase in deaths due to the other species (alternatives?)

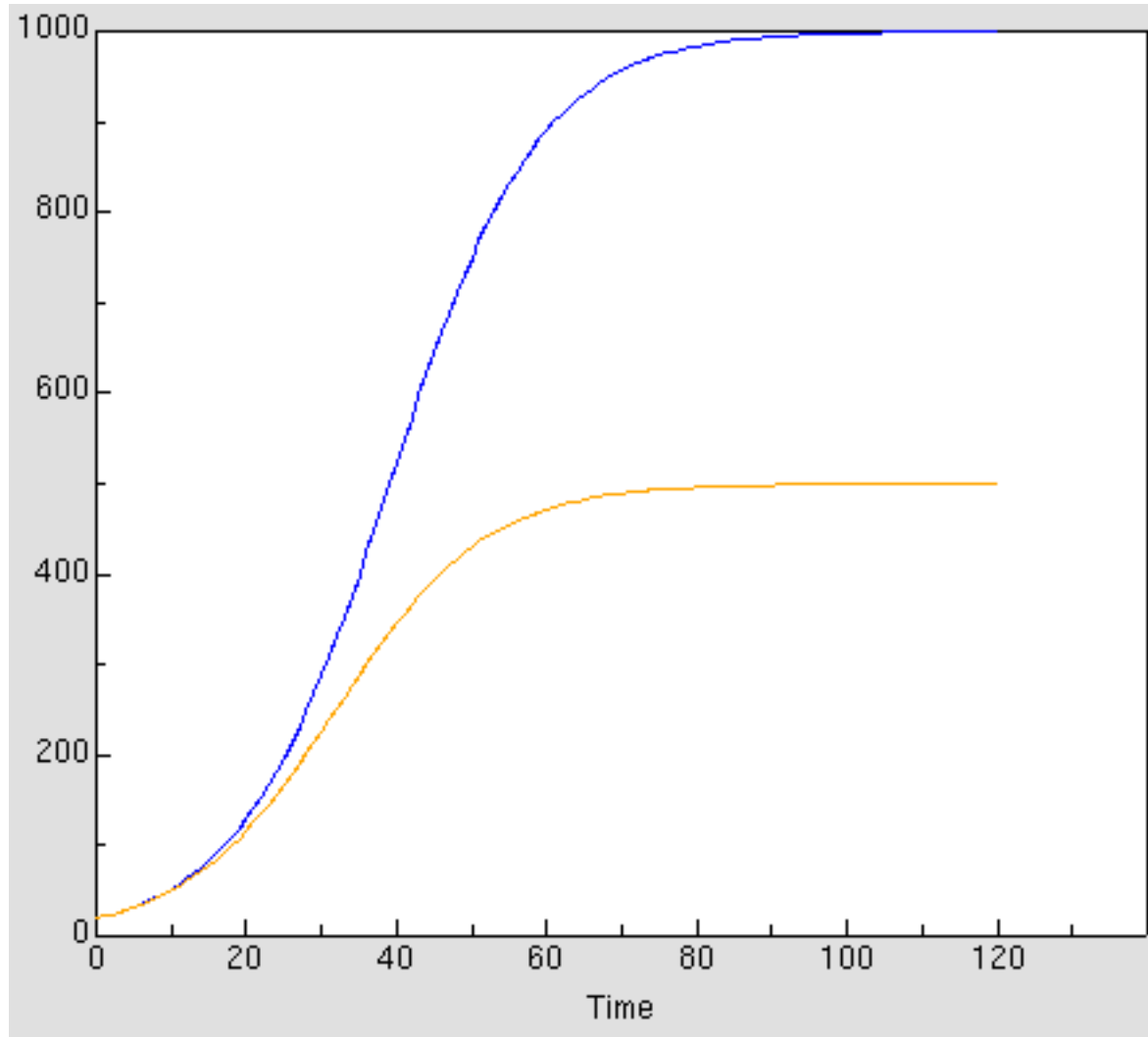
# Population Dynamics

## *competition*: model



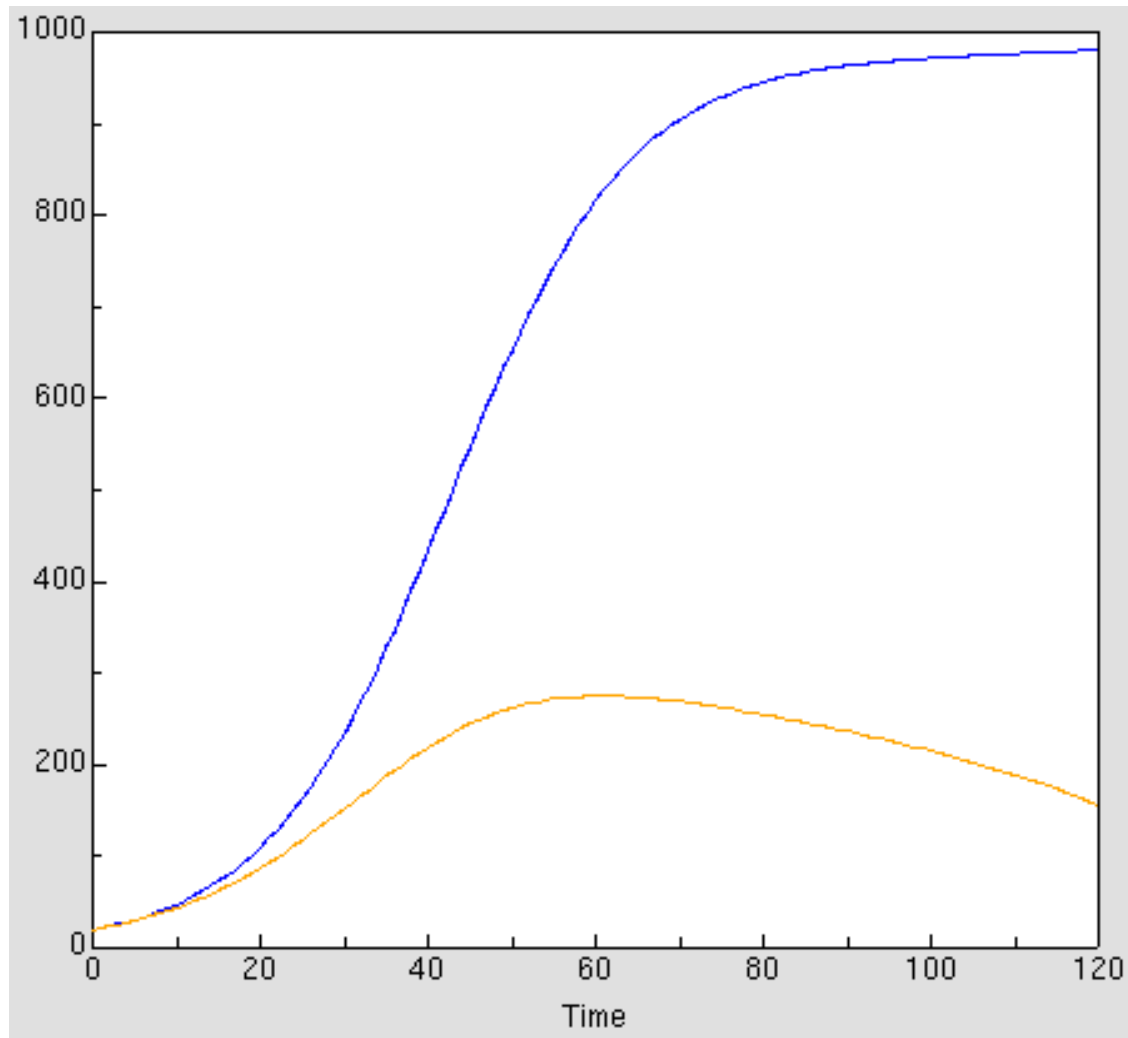
# Population Dynamics

*competition: none*



# Population Dynamics

*competition: suppression*



# Mathematical Formulation

## *competition*: statement and model

$$dX_1/dt = r_1 \cdot X_1 \cdot (1 - b_1 \cdot X_1 - c_1 \cdot X_2)$$

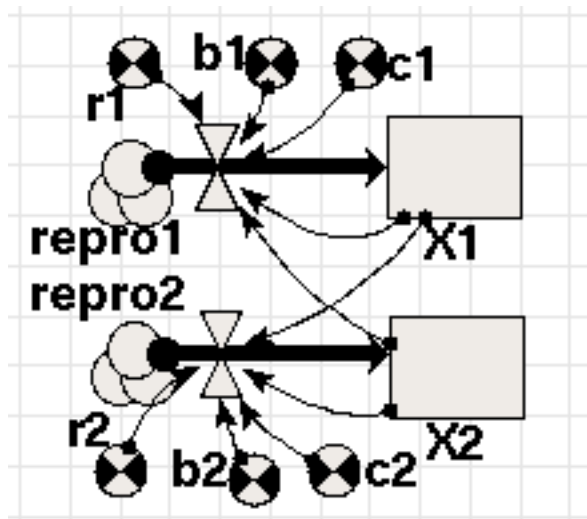
$$dX_2/dt = r_2 \cdot X_2 \cdot (1 - b_2 \cdot X_2 - c_2 \cdot X_1)$$

$X_1, X_2$  are the populations sizes of the two species;

$r_1, r_2$  are the intrinsic rate of increase of the two species;

$b_1, b_2$  are the self-inhibition coefficients for the two species;

$c_1, c_2$  are the competitor's inhibition coefficient for each species.



# Predator-Prey exercise

- [www.simulistics.com/tutorials/predprey](http://www.simulistics.com/tutorials/predprey)
- Look at the first page, try to build your own model
- Then look at the suggested way to model
- ... including the mathematical variant

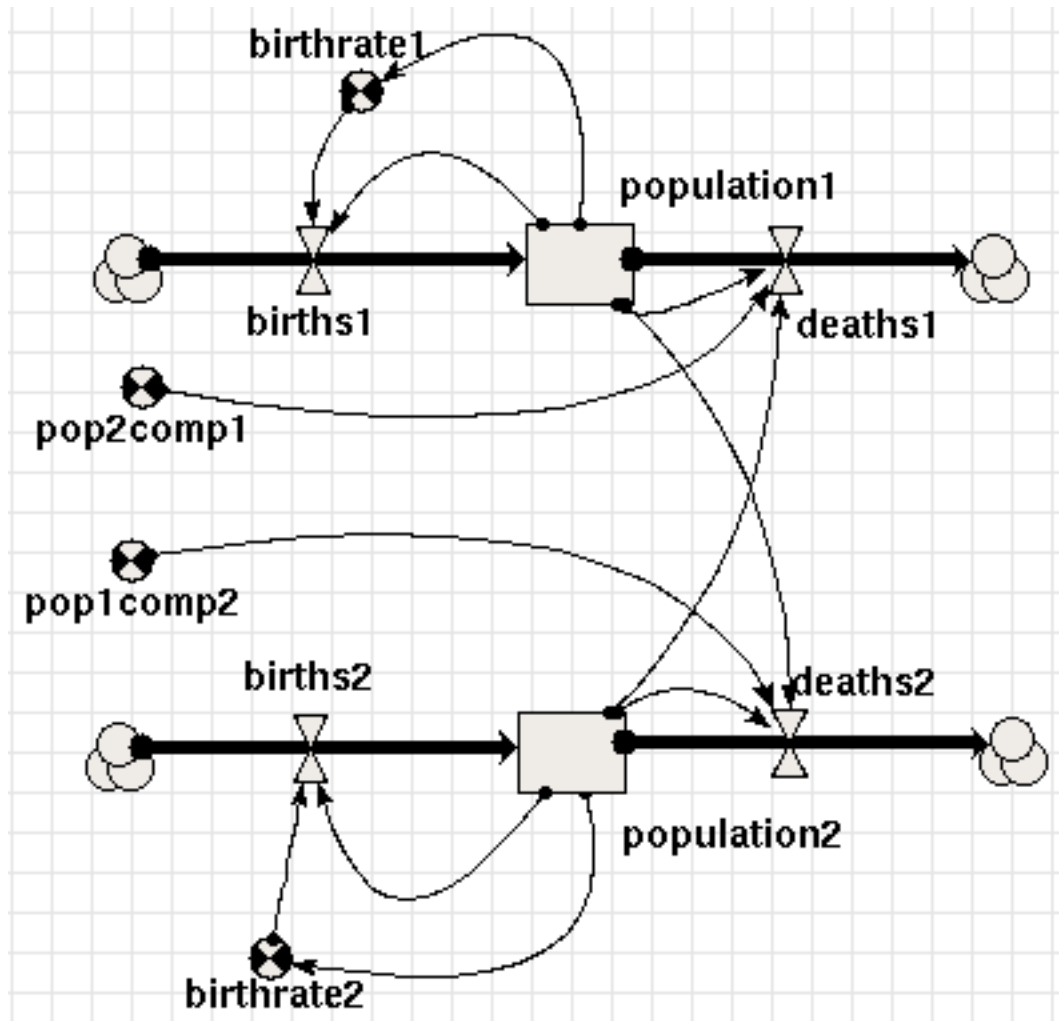
# Submodels

- In many real-world situations, things to be modelled are repeated
  - Animals, trees, species, land patches, ...
- Simulators should support the concept of a submodel



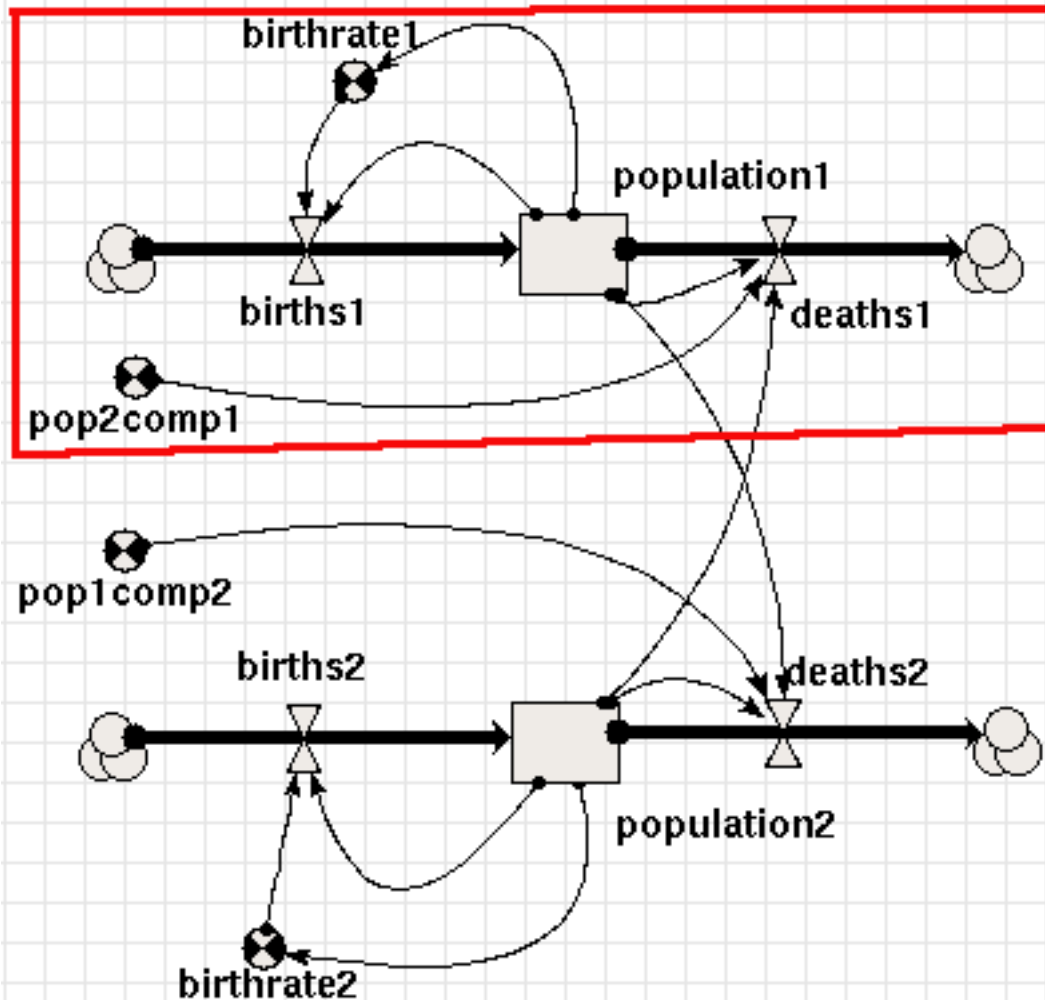
# Population Dynamics

## *competition*: model



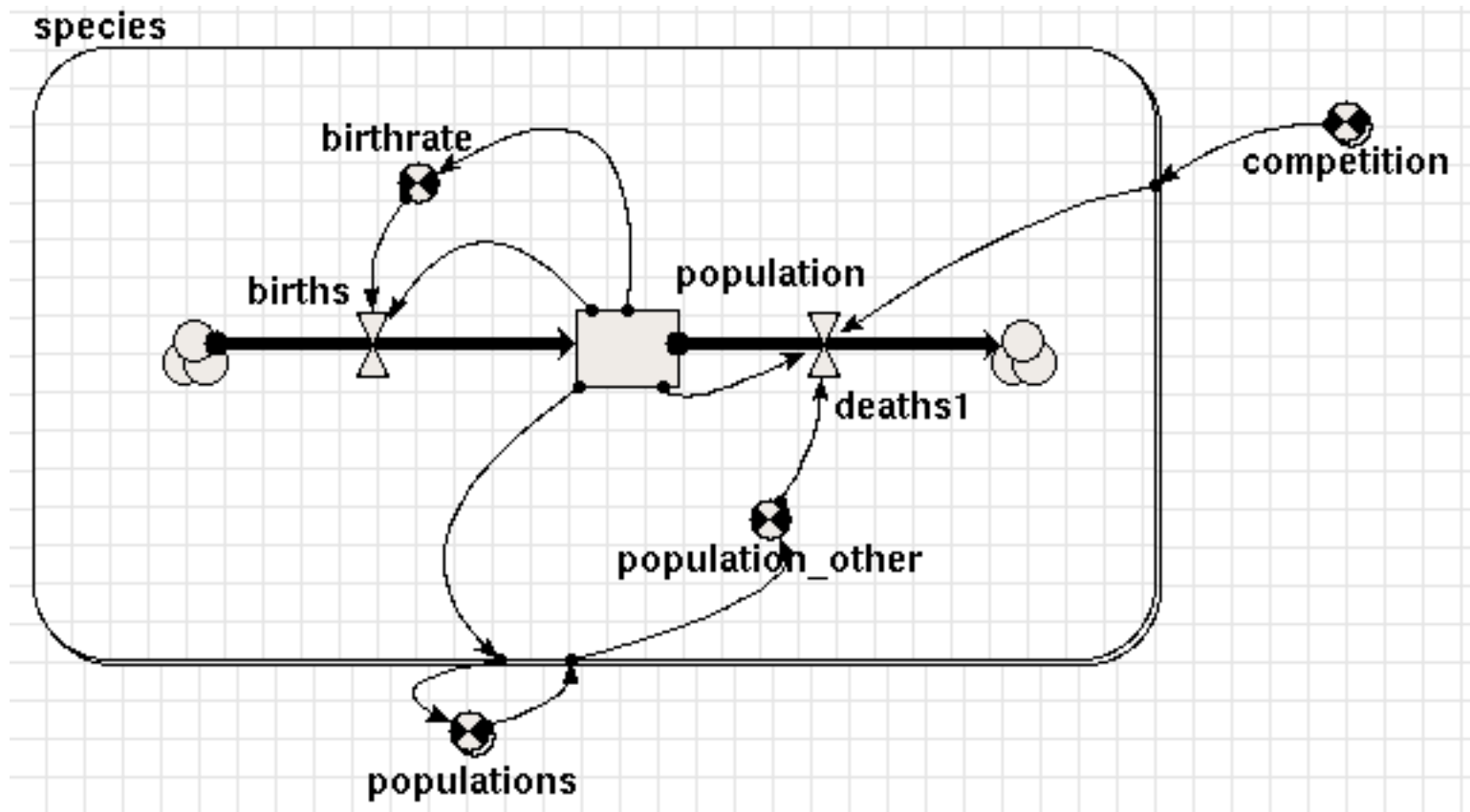
# Population Dynamics

## *competition*: model



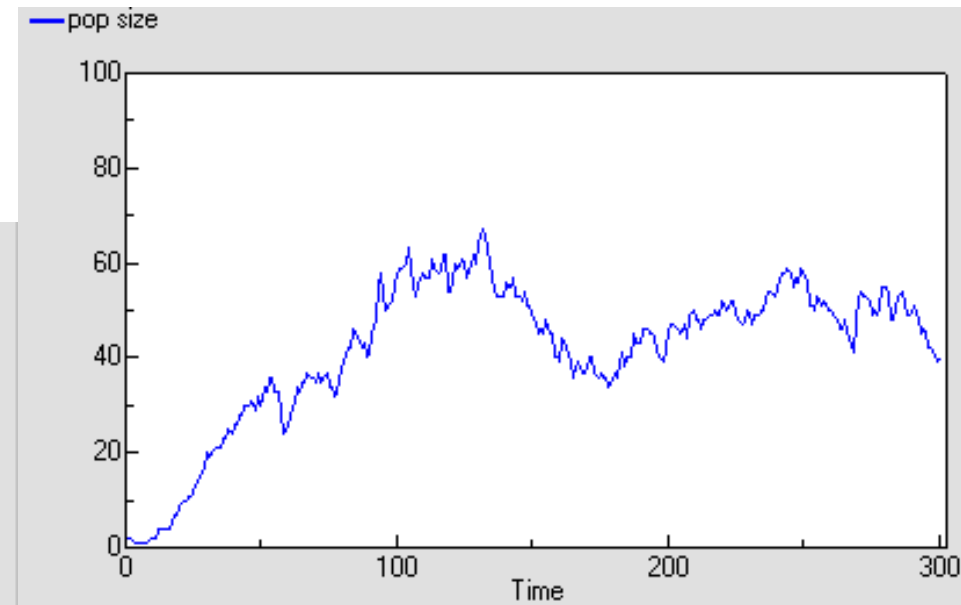
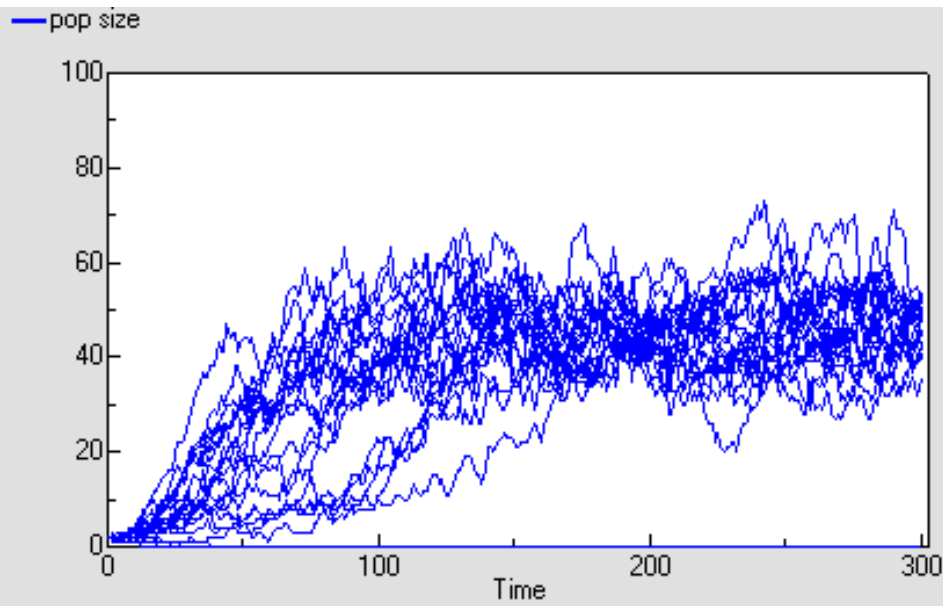
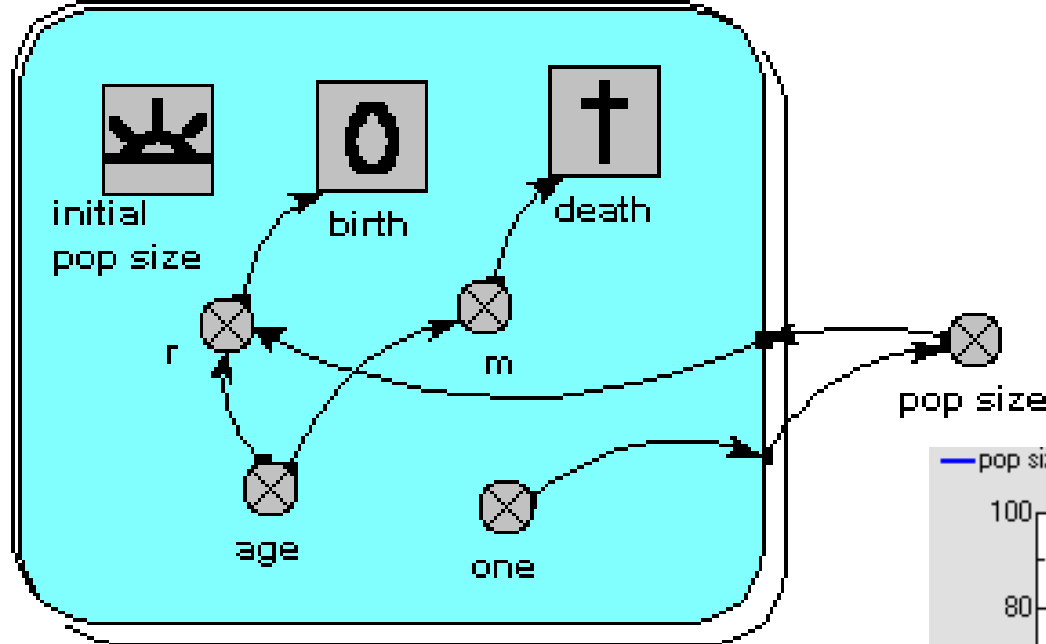
# Population Dynamics

## *competition*: submodel

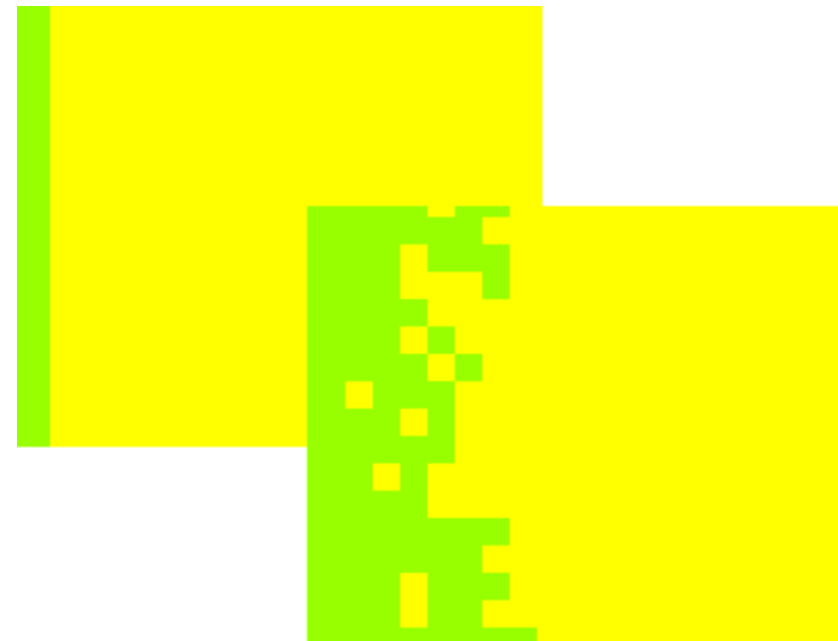
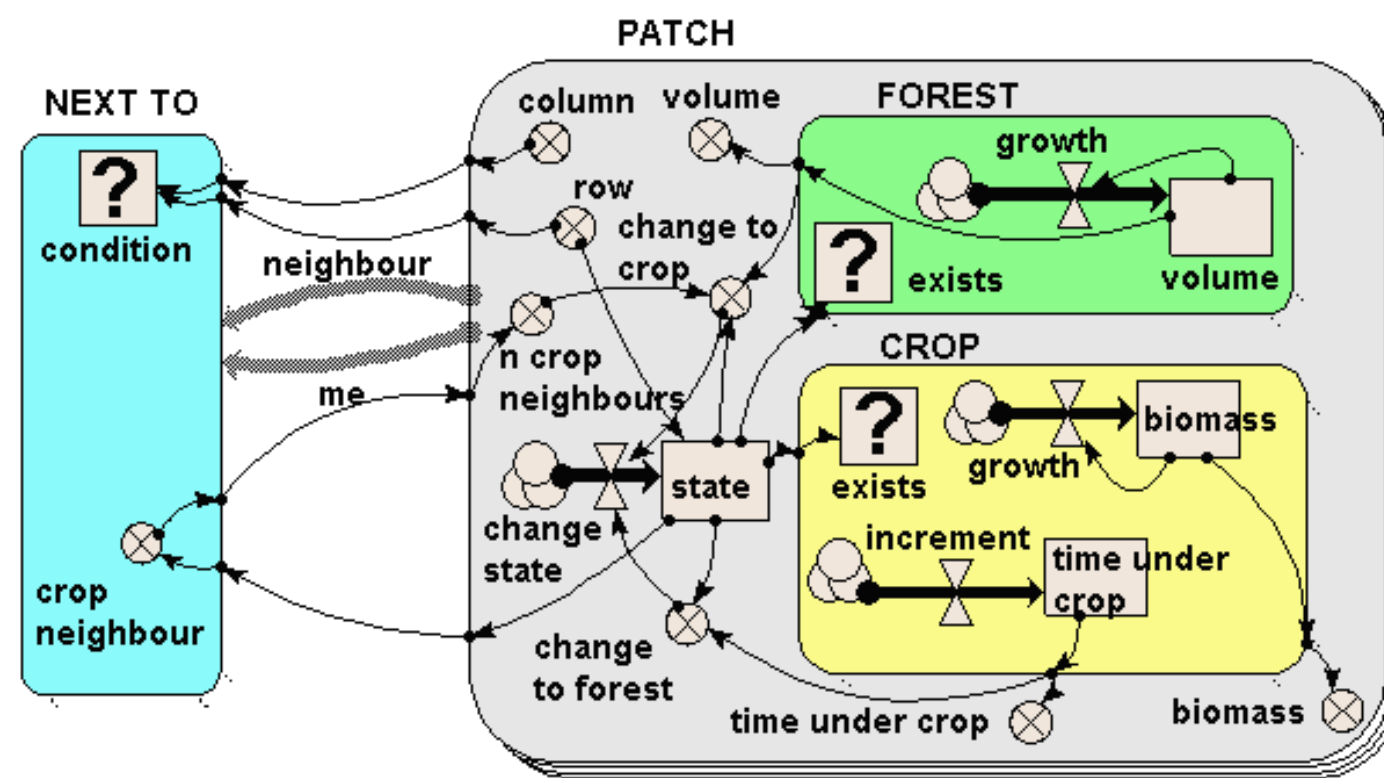


# Population dynamics: individual-based

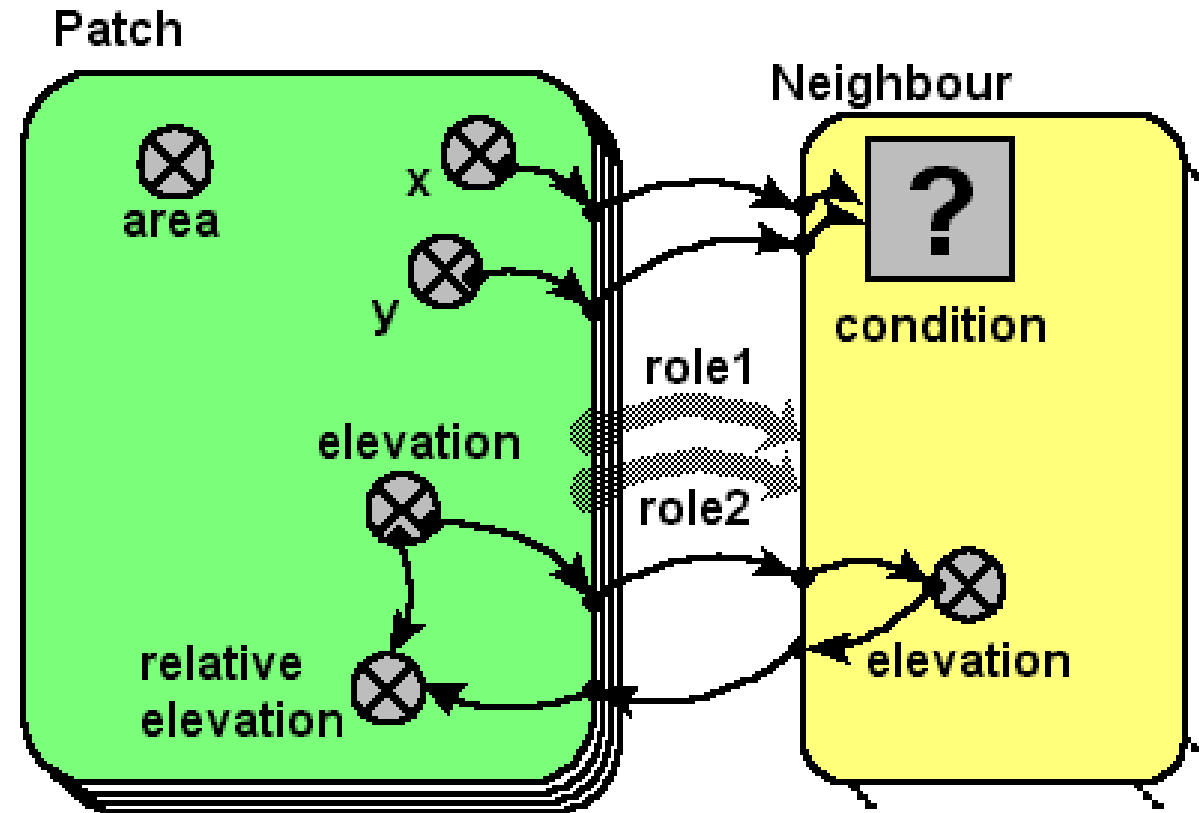
Individual



# Modelling land-use change at the forest margin

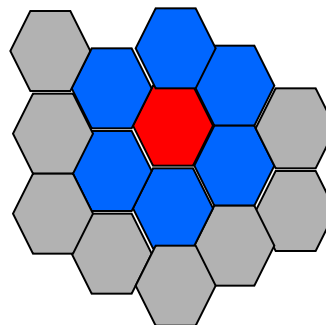
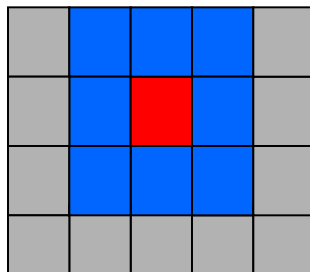
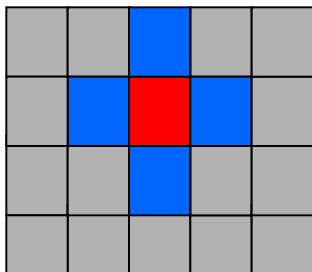


# Spatial modelling: defining neighbour associations

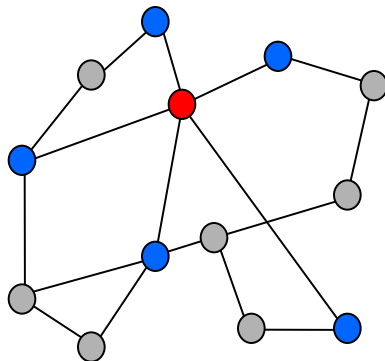
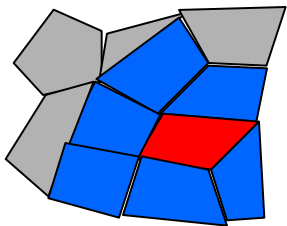
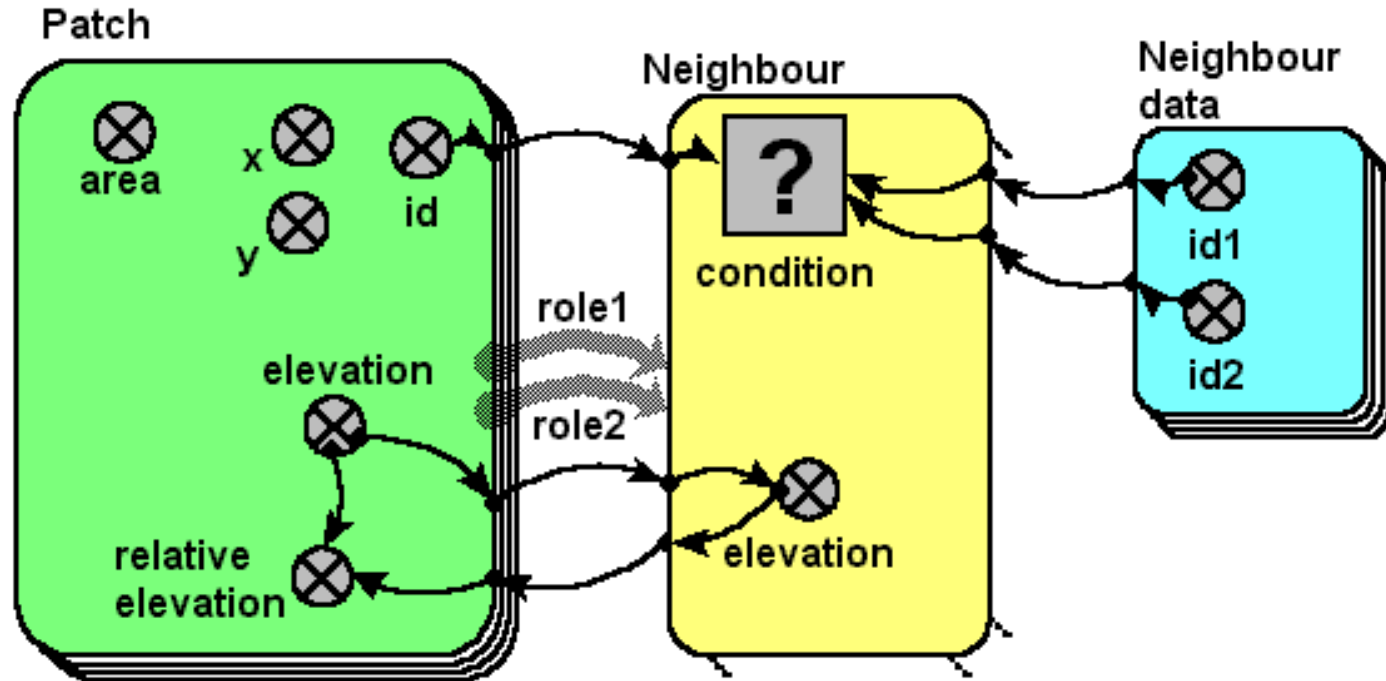


What type of neighbour association? Could be anything that can be inferred from x,y coordinates.

E.g. grid (4-nearest, 8-nearest), hexagon...

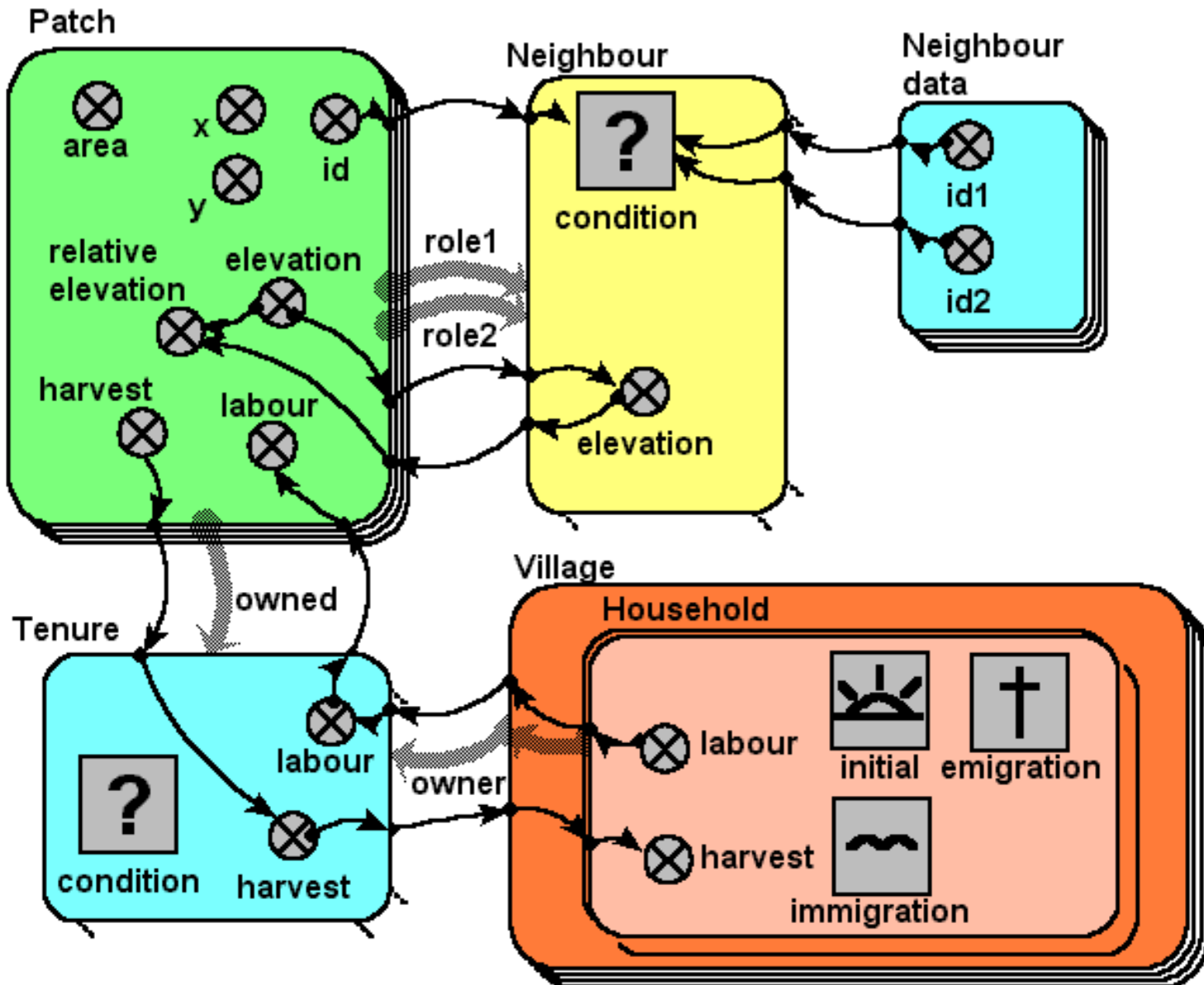


# Spatial modelling: explicit listing of neighbours



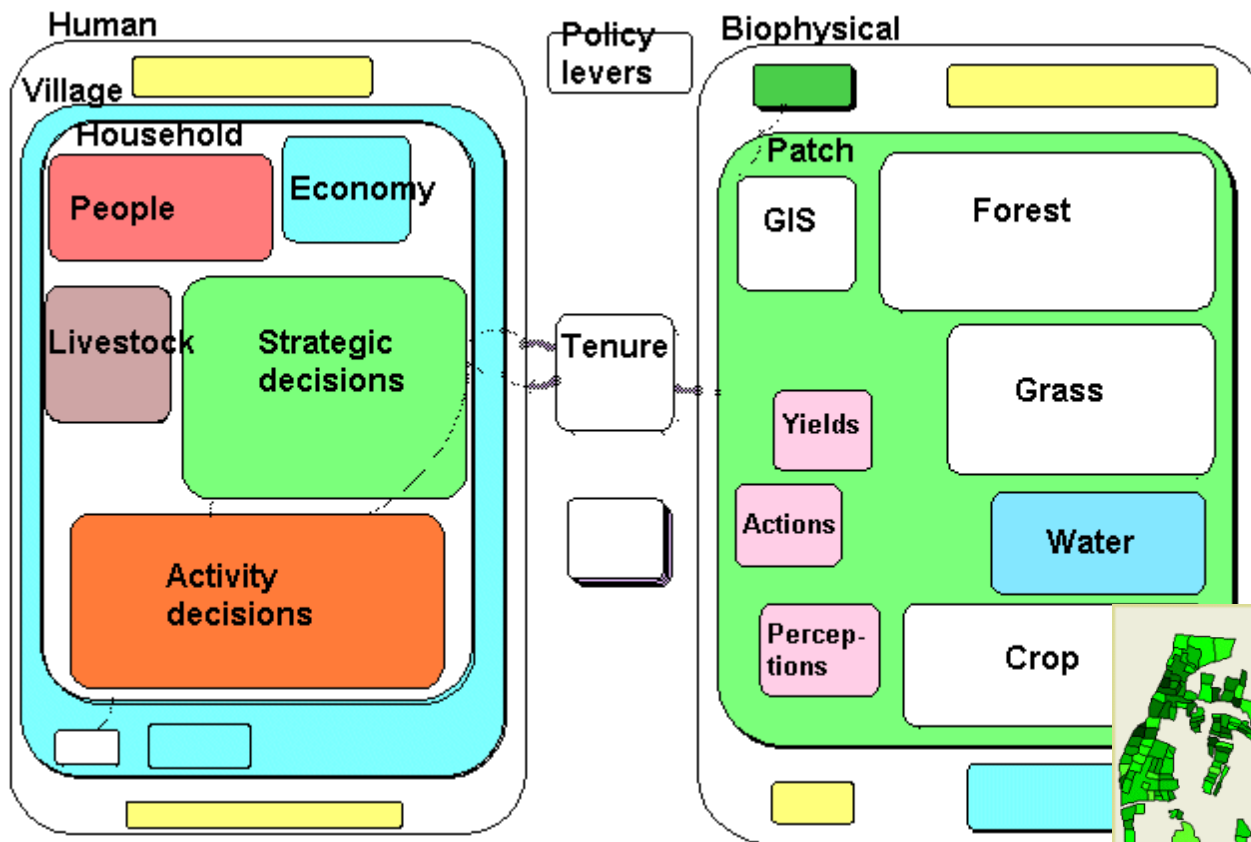
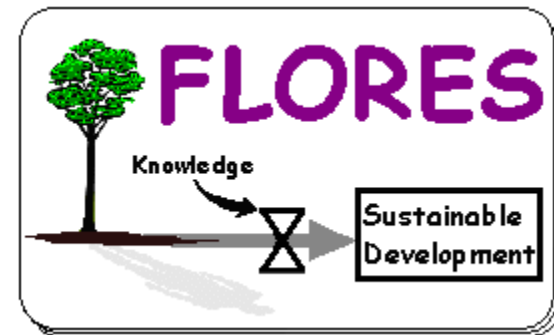
This could represent polygons (vector GIS), or networks.

# Including the human dimension

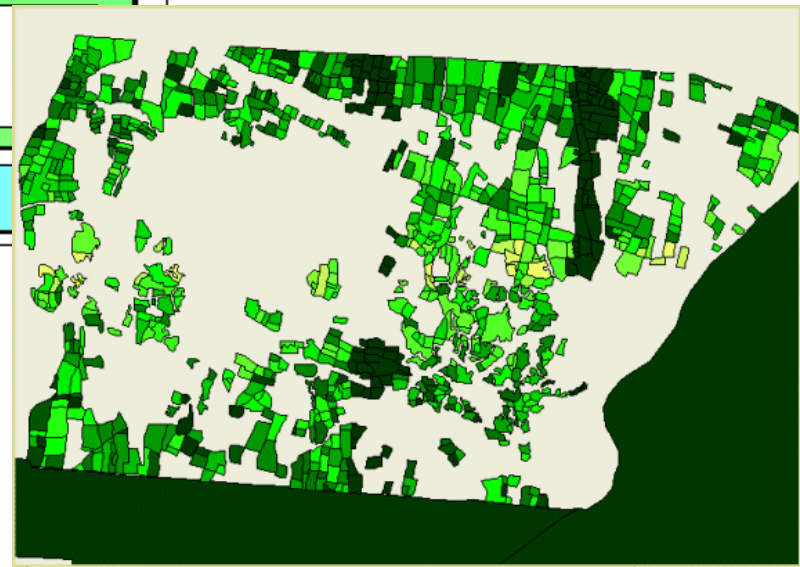
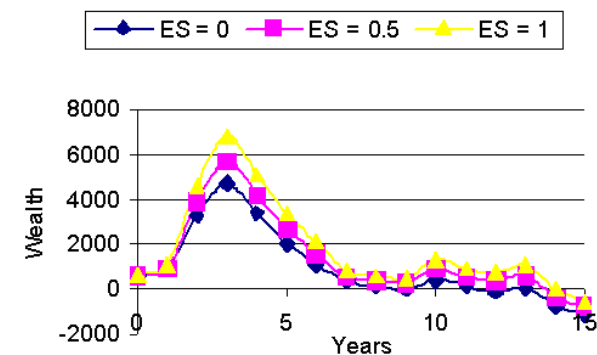




# FLORES: modelling sustainable livelihoods at the forest margin



Wealth vs Years with Economic Stimulus



# Tree Growth exercise

- [www.simulistics.com/tutorials/trees](http://www.simulistics.com/tutorials/trees)
- Work through the tutorial