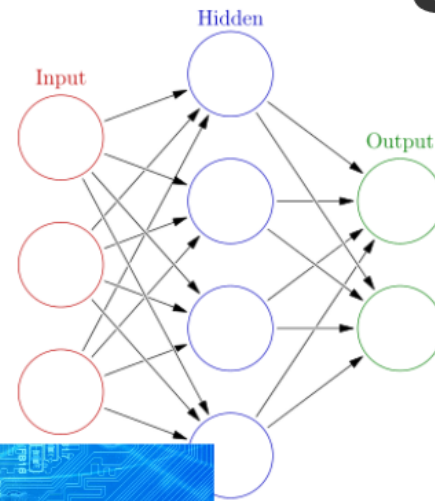
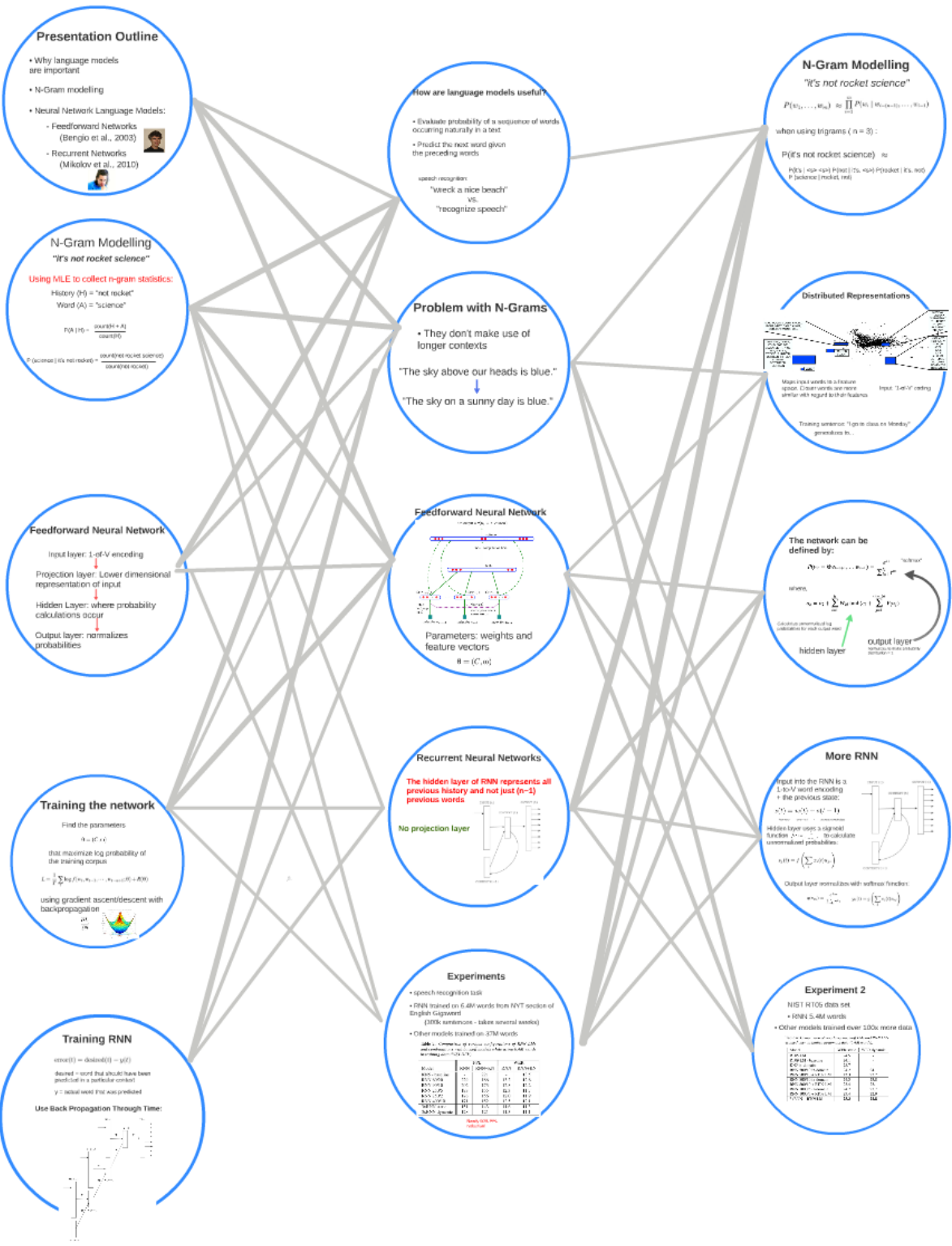


Neural Network Language Modelling

$$\prod_{i=1}^m P(w_i | w_{i-(n-1)}, \dots, w_{i-1})$$





Presentation Outline

- Why language models are important
- N-Gram modelling
- Neural Network Language Models:
 - Feedforward Networks
(Bengio et al., 2003)
 - Recurrent Networks
(Mikolov et al., 2010)



How are language models useful?

- Evaluate probability of a sequence of words occurring naturally in a text
- Predict the next word given the preceding words

speech recognition:

"wreck a nice beach"

vs.

"recognize speech"

N-Gram Modelling

"it's not rocket science"

$$P(w_1, \dots, w_m) \approx \prod_{i=1}^m P(w_i | w_{i-(n-1)}, \dots, w_{i-1})$$

when using trigrams ($n = 3$) :

$P(\text{it's not rocket science}) \approx$

$P(\text{it's} | \langle s \rangle \langle s \rangle) P(\text{not} | \text{it's}, \langle s \rangle) P(\text{rocket} | \text{it's}, \text{not})$
 $P(\text{science} | \text{rocket}, \text{not})$

N-Gram Modelling

"it's not rocket science"

Using MLE to collect n-gram statistics:

History (H) = "not rocket"

Word (A) = "science"

$$P(A | H) = \frac{\text{count}(H + A)}{\text{count}(H)}$$

$$P(\text{science} | \text{it's not rocket}) = \frac{\text{count}(\text{not rocket science})}{\text{count}(\text{not rocket})}$$

Problem with N-Grams

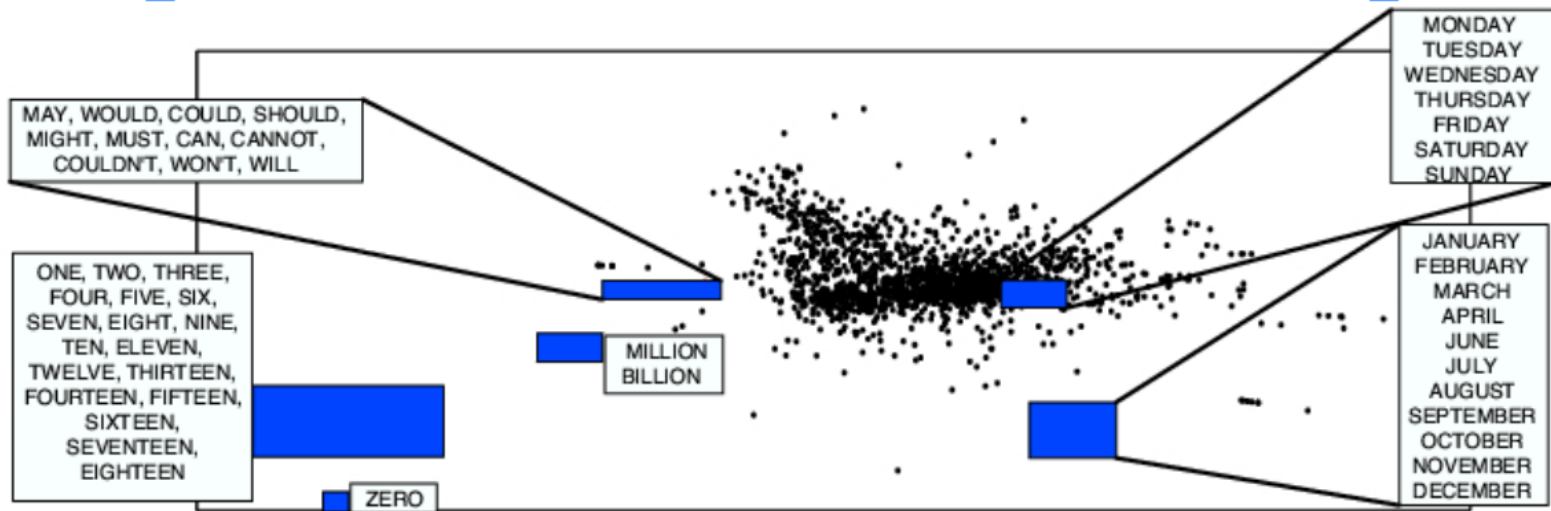
- They don't make use of longer contexts

"The sky above our heads is blue."



"The sky on a sunny day is blue."

Distributed Representations



Maps input words to a feature space. Closer words are more similar with regard to their features

Input: '1-of-V' coding

Training sentence: "I go to class on Monday"
generalizes to...

Feedforward Neural Network

Input layer: 1-of-V encoding



Projection layer: Lower dimensional representation of input

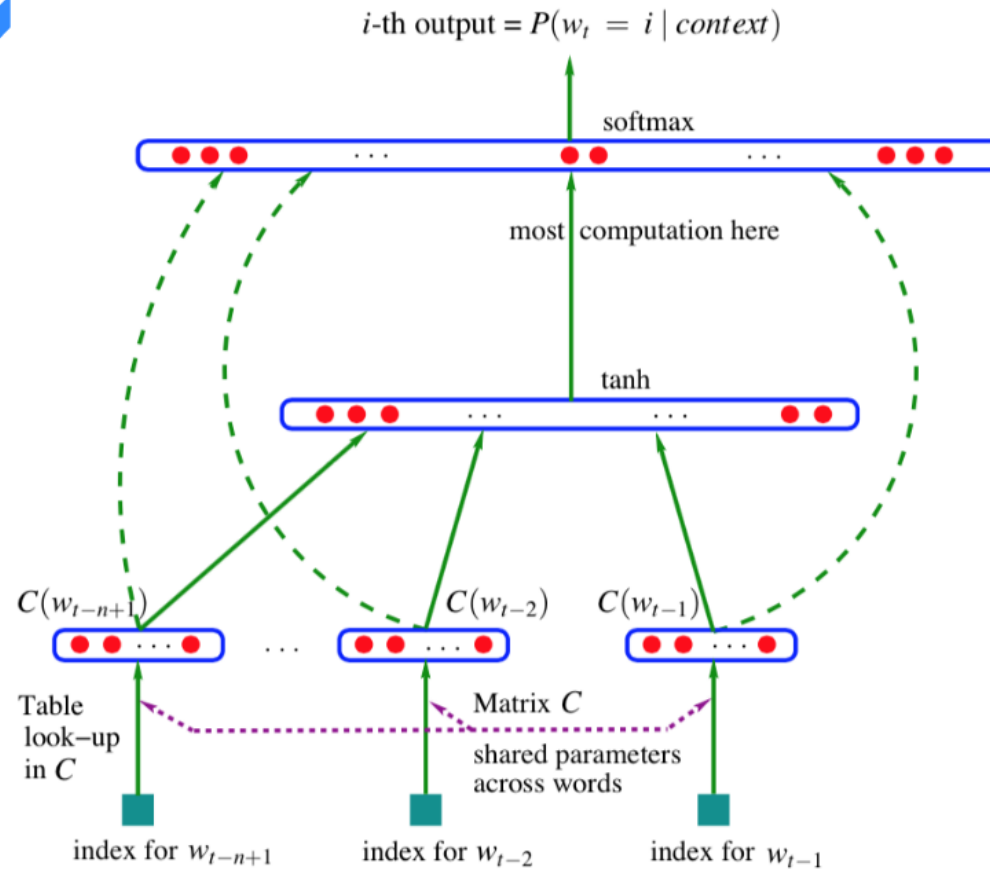


Hidden Layer: where probability calculations occur



Output layer: normalizes probabilities

Feedforward Neural Network



Parameters: weights and feature vectors

$$\theta = (C, \omega)$$

The network can be defined by:

$$P(w_t = k | w_{t-n+1}, \dots, w_{t-1}) = \frac{e^{a_k}}{\sum_{l=1}^N e^{a_l}} \quad \text{"softmax"}$$

where,

$$a_k = b_k + \sum_{i=1}^h W_{ki} \tanh\left(c_i + \sum_{j=1}^{(n-1)d} V_{ij} x_j\right)$$

Calculates unnormalized log probabilities for each output word

hidden layer

output layer

normalizes to make probability distribution = 1

Training the network

Find the parameters

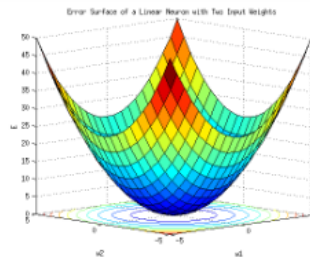
$$\theta = (C, \omega)$$

that maximize log probability of
the training corpus

$$L = \frac{1}{T} \sum_t \log f(w_t, w_{t-1}, \dots, w_{t-n+1}; \theta) + R(\theta)$$

using gradient ascent/descent with
backpropagation

$$\frac{\partial L}{\partial \theta}$$



Experiment

- Trained on 800,000 words in Brown corpus

- 24% lower perplexity than modified Kneser-Kney

- Context length of 5 worked best for the feedforward model

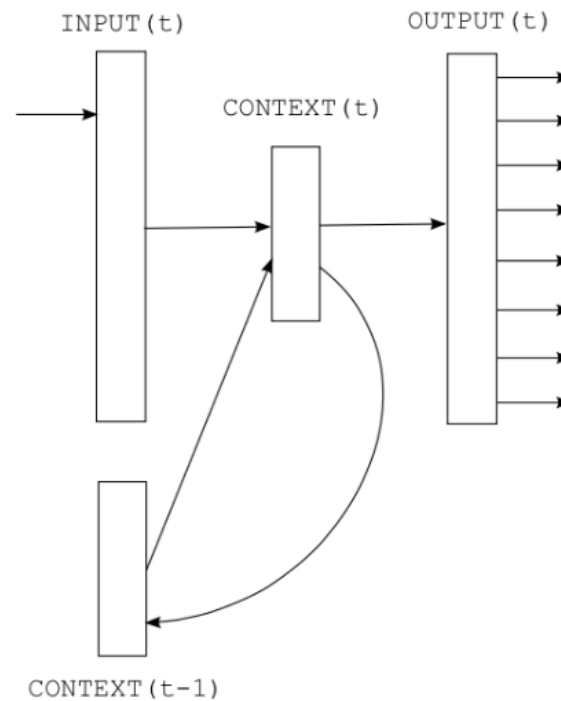
- Trigrams worked best for the Kneser-Kney

Do feedforward networks really make use of longer contexts?

Recurrent Neural Networks

The hidden layer of RNN represents all previous history and not just $(n-1)$ previous words

No projection layer



More RNN

Input into the RNN is a 1-to-V word encoding + the previous state:

$$x(t) = w(t) + s(t - 1)$$

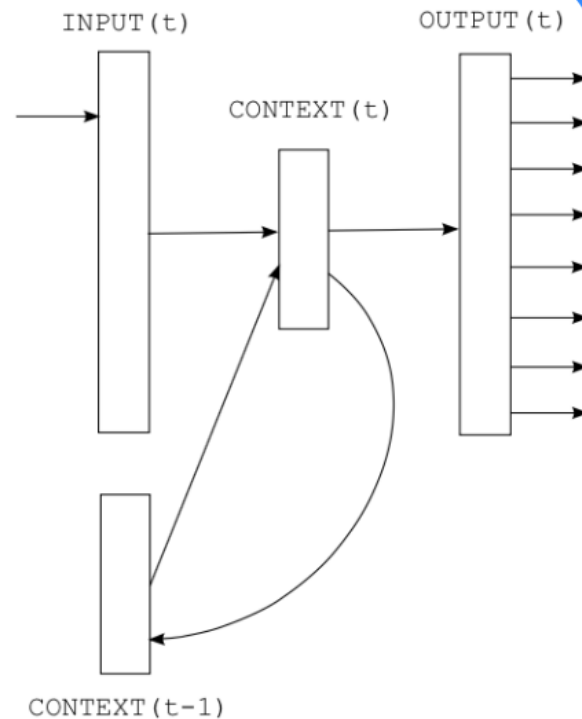
input vector = current word + previous network state

Hidden layer uses a sigmoid function $f(z) = \frac{1}{1 + e^{-z}}$ to calculate unnormalized probabilities:

$$s_j(t) = f\left(\sum_i x_i(t)u_{ji}\right)$$

Output layer normalizes with softmax function:

$$g(z_m) = \frac{e^{z_m}}{\sum_k e^{z_k}} \quad y_k(t) = g\left(\sum_j s_j(t)v_{kj}\right)$$



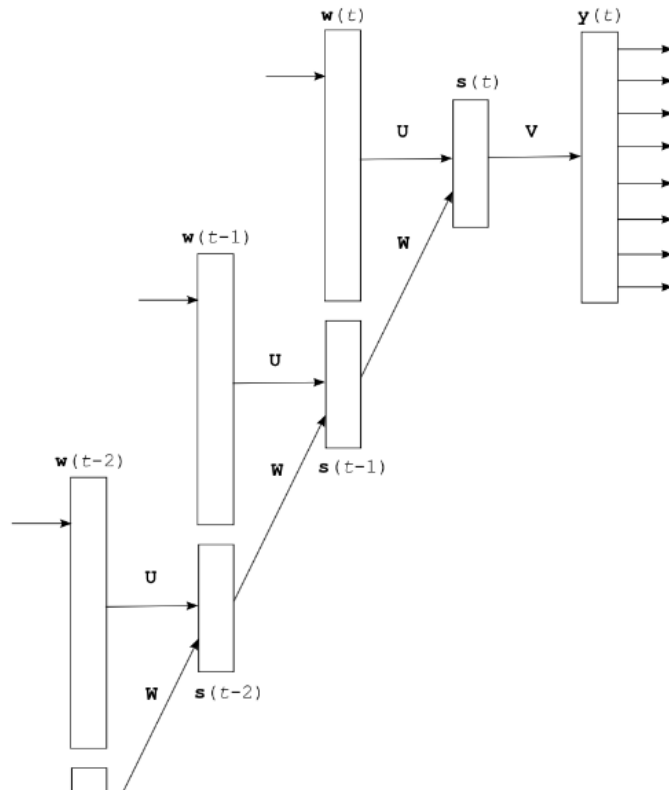
Training RNN

$$\text{error}(t) = \text{desired}(t) - y(t)$$

desired = word that should have been predicted in a particular context

y = actual word that was predicted

Use Back Propagation Through Time:



Experiments

- speech recognition task
- RNN trained on 6.4M words from NYT section of English Gigaword
(300k sentences - takes several weeks)
- Other models trained on 37M words

Table 2: Comparison of various configurations of RNN LMs and combinations with backoff models while using 6.4M words in training data (WSJ DEV).

Model	PPL		WER	
	RNN	RNN+KN	RNN	RNN+KN
KN5 - baseline	-	221	-	13.5
RNN 60/20	229	186	13.2	12.6
RNN 90/10	202	173	12.8	12.2
RNN 250/5	173	155	12.3	11.7
RNN 250/2	176	156	12.0	11.9
RNN 400/10	171	152	12.5	12.1
3xRNN static	151	143	11.6	11.3
3xRNN dynamic	128	121	11.3	11.1

Nearly 50% PPL
reduction!

Experiment 2

NIST RT05 data set

- RNN 5.4M words
- Other models trained over 100x more data

Table 4: Comparison of very large back-off LMs and RNN LMs trained only on limited in-domain data (5.4M words).

Model	WER static	WER dynamic
RT05 LM	24.5	-
RT09 LM - baseline	24.1	-
KN5 in-domain	25.7	-
RNN 500/10 in-domain	24.2	24.1
RNN 500/10 + RT09 LM	23.3	23.2
RNN 800/10 in-domain	24.3	23.8
RNN 800/10 + RT09 LM	23.4	23.1
RNN 1000/5 in-domain	24.2	23.7
RNN 1000/5 + RT09 LM	23.4	22.9
3xRNN + RT09 LM	23.3	22.8

questions...?