

#### An OpenCCG sentence plan **Directed graphs** Hybrid logic: @x restaurant ^ @x <THEME> w ^ @y inexpensive ^ **OpenCCG** input representations @y <THEME> w ^ @z attractive ^ @z <THEME> w ^ are fundamentally directed @w Giovanni's graphs: XML: • nodes - "points" English: • edges - "arrows" connecting <satop nomvar="X"> <prop name="restaurant"/> two points "Giovanni's is an attractive </satop> inexpensive restaurant. <satop nomvar="X"> <diamond mode="theme"> <nomvar name="W"/> If there is an edge from node X to node Y, there is a </diamond> dependency between entities X and Y </satop> • i.e., Y is a dependent of X **Directed graphs - topological Directed graphs - topological** constraints? constraints? OpenCCG directed graphs can be either trees or non-trees. OpenCCG directed graphs can even be nonconnected or cyclic "Re-entrancy" and "multi-rootedness" are permitted



#### Intermediate sentence plans



More realisations than surface, but fewer than deep:

- Giovanni's is an attractive inexpensive restaurant.
- Giovanni's is a restaurant that is cheap and attractive.
- Giovanni's, an attractive restaurant, serves inexpensive food.

## Graphs and logic

Think about first order logic.

#### Formulas:

•  $\exists x \exists y. x \neq y \land boy(x) \land girl(y) \land love(x,y) \land \sim love(y,x)$ 

Every formula describes a set of **models**:

· the set of models in which the formula is true

#### Models are graphs!

boy  $\xrightarrow{\text{LOVE}}$  girl

Node labels are unary predicates (properties). Edge labels are binary predicates (relations).

### Surface realisation with OpenCCG



How can we **represent** labelled directed graphs? i.e., we need a graph description language (a logic)

## Graphs and logic

- Want to encode labelled directed graphs in a linear format
- i.e., convert graph into a logic formula that describes *just that graph*
- But which logical system shall we use to encode labelled directed graphs?
  - first-order logic is way more expressive than we need
  - modal logic is perfectly suited to describe graphs (Kripke structures) - hence used in OpenCCG

# Describing directed graphs - modal propositional logic

The <> modal operator is used to signal a link between two nodes (i.e. a relation/dependency between two entities)



# Describing *labelled* directed graphs - *multimodal* propositional logic

Instead of just one modal operator <>, there is a range of different multimodal operators, e.g., <PRICE>, <DECOR>

 denote different types of relation/dependency between two entities







Also, no way of combining the three fragments into a single formula - conjunction won't do.

### Hybrid multimodal logic - @ operator



## Hybrid multimodal logic - nominals



restaurant ^ <THEME> (w ^ Giovanni's)
inexpensive ^ <THEME> w
attractive ^ <THEME> w

Nominals capture reentrancy, but not multi-rootedness.

#### **Elementary predications**

Every hybrid logic formula can be turned into an equivalent **conjunction** of **elementary predications (EP)** 

Two kinds of EP:

- 1. Node label statements:
- @x restaurant
- node x is labelled "restaurant"
- 2. Edge statements:
- @x < THEME > y
- there is an edge labelled "theme" from node x to node y



#### Elementary predications in XML

#### Node label statements: @x attractive

<satop nomvar="X"> <prop name="attractive"/> </satop>

#### Edge statements: @x <THEME> y

```
<satop nomvar="X">
<diamond mode="theme">
<nomvar name="Y"/>
</diamond>
</satop>
```

#### Learn more about hybrid logic

Patrick Blackburn (2000): "Representation, Reasoning and Relational Structures: a Hybrid Logic Manifesto". Logic Journal of the IGPL, 8(3), 339-365. *URL: http://www.loria.fr/~blackbur/papers/manifesto.pdf* 

Patrick Blackburn (1993): "Modal Logic and Attribute Value Structures". In *Diamonds and Defaults*, edited by M. de Rijke, Kluwer Academic Publishers, 1993, pages 19-65.

URL: http://www.loria.fr/~blackbur/papers/attribute.pdf

#### What you need to know

How to convert a labelled directed graph into a set of elementary predications of hybrid multimodal logic

How to convert a set of elementary predications of hybrid multimodal logic into a labelled directed graph

- Reading for Week 2:
  - Michael White. Efficient Realization of Coordinate Structures in Combinatory Categorial Grammar. *Research on Language and Computation*, 4(1):39–75, 2006.