Algorithms and Data Structures 2023/24 Week 9 tutorial sheet

Below are a list of *suggested* exercises. You should also see the tutorial as a resource to get answers to questions you have, don't feel compelled to stick to the sheet.

- 1. Draw an example of a weighted graph which has 2 MSTs.
- 2. Let G, W be a weighted graph in which all edge weights are distinct. Prove that the MST of G, W is unique.
- 3. In line 3 of Prim's algorithm, there may be more than one fringe edge of minimum weight. Suppose we add all these minimum edges in one step. Does the algorithm still compute a MST?
- 4. Kruskal's algorithm can return different spanning trees for the same input graph G, depending on how ties are broken when the edges are initially sorted. Show that for every MST T of G, there is some way to sort the edges of G in Kruskal's algorithm so that T will be the MST that is returned.