## Dependence and Data Flow Models



#### Why Data Flow Models?

- Models from Chapter 5 emphasized control
  - Control flow graph, call graph, finite state machines
- We also need to reason about dependence
  - Where does this value of x come from?
  - What would be affected by changing this?
  - ...
- Many program analyses and test design techniques use data flow information
  - Often in combination with control flow
    - Example: "Taint" analysis to prevent SQL injection attacks
    - Example: Dataflow test criteria (Ch.13)



#### Learning objectives

- Understand basics of data-flow models and the related concepts (def-use pairs, dominators...)
- Understand some analyses that can be performed with the data-flow model of a program
  - The data flow analyses to build models
  - Analyses that use the data flow models
- Understand basic trade-offs in modeling data flow
  - variations and limitations of data-flow models and analyses, differing in precision and cost

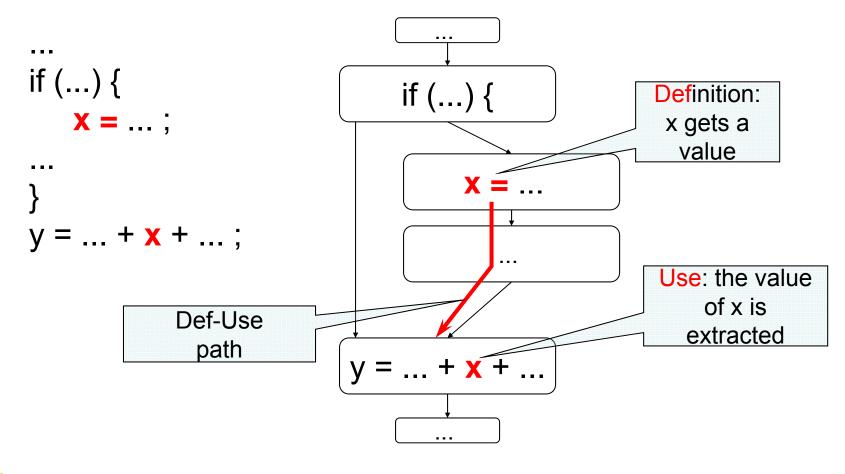


#### Def-Use Pairs (1)

- A def-use (du) pair associates a point in a program where a value is produced with a point where it is used
- Definition: where a variable gets a value
  - Variable declaration (often the special value "uninitialized")
  - Variable initialization
  - Assignment
  - Values received by a parameter
- Use: extraction of a value from a variable
  - Expressions
  - Conditional statements
  - Parameter passing
  - Returns

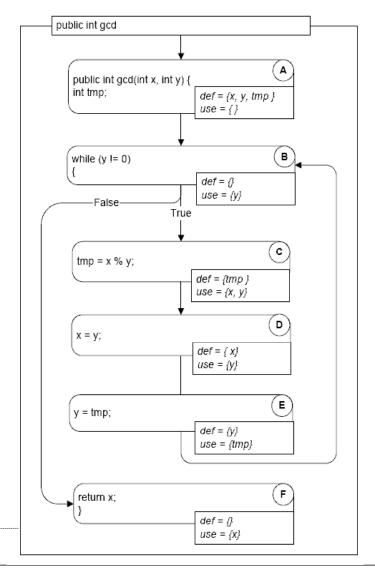


#### **Def-Use Pairs**





#### Def-Use Pairs (3)



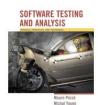


Figure 6.2, page 79

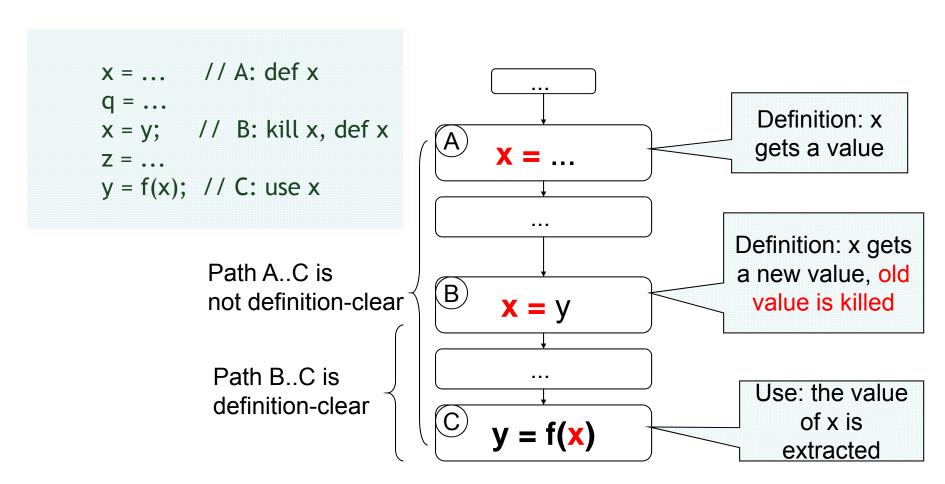
#### Def-Use Pairs (3)

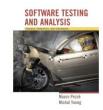
- A definition-clear path is a path along the CFG from a definition to a use of the same variable without\* another definition of the variable between
  - If, instead, another definition is present on the path, then the latter definition kills the former
- A def-use pair is formed if and only if there is a definition-clear path between the definition and the use



\*There is an over-simplification here, which we will repair later.

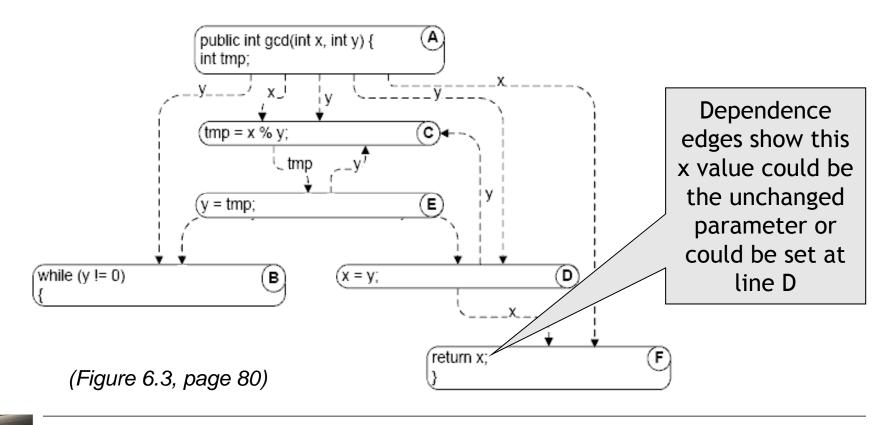
#### **Definition-Clear or Killing**





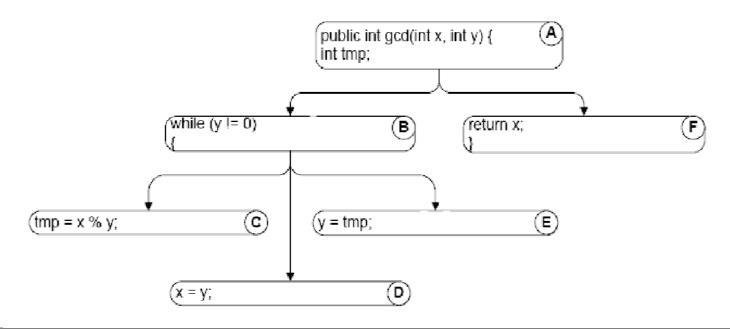
#### (Direct) Data Dependence Graph

- A direct data dependence graph is:
  - Nodes: as in the control flow graph (CFG)
  - Edges: def-use (du) pairs, labelled with the variable name



### Control dependence (1)

- Data dependence: Where did these values come from?
- Control dependence: Which statement controls whether this statement executes?
  - Nodes: as in the CFG
  - Edges: unlabelled, from entry/branching points to controlled blocks



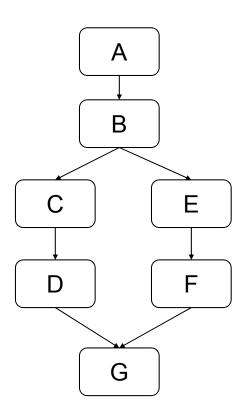


#### **Dominators**

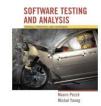
- Pre-dominators in a rooted, directed graph can be used to make this intuitive notion of "controlling decision" precise.
- Node M dominates node N if every path from the root to N passes through M.
  - A node will typically have many dominators, but except for the root, there is a unique immediate dominator of node N which is closest to N on any path from the root, and which is in turn dominated by all the other dominators of N.
  - Because each node (except the root) has a unique immediate dominator, the immediate dominator relation forms a tree.
- Post-dominators: Calculated in the reverse of the control flow graph, using a special "exit" node as the root.



#### Dominators (example)



- A pre-dominates all nodes; G post-dominates all nodes
- F and G post-dominate E
- G is the immediate postdominator of B
  - C does *not* post-dominate B
- B is the immediate predominator of G
  - F does *not* pre-dominate G

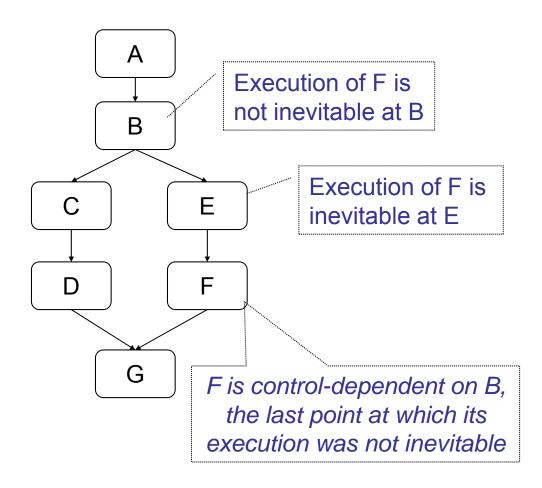


#### Control dependence (2)

- We can use post-dominators to give a more precise definition of control dependence:
  - Consider again a node N that is reached on some but not all execution paths.
  - There must be some node C with the following property:
    - C has at least two successors in the control flow graph (i.e., it represents a control flow decision);
    - C is not post-dominated by N
    - there is a successor of C in the control flow graph that is post-dominated by N.
  - When these conditions are true, we say node N is controldependent on node C.
    - Intuitively: C was the last decision that controlled whether N executed



#### **Control Dependence**





# **Data Flow Analysis**

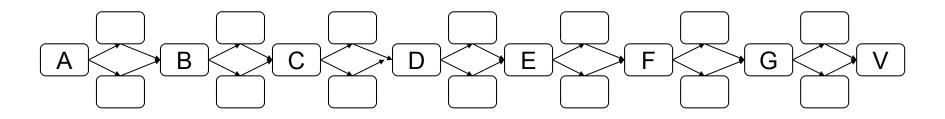
Computing data flow information



#### Calculating def-use pairs

- Definition-use pairs can be defined in terms of paths in the program control flow graph:
  - There is an association (d,u) between a definition of variable v at d and a use of variable v at u iff
    - there is at least one control flow path from d to u
    - with no intervening definition of v.
  - v<sub>d</sub> reaches u (v<sub>d</sub> is a reaching definition at u).
  - If a control flow path passes through another definition e of the same variable v,  $v_e$  kills  $v_d$  at that point.
- Even if we consider only loop-free paths, the number of paths in a graph can be exponentially larger than the number of nodes and edges.
- Practical algorithms therefore do not search every individual path.
   Instead, they summarize the reaching definitions at a node over all the paths reaching that node.

# Exponential paths (even without loops)



- 2 paths from A to B
- 4 from A to C
- 8 from A to D
- 16 from A to E

. . .

128 paths from A to V

Tracing each path is not efficient, and we can do much better.



#### **DF Algorithm**

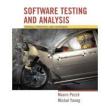
- An efficient algorithm for computing reaching definitions (and several other properties) is based on the way reaching definitions at one node are related to the reaching definitions at an adjacent node.
- Suppose we are calculating the reaching definitions of node n, and there is an edge (p,n) from an immediate predecessor node p.
  - If the predecessor node p can assign a value to variable v, then the definition  $v_p$  reaches n. We say the definition  $v_p$  is generated at p.
  - If a definition  $v_p$  of variable v reaches a predecessor node p, and if v is not redefined at that node (in which case we say the  $v_p$  is killed at that point), then the definition is propagated on from p to n.



### Equations of node E(y = tmp)

```
Calculate reaching definitions at E in terms of its immediate predecessor D
```

```
Reach(E) = ReachOut(D)
ReachOut(E) = (Reach(E) \ \{y_A\}) \cup \{y_F\}
```



#### Equations of node B (while (y != 0))

- Reach(B) = ReachOut(A) ∪ ReachOut(E)
- ReachOut(A) = gen(A) =  $\{x_A, y_A, tmp_A\}$
- ReachOut(E) = (Reach(E) \  $\{y_A\}$ )  $\cup \{y_E\}$

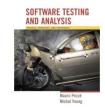


#### General equations for Reach analysis

Reach(n) = 
$$\bigvee$$
 ReachOut(m)  $m \in pred(n)$ 

ReachOut(n) = (Reach(n) \ kill (n)) 
$$\cup$$
 gen(n)

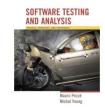
gen(n) = { 
$$v_n | v$$
 is defined or modified at n }  
kill(n) = {  $v_x | v$  is defined or modified at x, x $\neq$ n }



#### **Avail equations**

Avail (n) = 
$$\bigcap$$
 AvailOut(m)  
mepred(n)

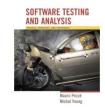
```
AvailOut(n) = (Avail (n) \ kill (n)) \cup gen(n)
```



#### Live variable equations

Live(n) = 
$$\bigcup$$
 LiveOut(m)  
m  $\in$  succ(n)

LiveOut(n) = (Live(n) \ kill (n)) 
$$\cup$$
 gen(n)



#### Classification of analyses

- Forward/backward: a node's set depends on that of its predecessors/successors
- Any-path/all-path: a node's set contains a value iff it is coming from any/all of its inputs

	Any-path (∪)	All-paths (∩)
Forward (pred)	Reach	Avail
Backward (succ)	Live	"inevitable"



#### Iterative Solution of Dataflow Equations

- Initialize values (first estimate of answer)
  - For "any path" problems, first guess is "nothing" (empty set) at each node
  - For "all paths" problems, first guess is "everything" (set of all possible values = union of all "gen" sets)
- Repeat until nothing changes
  - Pick some node and recalculate (new estimate)

This will converge on a "fixed point" solution where every new calculation produces the same value as the previous guess.



### Worklist Algorithm for Data Flow

See figures 6.6, 6.7 on pages 84, 86 of Pezzè & Young One way to iterate to a fixed point solution.

#### General idea:

- Initially all nodes are on the work list, and have default values
  - Default for "any-path" problem is the empty set, default for "all-path" problem is the set of all possibilities (union of all gen sets)
- While the work list is not empty
  - Pick any node n on work list; remove it from the list
  - Apply the data flow equations for that node to get new values
  - If the new value is changed (from the old value at that node), then
    - Add successors (for forward analysis) or predecessors (for backward analysis) on the work list
- Eventually the work list will be empty (because new computed values = old values for each node) and the algorithm stops.

# Cooking your own: From Execution to Conservative Flow Analysis

- We can use the same data flow algorithms to approximate other dynamic properties
  - Gen set will be "facts that become true here"
  - Kill set will be "facts that are no longer true here"
  - Flow equations will describe propagation
- Example: Taintedness (in web form processing)
  - "Taint": a user-supplied value (e.g., from web form) that has not been validated
  - Gen: we get this value from an untrusted source here



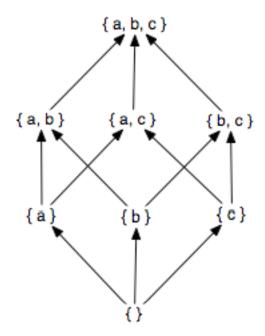
- Kill: we validated to make sure the value is proper

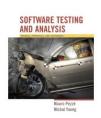
# Cooking your own analysis (2)

- Flow equations must be monotonic
  - Initialize to the bottom element of a lattice of approximations
  - Each new value that changes must move up the lattice
- Typically: Powerset lattice
  - Bottom is empty set, top is universe
  - Or empty at top for allpaths analysis

*Monotonic*: y > x implies  $f(y) \ge f(x)$ 

(where f is application of the flow equations on values from successor or predecessor nodes, and ">" is movement up the lattice)





#### Data flow analysis with arrays and pointers

- Arrays and pointers introduce uncertainty:
   Do different expressions access the same storage?
  - a[i] same as a[k] when i = k
  - a[i] same as b[i] when a = b (aliasing)
- The uncertainty is accommodated depending to the kind of analysis
  - Any-path: gen sets should include all potential aliases and kill set should include only what is definitely modified



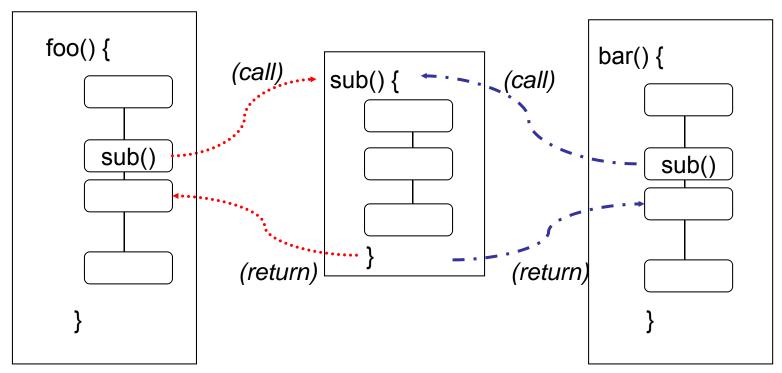
All-path: vice versa

#### Scope of Data Flow Analysis

- Intraprocedural
  - Within a single method or procedure
    - as described so far
- Interprocedural
  - Across several methods (and classes) or procedures
- Cost/Precision trade-offs for interprocedural analysis are critical, and difficult
  - context sensitivity
  - flow-sensitivity



#### **Context Sensitivity**



A **context-sensitive** (interprocedural) analysis distinguishes sub() called from foo() from sub() called from bar();

A **context-insensitive** (interprocedural) analysis does not separate them, as if foo() could call sub() and sub() could then return to bar()



#### Flow Sensitivity

- Reach, Avail, etc. were flow-sensitive, intraprocedural analyses
  - They considered ordering and control flow decisions
  - Within a single procedure or method, this is (fairly)  $cheap O(n^3)$  for n CFG nodes
- Many interprocedural flow analyses are flowinsensitive
  - O(n³) would not be acceptable for all the statements in a program!
    - Though O(n³) on each individual procedure might be ok
  - Often flow-insensitive analysis is good enough ... consider type checking as an example



#### Summary

- Data flow models detect patterns on CFGs:
  - Nodes initiating the pattern
  - Nodes terminating it
  - Nodes that may interrupt it
- Often, but not always, about flow of information (dependence)
- Pros:
  - Can be implemented by efficient iterative algorithms
  - Widely applicable (not just for classic "data flow" properties)
- Limitations:
  - Unable to distinguish feasible from infeasible paths
  - Analyses spanning whole programs (e.g., alias analysis) must trade off precision against computational cost

