

# **Cellular Automata and Agent-Based Models for Earth Systems Research**

# Outline

- Introduction to Modelling and Simulation
- CA
  - theory and application
  - examples
- ABM
  - theory and application
  - examples

# General Principles

- Natural systems can often be represented as continua
- These can be represented by continuous discrete fields or by equations describing rates of change
- Mathematically rates of change are expressed by differential equations.
- Sometimes precise analytical solutions exist but often they must be solved numerically.
- Advection and diffusion processes describe the rate of change of quantities in time and space.
- They are best represented by partial differential equations and frequently solved numerically using finite differences/ finite elements.

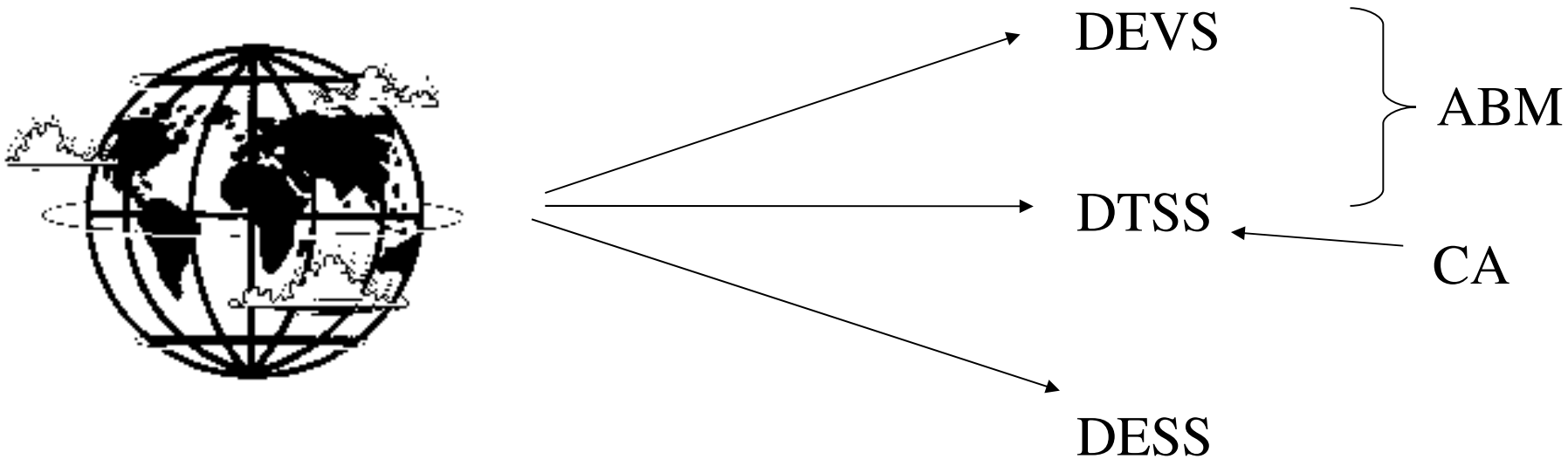
# Modelling vs. Simulation

- Modelling:  
the act of abstracting from the real world and  
specifying it in some formalism
- Simulation:  
running the model

# Discrete vs. Continuous

- Time, Space, & Attributes
- Discrete as approximation of continuous
- Not either/or

# Modelling Framework



Discrete Event/Time/Equation Simulation System

Following Zeigler *et al.* 2000

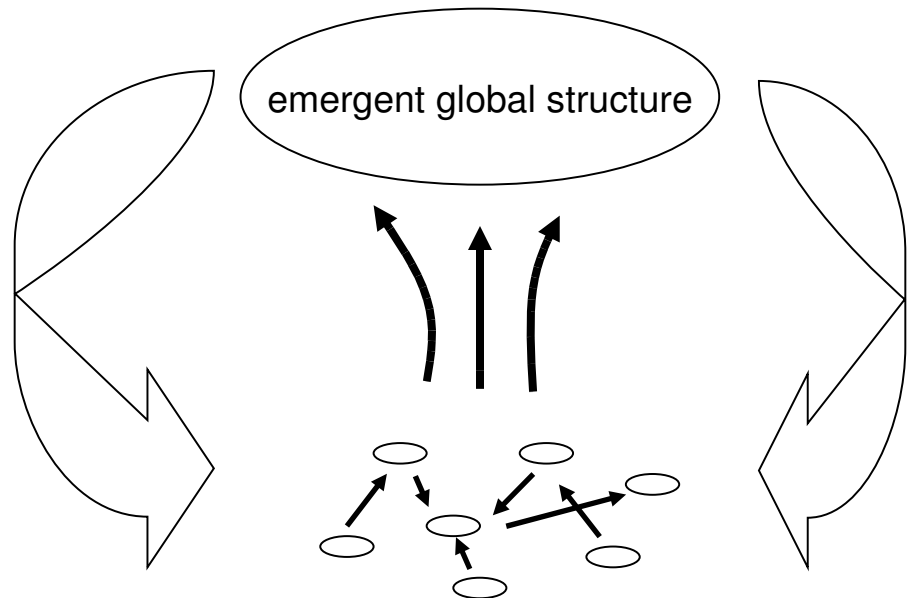
# Complexity Theory

- Not a theory
- Chaos theory – Edward Lorenz
- Related to emergence

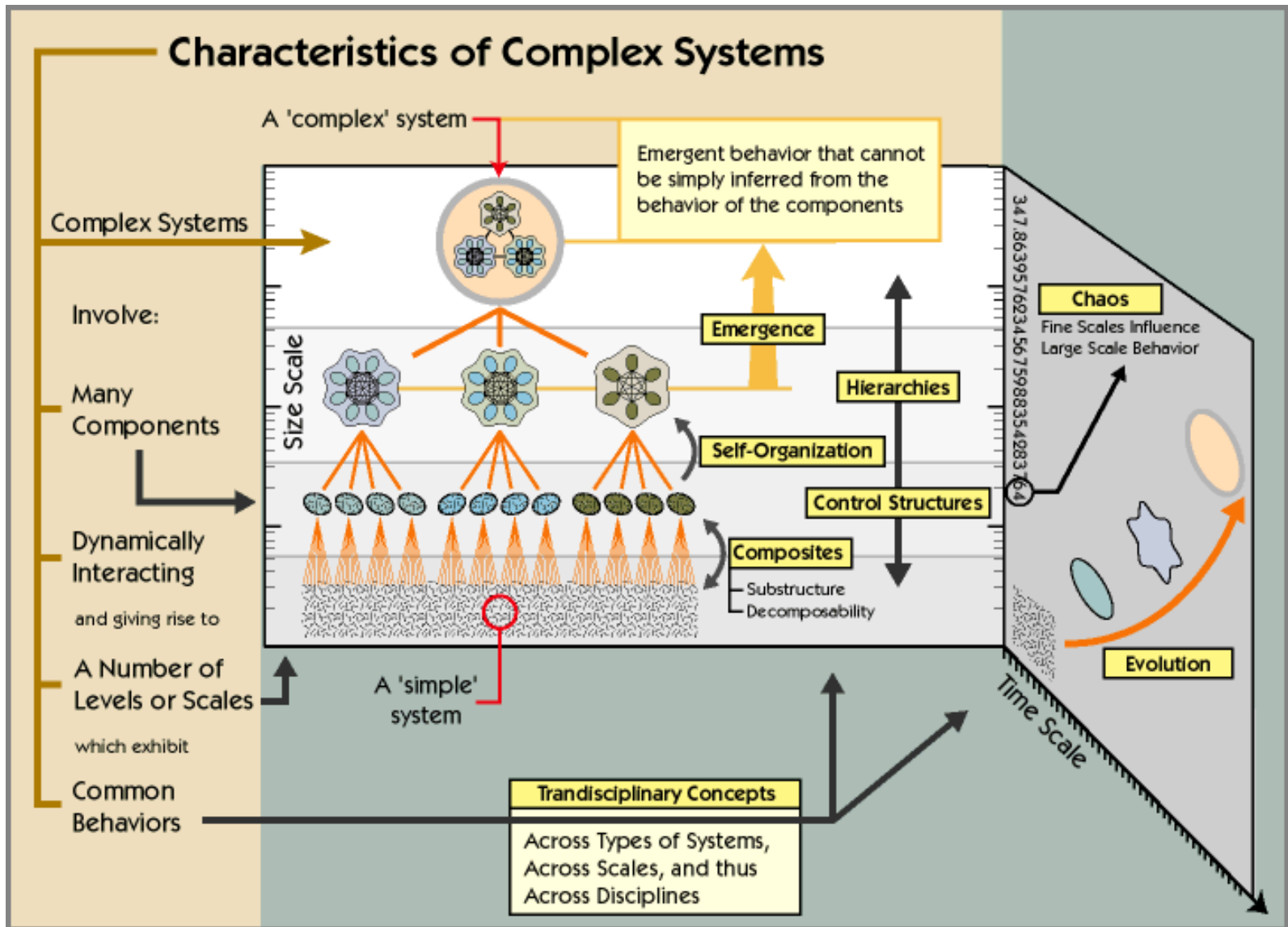


# Emergence

- Complex behaviour emerges from simple interactions
- Inter-scale emergence vs. intra-scale emergence







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# Cellular Automata (CA)

- Discrete dynamical systems
- Discrete = space, time, and properties have finite, countable states
- Complexity is bottom up



# CA background

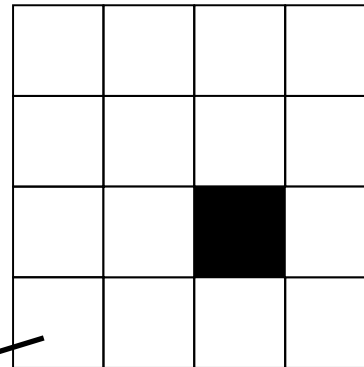


- Early research in the 40's
- Popularised by The Game of Life
- Now used in modelling physical and human systems, e.g.
  - soil erosion
  - vegetation dynamics
  - urbanization/ land use change
  - sand piles

(And studied by a bunch of people obsessed with discovering all of the possible patterns that can be created by CA)

# CA components

- Cellular Space or Lattice
- Cell States
- Neighbourhood
- Transition Rules
- Discrete Time

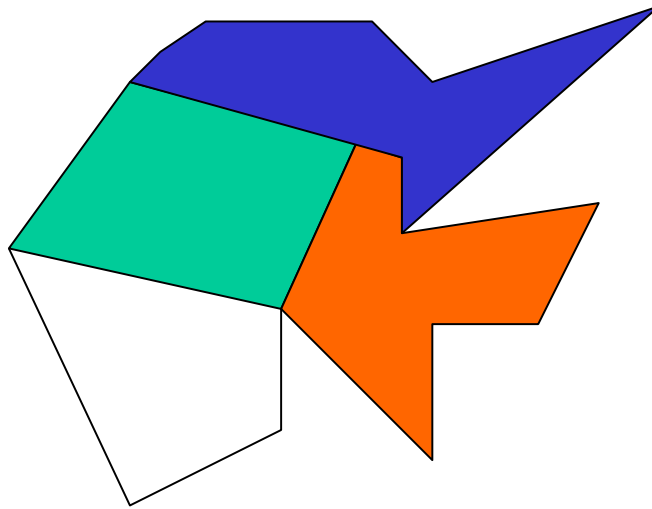


finite set of cell states

if (some condition holds)  
do x

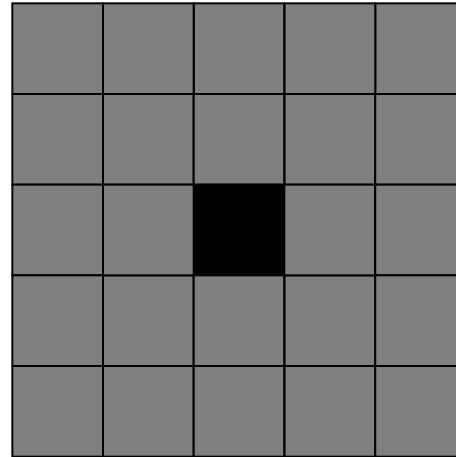
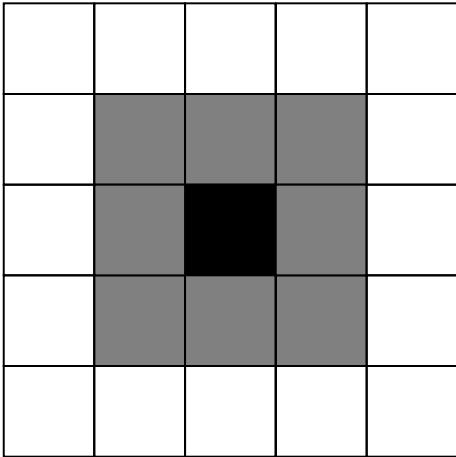
# Spaces

- Traditionally Raster
- Vector
- Graph
- Higher dimensional spaces?



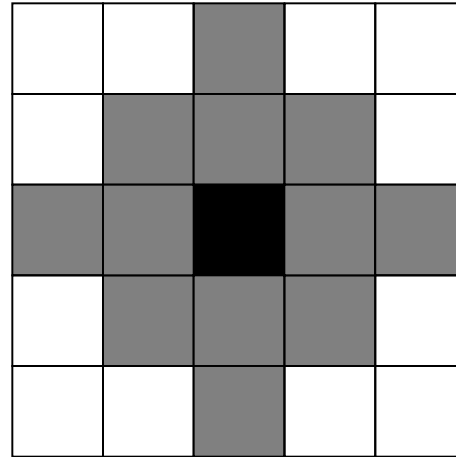
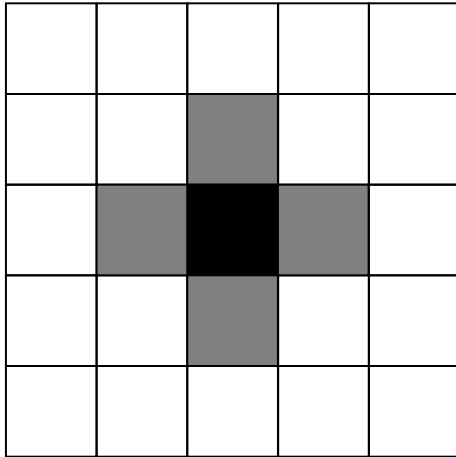
# CA Neighbourhoods

Moore:



# CA Neighbourhoods

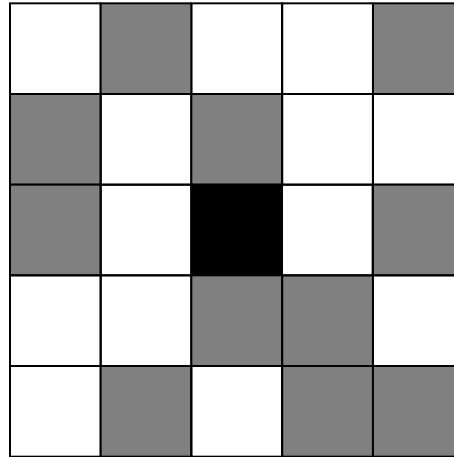
von Neumann:

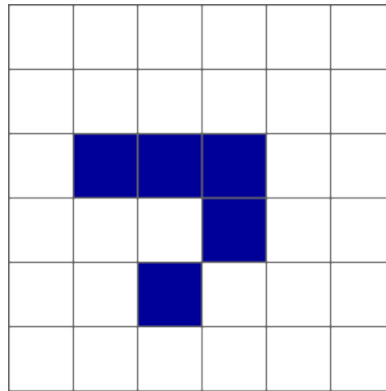




# CA Neighbourhoods

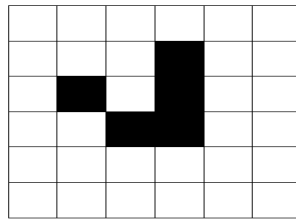
Arbitrary:



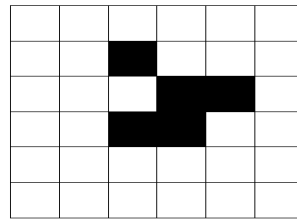


game of life glider

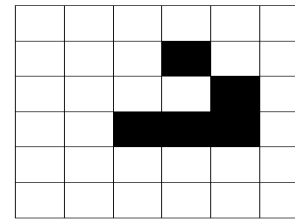
# Game of Life Rules



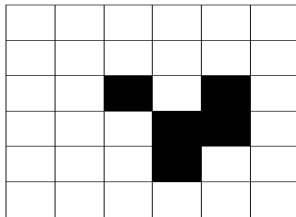
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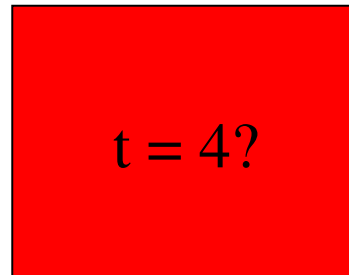
$t = 1$



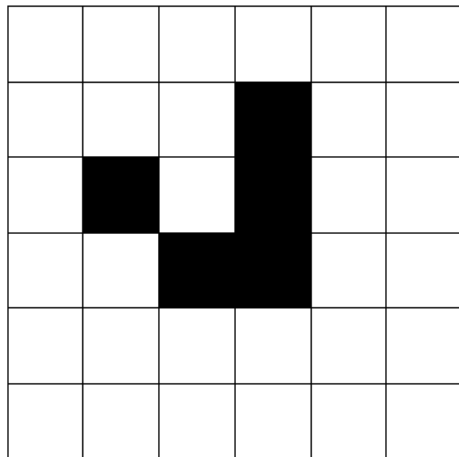
$t = 2$



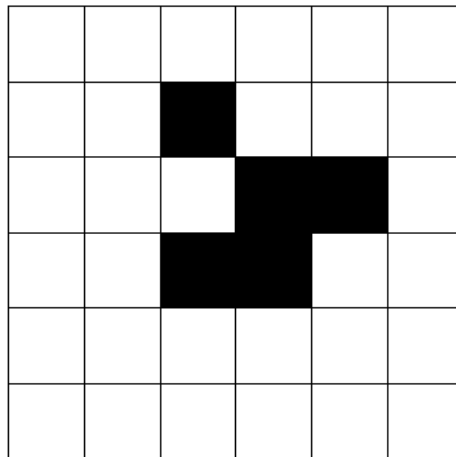
$t = 3$



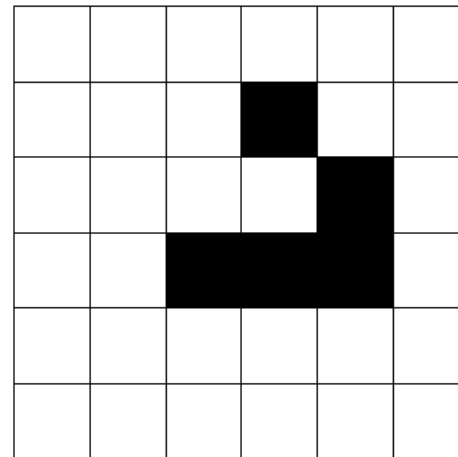
1. A dead cell with exactly 3 live neighbours becomes alive
2. A live cell with 2 or 3 live neighbours stays alive; otherwise it dies.



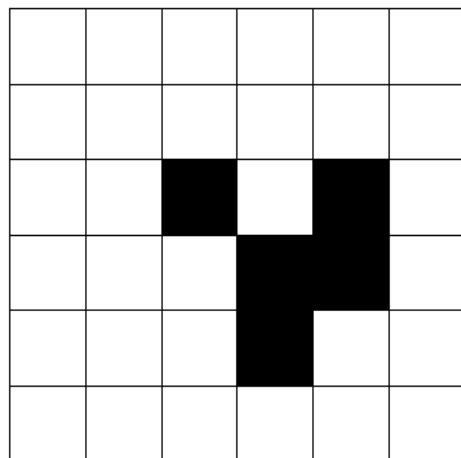
$t = 0$



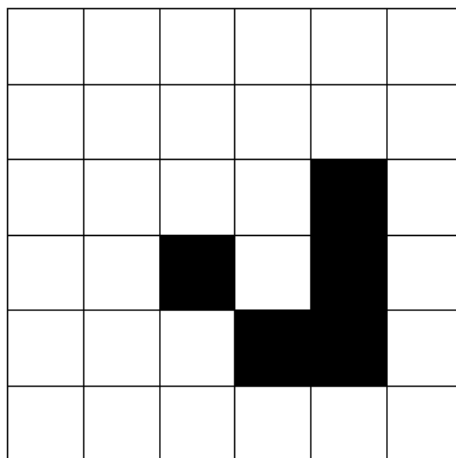
$t = 1$



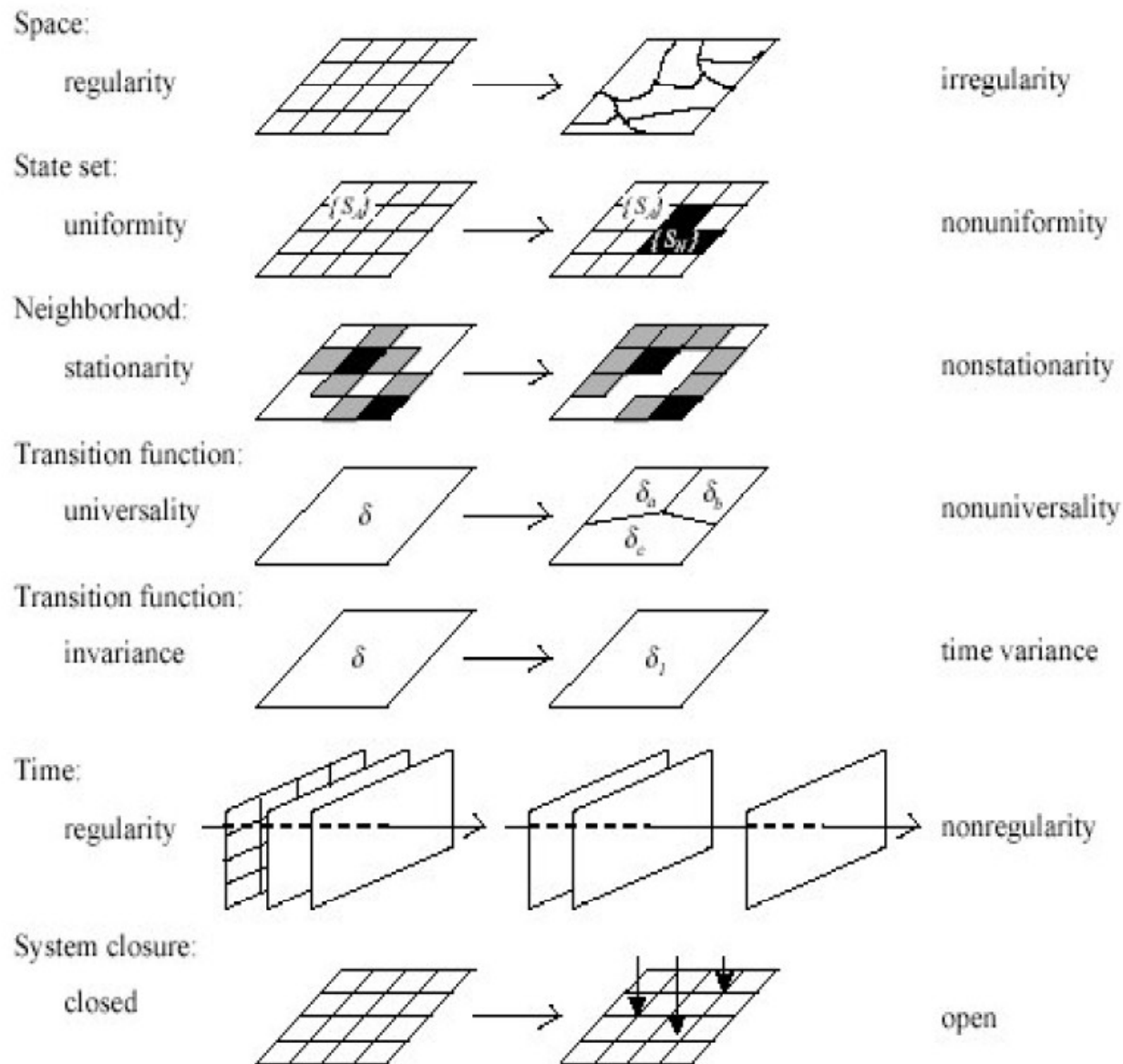
$t = 2$



$t = 3$

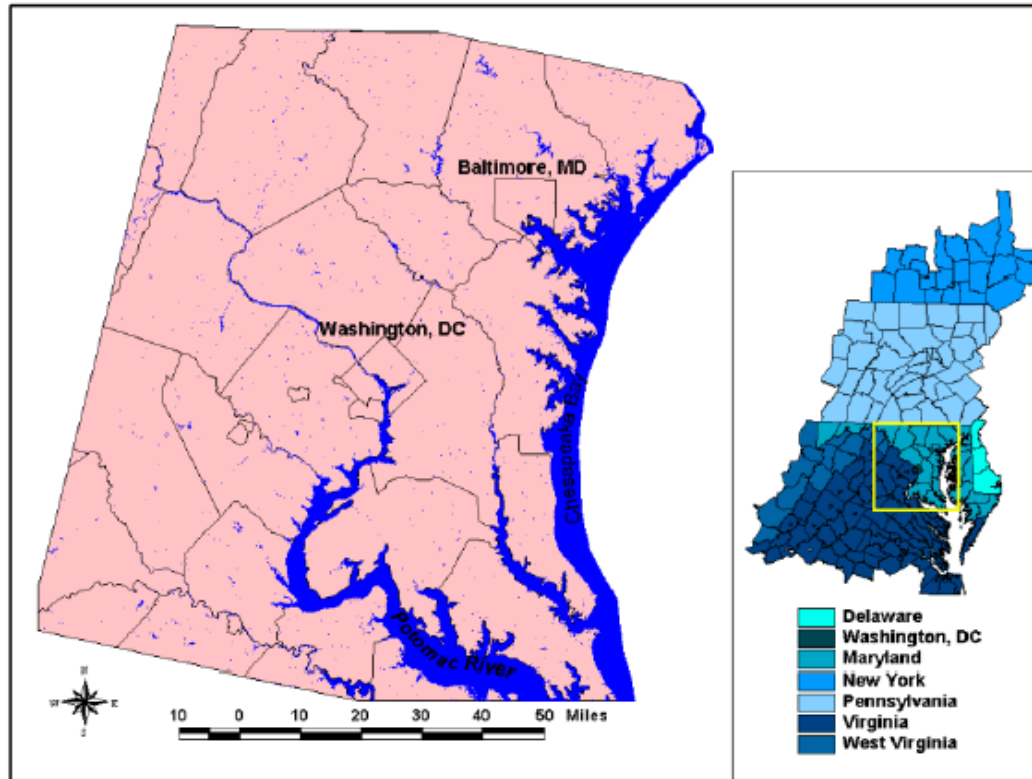


$t = 4$



Rinaldi E (1999). "The Multi-Cellular Automaton: a tool to build more sophisticated models. A theoretical foundation and a practical implementation" in Rizzi P. e Savino M. (eds) *On the edge of the Millennium. Proceedings of Computer in Urban Planning and Urban Management 6th International Conference* F. Angeli 1999 (in pubblicazione) e in *Proceedings ESIT Creta* (in pubblicazione)

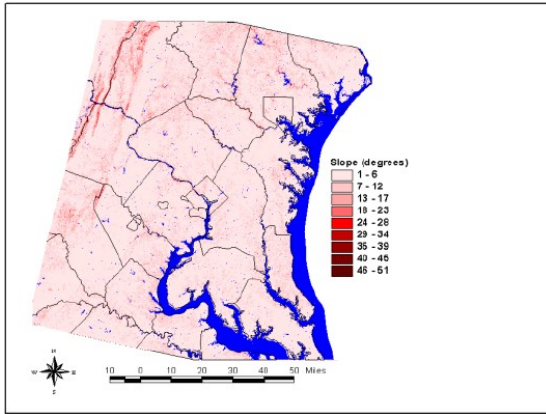
# CA Applications: urban growth



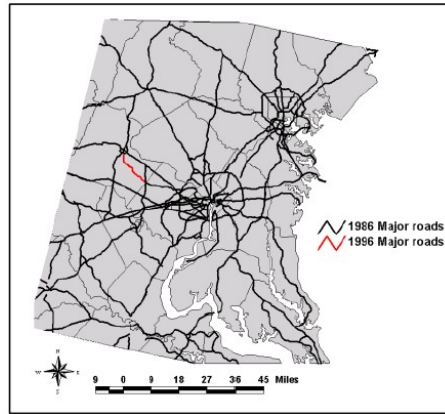
**Model of Future Growth in the Washington, DC-Baltimore Region 1986-2030 using the SLEUTH model**

# SLEUTH growth coefficients

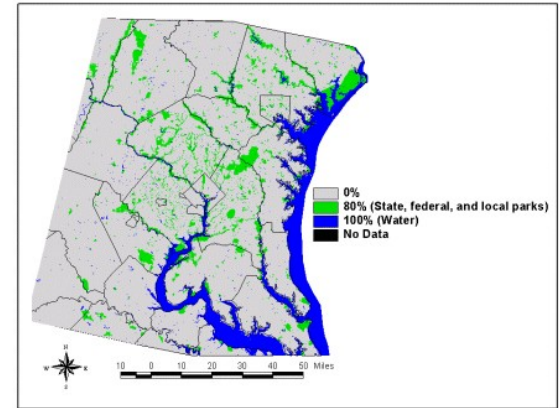
- dispersion coefficient
  - spontaneous or road influenced growth
- breed coefficient
  - new spreading centre or road influenced growth
- spread coefficient
  - edge growth from spreading centre
- slope coefficient
  - lower slopes are easier to build on
- road gravity coefficient
  - distance from road influences growth



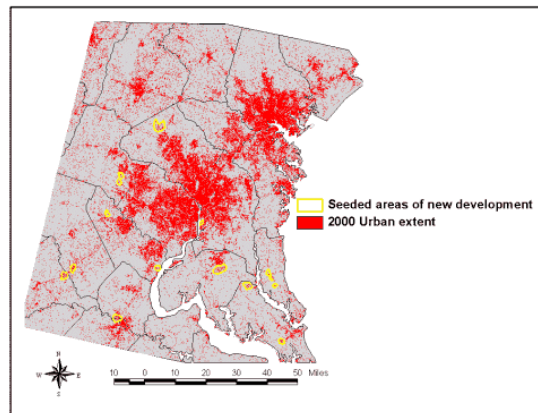
slope



roads



excluded areas

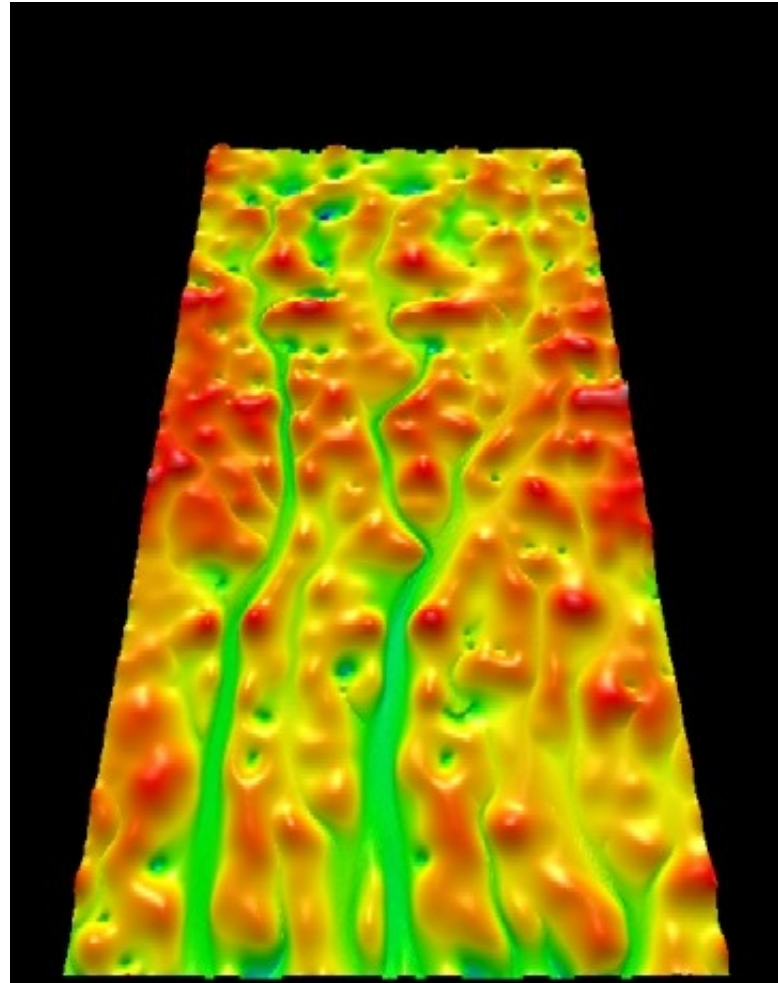


CA results



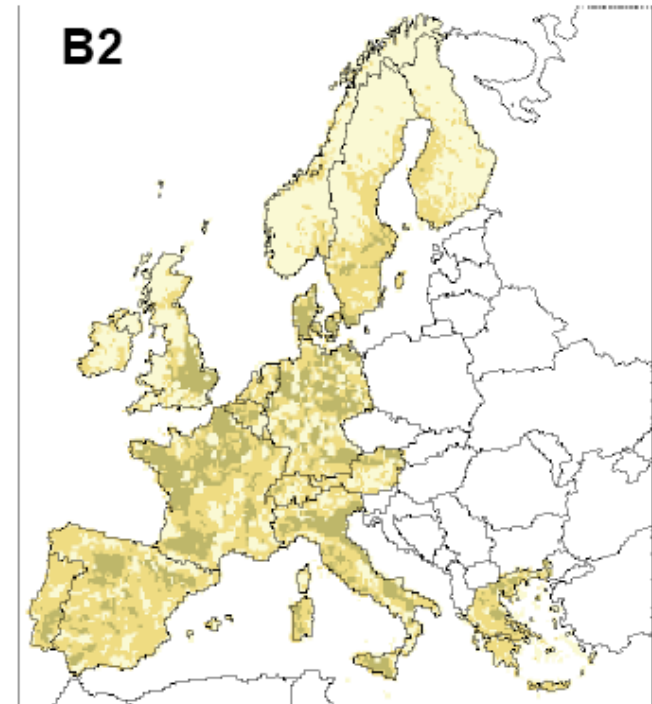
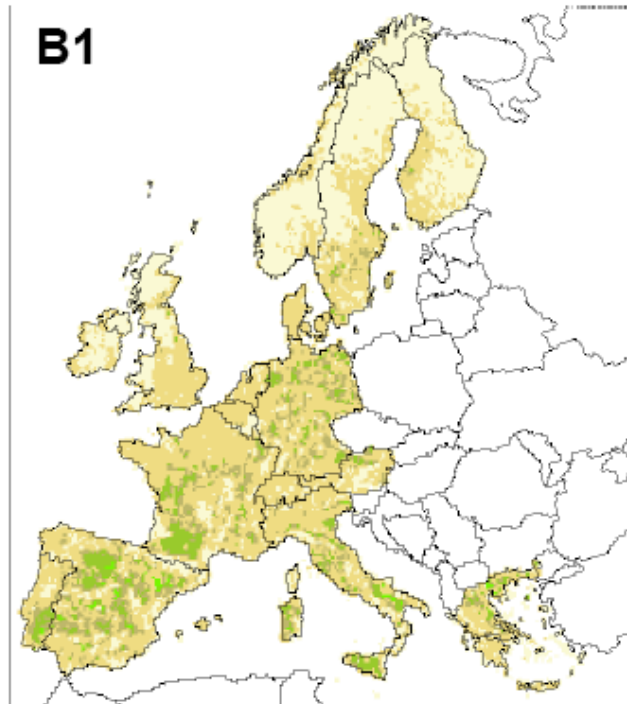
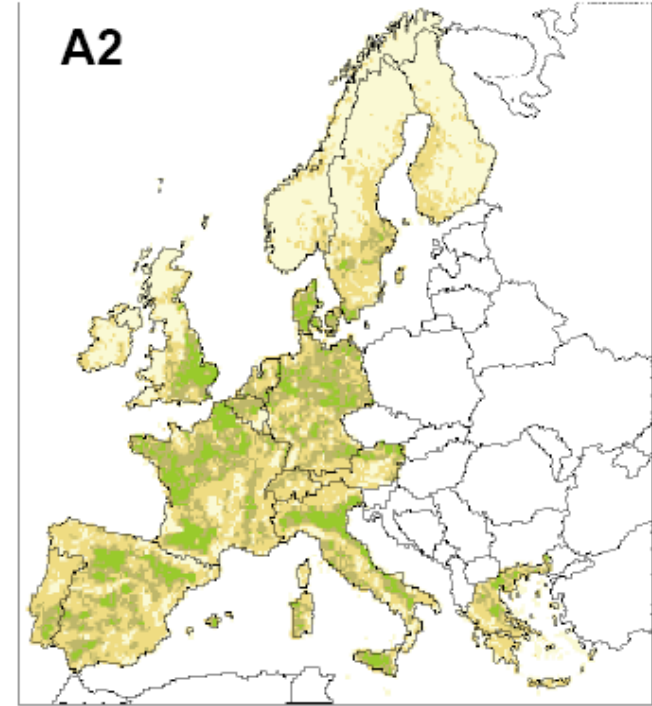
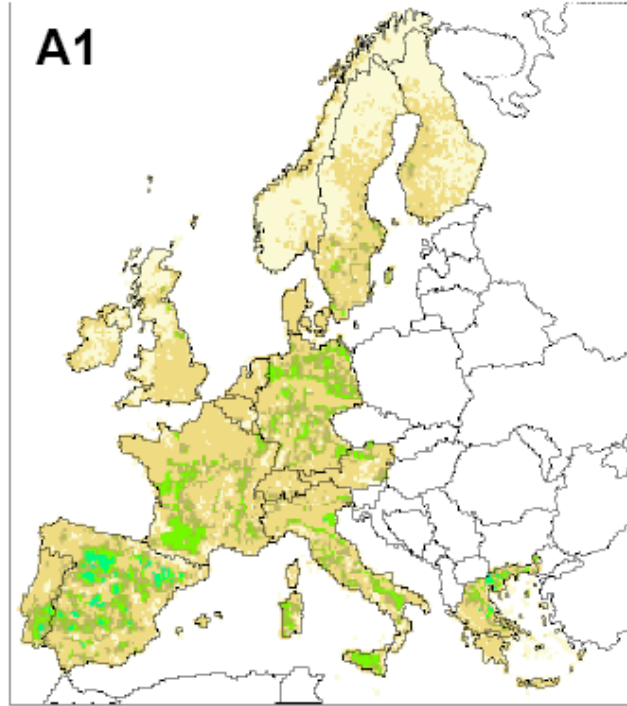
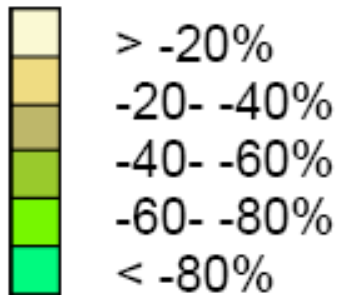
# CA Applications: Soil Erosion

- RillGrow 2 by Favis-Mortlock



# CELLULAR AUTOMATA IN INTEGRATED MODELLING

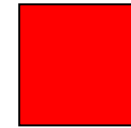
**Change in cropland area (for food production) by 2080 compared to baseline (%) for the 4 SRES storylines and HADCM3**



After: Schröter et al. (2005).  
Ecosystem service supply and  
vulnerability to global change in  
Europe. *Science*, **310** (5752),  
1333-1337

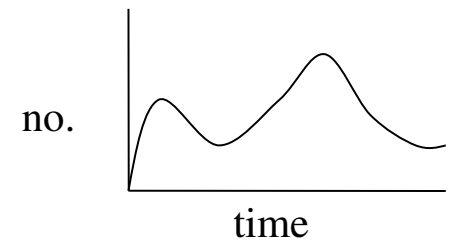
# Analysis of CA Output

- Plot cell attributes



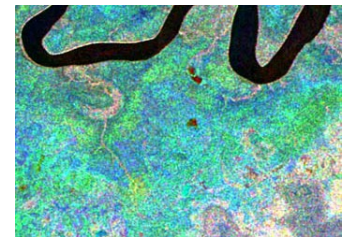
Height  
Mass  
Land Use....etc

- Plot number of cells in certain state



- Use metrics for describing spatial pattern

e.g. patch size metrics



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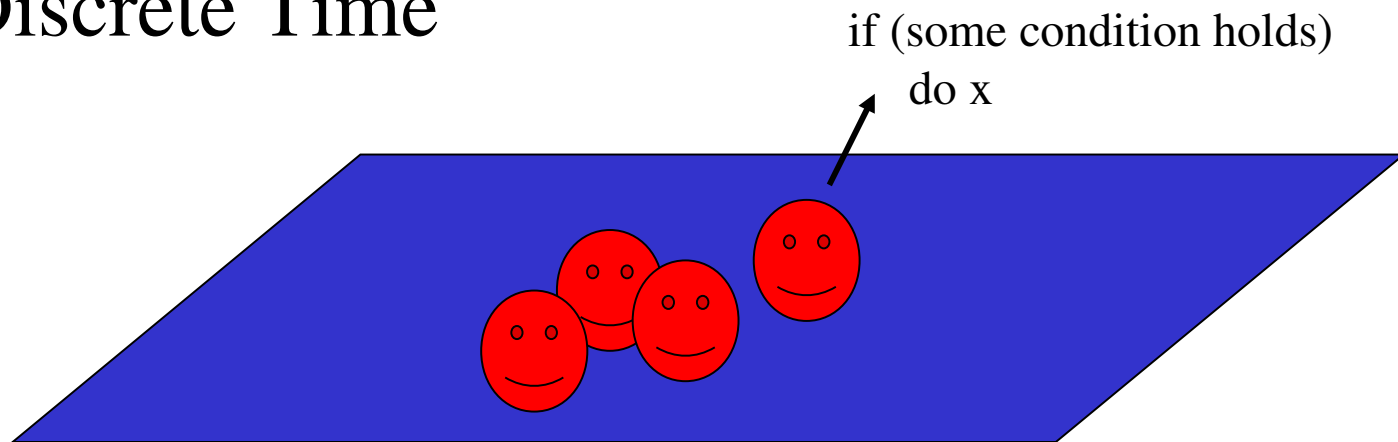
# Agent Based Model (ABM)

A representation of a system in which *agents* interact with each other and their *environment* using a set of rules

- Also called multi-agent systems (MAS)

# ABM Components

- Space (environment)
- Agent(s) — rules defining interaction and neighbourhoods
- Discrete Time



# what is an agent?

Represents:

- some discrete thing in the world (usually a living thing)
- something with behaviour

Representation:

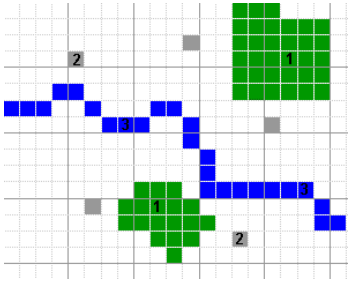
- Physically - Geometric object
- Programmed – an object with attributes and behaviour

# agent

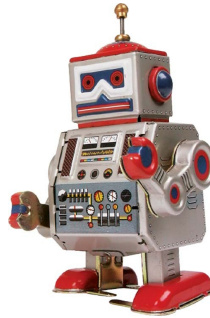
- behaviour:
  - Rational – deterministic / Stochastic
  - e.g. BDI algorithm
- communication:
  - Stigmergic
  - Message passing



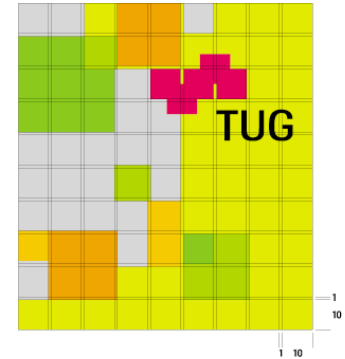




+



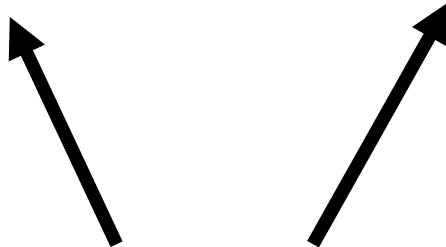
=



same initial conditions

deterministic  
agents

same final state



+stochasticity

# Environmental Examples

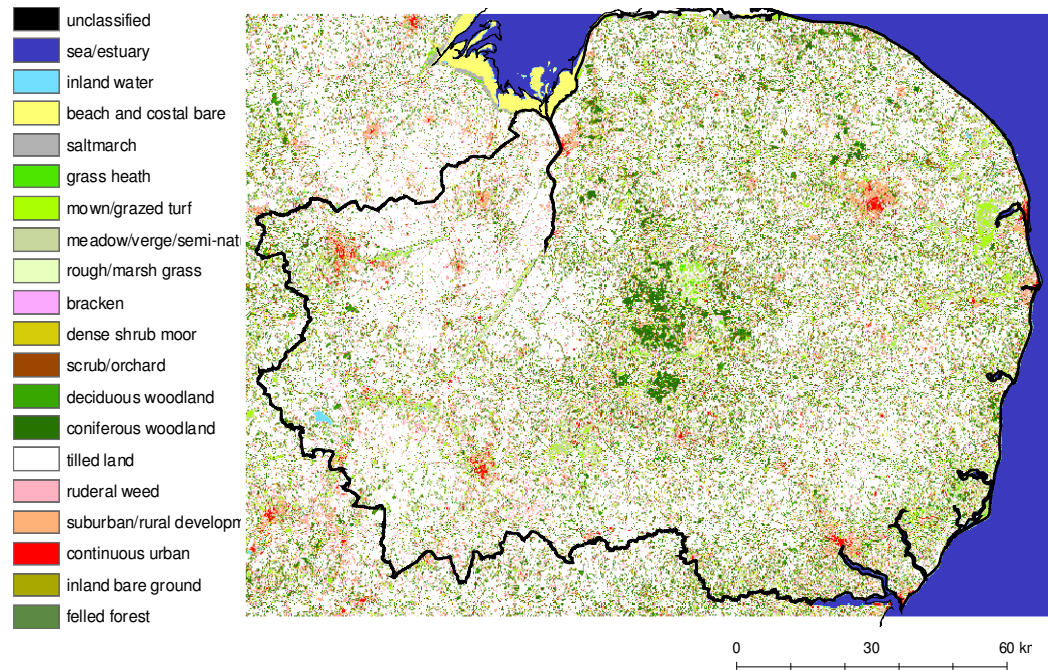
?

# Types of ABM

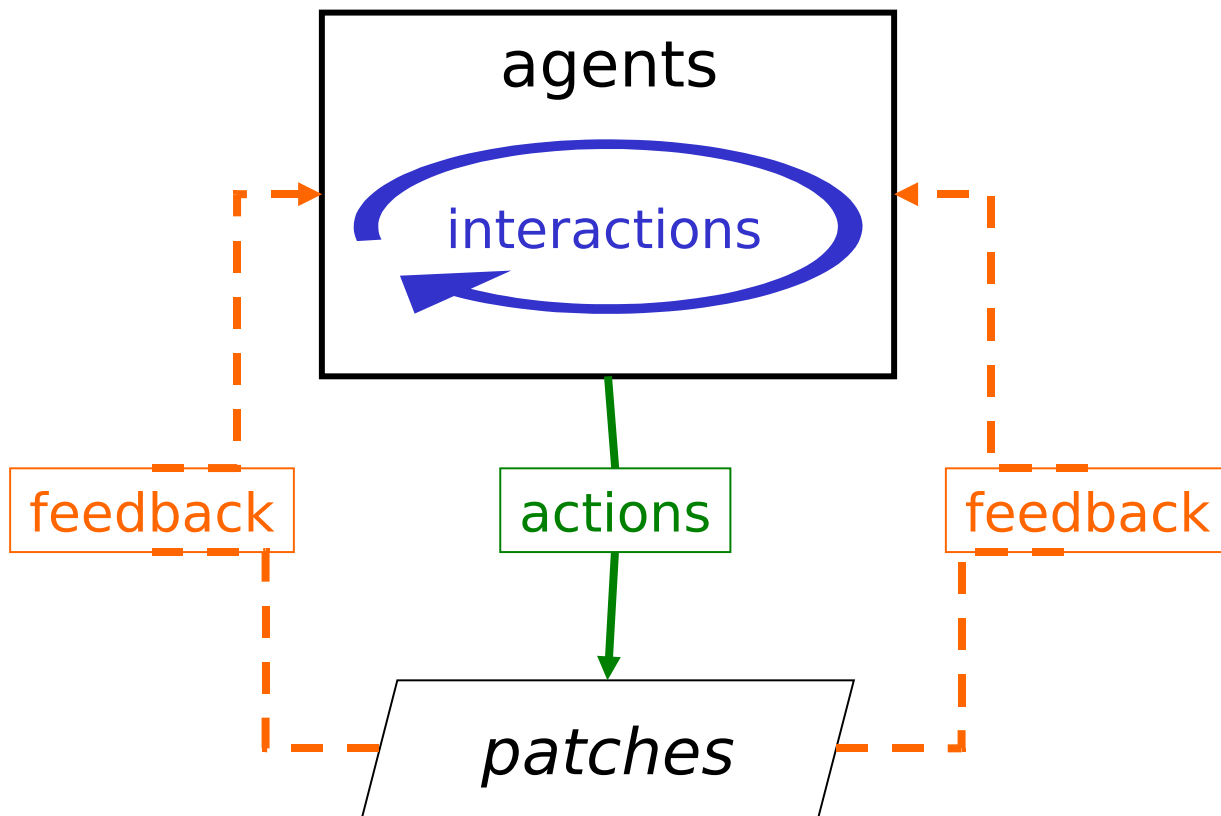
- Fixed behaviour model vs. evolutionary model
  - e.g. genetic algorithms
- Top down vs. or plus bottom up

# Example – urban land use in East Anglia

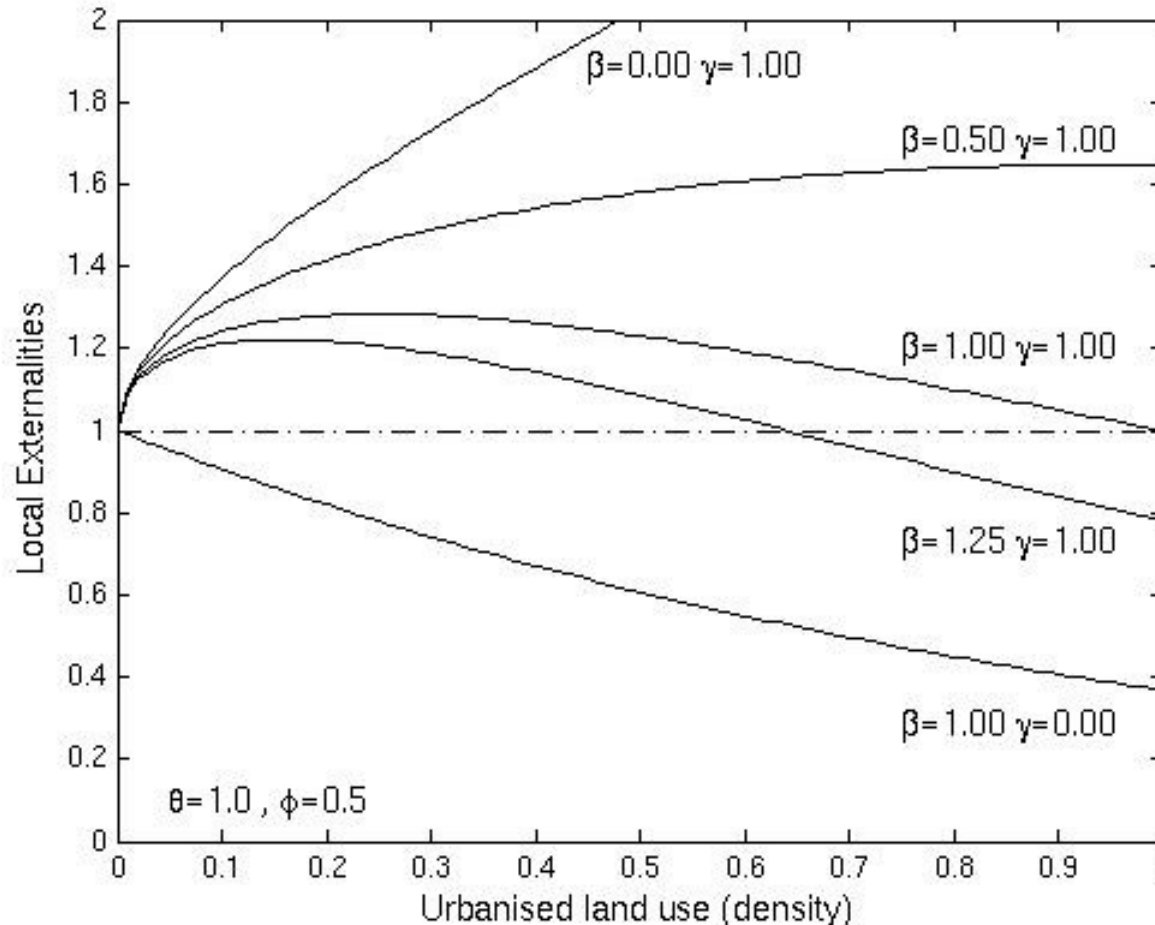
- Endogenising the planning process



Source: Lilibeth Acosta-Michlik and Corentin Fontaine; funded by the Tyndall Centre



# Agent-environment interaction



$\beta$  and  $\gamma$  are parameters affecting preferences for landscape and service amenities, respectively

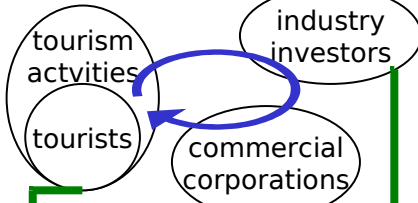
# agents

## public sector

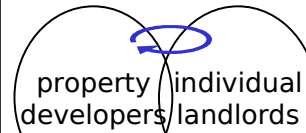


## private sector

### non-residential

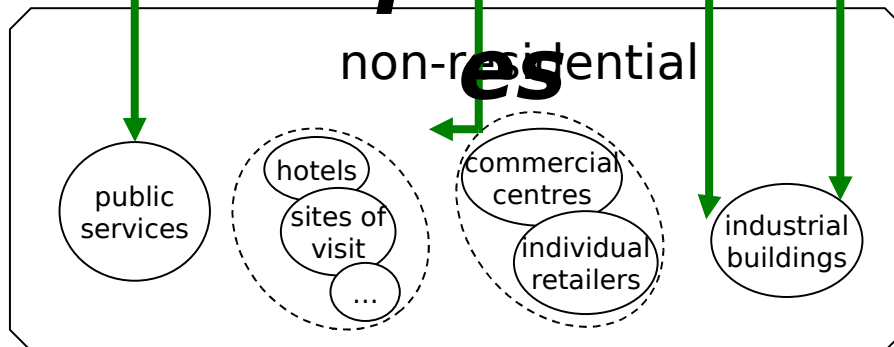


### residential

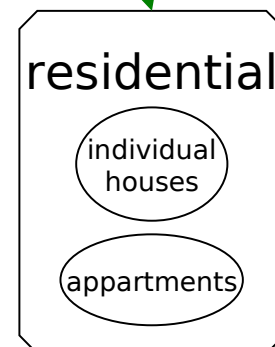


# patches

## non-residential



## residential



feedback

feedback

# Residential agents

- Socio-economic data analysis
- Agent profiles (household types) & location trends

		CLUSTERS											
		1	2	3	4	5	6	7	8	9	10	11	12
isolated student	HA1										++	+	+++
single person	HA2							+	+++	++	++	+	
couple	HA3		++	+	+			+++	++		+++	++	
couple with dep. children	HA4			+		++		+++		+	+		
single-parent family	HA5					+++	++			++			+
couple with non-dep. children	HA6	+++	++	+	+								
all retired	HA7	+	+		+++		++						+



# Household agent location preferences

## Legend

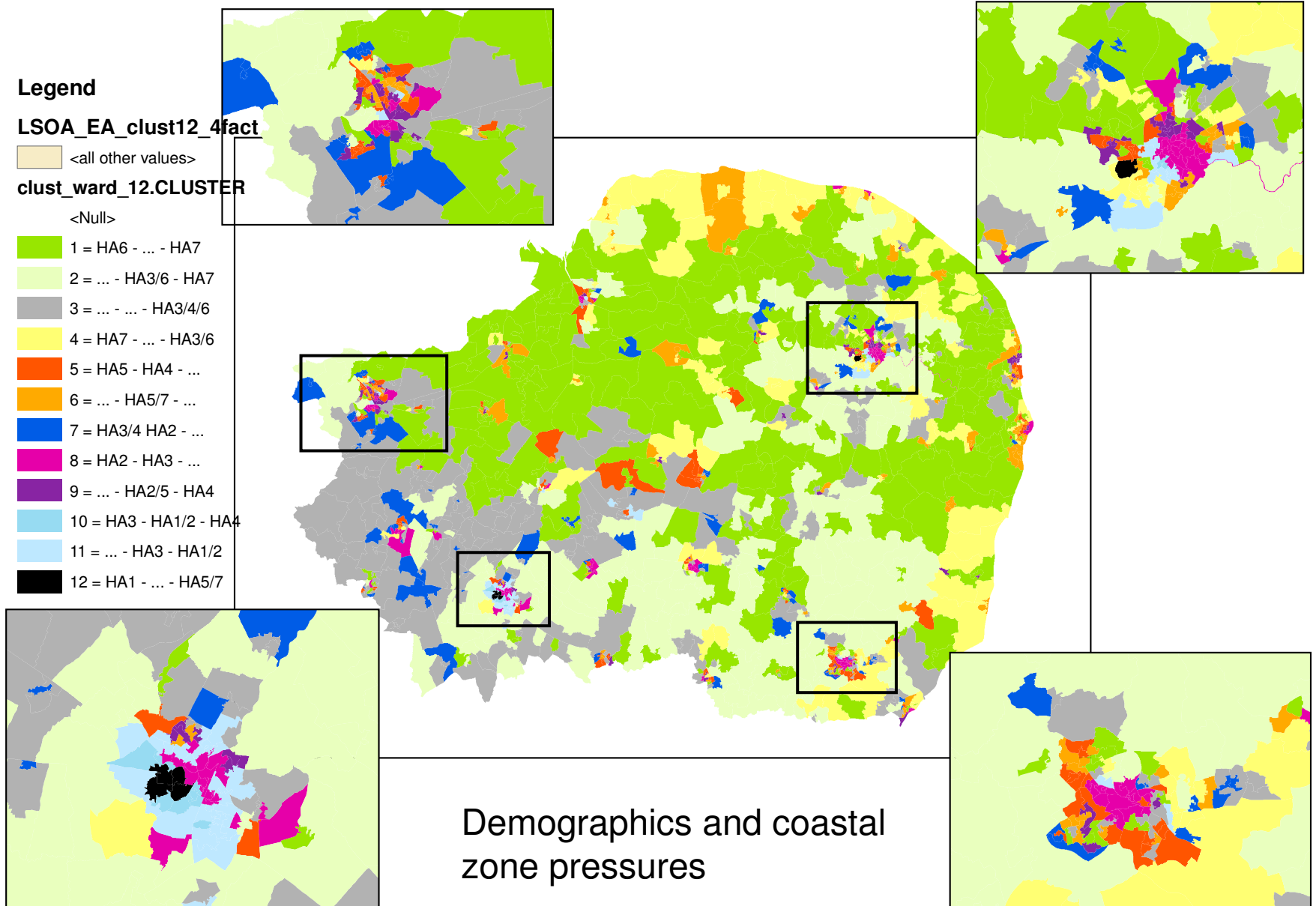
LSOA\_EA\_clust12\_4fact

<all other values>

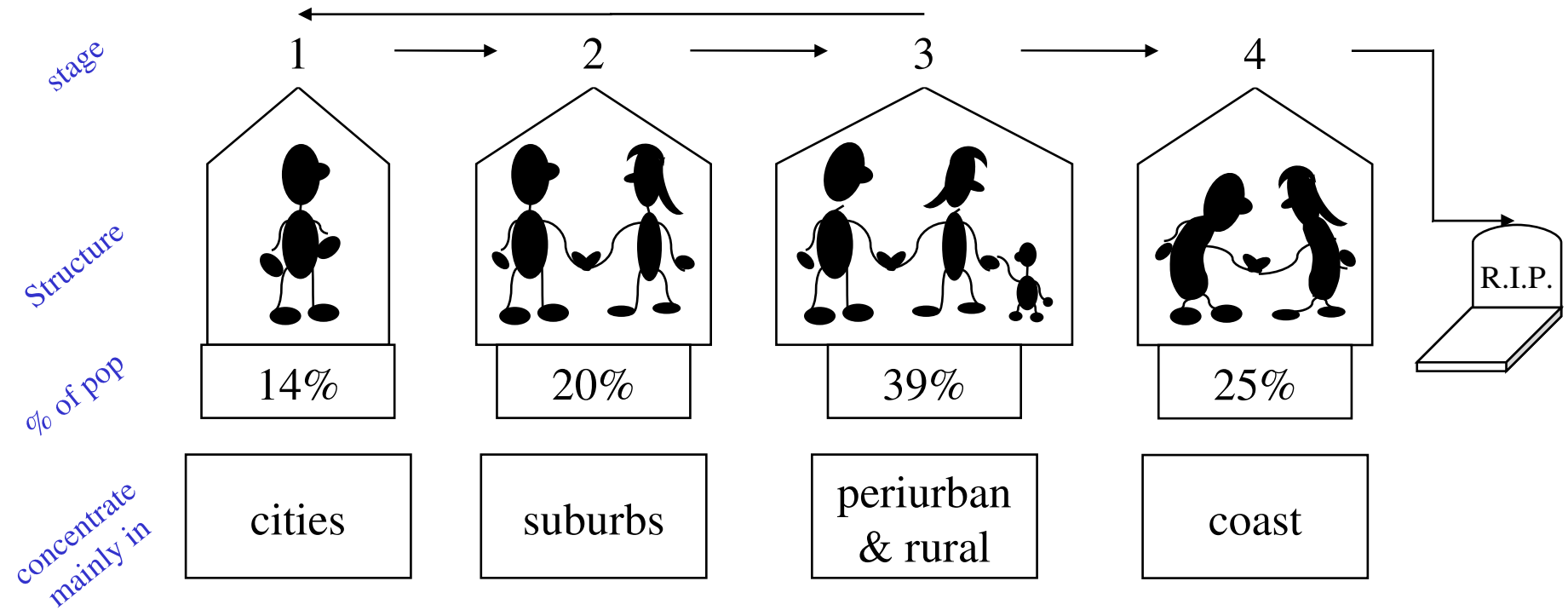
clust\_ward\_12.CLUSTER

<Null>

- 1 = HA6 - ... - HA7
- 2 = ... - HA3/6 - HA7
- 3 = ... - ... - HA3/4/6
- 4 = HA7 - ... - HA3/6
- 5 = HA5 - HA4 - ...
- 6 = ... - HA5/7 - ...
- 7 = HA3/4 HA2 - ...
- 8 = HA2 - HA3 - ...
- 9 = ... - HA2/5 - HA4
- 10 = HA3 - HA1/2 - HA4
- 11 = ... - HA3 - HA1/2
- 12 = HA1 - ... - HA5/7

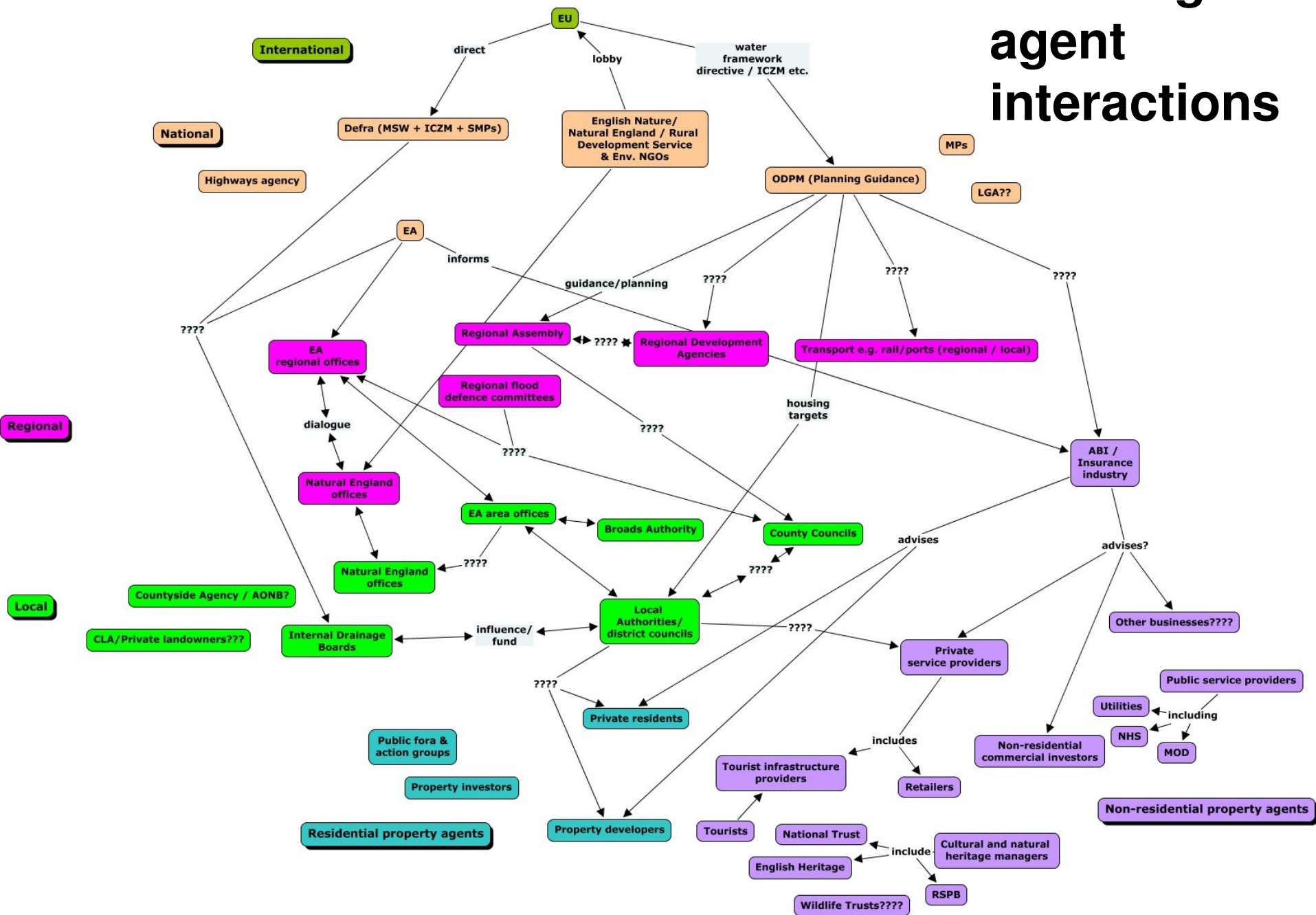


# Residential model runs



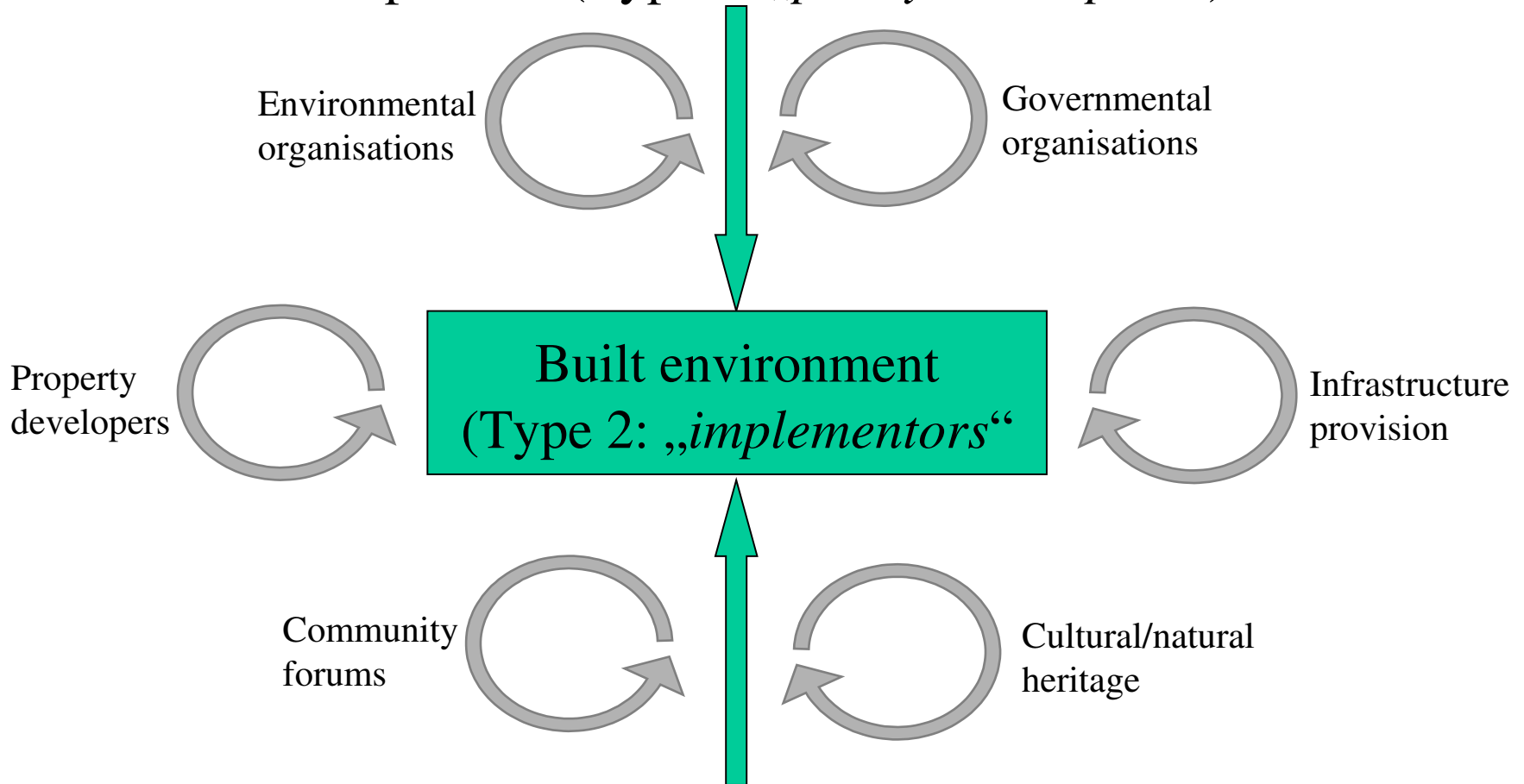
Model run animation

# Planning agent interactions



# Conceptual planning model

Top-down (Type 1: „*policy developers*“)



Bottom-up: (Type 3 „*lobbyists*“)

# ABM as Computational Laboratory

- Testing hypotheses
- Testing methodologies
- Is your ABM deterministic or has it got a stochastic component?
- How many simulations is enough?
- How do we interpret model results?
- Statistical analysis of results

# Analysis of ABM Output

- Plot agent attributes
- Plot number of agents of certain type
- Spatial pattern metrics
  - temporal considerations (at a time or over time)

# Difference between CA and ABM

?

# What is the goal of modelling?

- to predict the represented system?
- to understand and explain the represented system?



# References

## General Modelling:

- Zeigler, B. P., H. Praehofer, and T. G. Kim, 2000. *Theory of Modeling and Simulation: integrating discrete event and continuous complex dynamic systems*. Academic Press, San Diego.

## CA:

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## ABM:

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- Gimblett, H. R., Ed., 2002: *Integrating Geographic Information Systems and Agent-Based Modeling Techniques for Simulating Social and Ecological Processes*. Sante Fe Institute Studies in the Sciences of Complexity, Oxford University Press.
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- Papers on the RePast site: [repast.sourceforge.net/papers](http://repast.sourceforge.net/papers)