Notes about correlation (for Asgn 2)

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Overview of assignment

Exploration of distributional similarity.

- Work with data extracted from Twitter (co-occurrence counts)
- Compare different ways to contruct context vectors and compute similarities
- Analyze and discuss differences between approaches, qualitatively and quantitatively.

Work through the lab **before** you start the assignment!

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Correlation

1

Qualitative and quantitative analysis

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Assignment asks you to do some of each.

- Examples of qualitative analysis:
- Using visualization to illustrate/discuss examples or trends
- Discussing one or a few examples in more detail, by looking at our dataset and/or other Tweets (e.g., use the Twitter search page).
- Examples of quantitative analysis:
- Often: numerical comparison to a gold standard of accuracy
- Here: consider other options, such as correlating similarity measures against word frequency.

One kind of quantitative analysis

- Assignment spec suggests you may want to consider **correlation** between similarity measures and word frequency.
- Why?
 - A good similarity measure should measure (only) similarity.
 - So presumably *not* be correlated with frequency.
 - Unless more frequent words really are more similar to each other! (Would need to test with humans... let's assume not)

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2

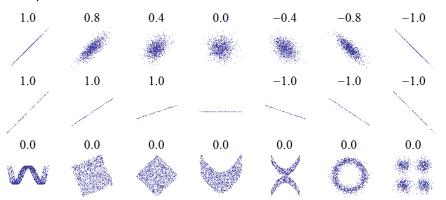
What is correlation?

- Intuitively: two random variables X and Y are **correlated** if, when the value of X increases, the value of Y also tends to increase (positive correlation) or decrease (negative correlation).
- \bullet Often, X and Y are different measurements for each data point.
- A person's height X and weight Y
- A word's frequency X and length Y
- Two standard ways to measure correlation:
- Spearman (rank) correlation: roughly as above.
- Pearson (linear) correlation: more specific.

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Pearson correlation



Examples datasets with Pearson r values shown:

Image source: https://commons.wikimedia.org/wiki/File:Correlation_examples.png

Pearson correlation

- Mathematically: the covariance of X and Y, normalized by the product of their individual standard deviations.
- Intuitively: if I plot X against Y, how close to a perfect linear relationship do I see?
 - Does not measure the *slope* of the line, just whether there is one. (Compare rows 1 and 2, next page.)
 - Does not tell us if there's some other *non-linear* relationship between X and Y. (See row 3, next page.)
- \bullet For data samples, the Pearson correlation coefficient is usually denoted r.

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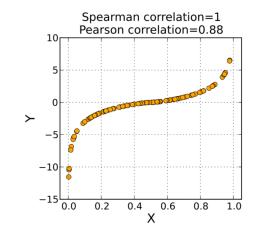
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5

Spearman rank correlation

- Mathematically: compute the Pearson correlation between the **rank ordering** of *X* and *Y* values.
- Intuitively: how close to a perfectly monotonic relationship do X and Y have? (i.e., when X increases, Y increases)
- \bullet For data samples, the Spearman rank correlation coefficient is usually denoted ρ or $r_s.$

Spearman correlation



Data with perfect rank correlation, but not perfectly linear:

Image by Skbkekas (CC-BY-SA 3.0)

https://en.wikipedia.org/wiki/Spearman\%27s_rank_correlation_coefficient

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But usually we do know something

Best to look at the data first! For example, word freq vs length:

Frequency

Seems to follow a pattern, but not strongly 1 linear. Indeed, 1

- Spearman: $\rho = -0.18$
- Pearson: r = -0.10

(Note: I "jittered" the data so those with same (x,y) are not right on top of each other.)

Which one to use?

- If correlation is roughly linear, Pearson will normally yield stronger results (larger absolute values)
 - If hypothesis testing against the possibility of no correlation, likely to have higher significance level than Spearman.
 - But if using large samples from corpora, often nearly *any* result is clearly "non-zero". We may care more about the actual degree of correlation.
- If correlation is non-linear, or nothing is known, use Spearman.

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9

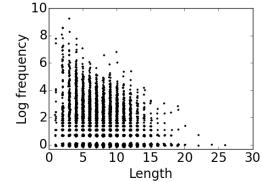
Log frequency

Of course, using log frequencies is often more sensible:

We now have

- Spearman: $\rho = -0.18$
- Pearson: r = -0.21

Notice that ρ is not affected by rescaling the data. r is higher, but still only a weak linear correlation.



8

So, which one to use?

- So, Pearson can still work if there is an obvious tranformation to make the correlation roughly linear.
- But if in doubt, usually fine to use Spearman.
- As with all statistics, many subtleties if using for really careful analysis (see statistics course or online tutorials), but what I've said is probably enough for exploratory studies (i.e., your assignment).

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12