

Knowledge Engineering Semester 2, 2004-05

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Lecture 17 – Knowledge Evolution I: TMS & EBL
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Where are we?

In the last few lectures ...

- ▶ Knowledge Synthesis
- ▶ Automated Software Synthesis
- ▶ Agents & Multiagent Systems
- ▶ Semantic Web & Knowledge Engineering

In the final two lectures ...

- ▶ Knowledge Evolution
- ▶ Today:
 - ▶ Belief Revision: Truth Maintenance Systems
 - ▶ Knowledge in Learning: Explanation-Based Learning

Knowledge Evolution

- ▶ So far, we discussed knowledge acquisition, representation & reasoning, and synthesis as if we are always building systems from scratch
- ▶ In real-world applications, we expect our KBS to operate over an extended period of time in an environment that changes
 - ▶ How to deal with a changing world *considering our current knowledge?*
- ▶ Knowledge evolution denotes in this sense the evolution of existing knowledge in the light of new information
- ▶ Also an issue for human involvement in the design and implementation of KBS, we will focus on computational aspects
 - ▶ Today: belief revision & learning with prior knowledge

Truth Maintenance Systems (TMS)

- ▶ In section on non-monotonic reasoning, we mentioned that some inferences have only default status until more specific information is known
- ▶ More general problem: **belief revision**, i.e. if we add $\neg P$ to a KB that contains P , how do we make sure all inferences drawn from P are retracted?
 - ▶ If $P \Rightarrow Q$, we have to retract Q as well ...
 - ▶ but what if also $R \Rightarrow Q$?
- ▶ **Truth maintenance systems (TMS)** deal with this problem
- ▶ Naive approach:
 - ▶ Number all facts P_1 to P_n in the order in which they were added to the KB
 - ▶ If P_i is removed, go back to state before addition of P_i and add P_{i+1} to P_n (and what was inferred from them) again
 - ▶ Simple, but impractical!

Justification-Based TMS (JTMS)

- ▶ Based on idea of annotating each fact with its “justification” (set of logical sentences from which it was inferred)
- ▶ Example: A forward-chaining KBS that adds sentences it can infer from existing ones automatically
 - ▶ Using JTMS, it will add Q to the KB because of P and $P \Rightarrow Q$ and annotate it with $\{P, P \Rightarrow Q\}$
- ▶ A sentence can have several justifications
- ▶ If P is to be retracted from the KB, all sentences that require P in every justification have to be removed, too
- ▶ In the above example: Consider the following justification sets for Q
 - ▶ $\{\{P, P \Rightarrow Q\}, \{P, R \vee P \Rightarrow Q\}\} \Rightarrow Q$ will have to be removed
 - ▶ $\{\{P, P \Rightarrow Q\}, \{R, R \vee P \Rightarrow Q\}\} \Rightarrow Q$ can be retained

Example

- ▶ Consider exam schedule with exam e taking place in time-slot t denoted by $Time(e) = t$
 - ▶ Concrete schedule: a conjunction
 $Time(KM) = 6 \wedge Time(KE) = 2 \wedge \dots \wedge Time(PMR) = 12$
 - ▶ $Takes(s, e)$ denotes that a student s has to take exam e
- ▶ Rule for exam clashes:

$$\exists s Takes(s, e) \wedge Takes(s, f) \wedge Time(e) = Time(f) \Rightarrow Clash(e, f)$$
- ▶ Consider $Clash(KE, KM)$ with the following justification
 $\{Takes(Moe, KM), Takes(Moe, KE), Time(KM) = 2, Time(KE) = 2, Takes(Moe, KE) \wedge Takes(Moe, KM) \wedge Time(KE) = Time(KM) \Rightarrow Clash(KM, KE)\}$
- ▶ Easy to check alternative schedules, e.g. by retracting $Time(KE) = 2$ and asserting $Time(KE) = 5$ (other clashes become immediately visible)

Justification-Based TMS (JTMS)

- ▶ Obvious advantage: when retracting P , only those sentences derived from P have to be considered (not all those inferred since P had been added)
- ▶ JTMS mark sentences as **in** or **out** (rather than deleting them completely)
 - ▶ All inference chains are retained, useful if some facts might become true again
 - ▶ Of course, in practice sentences will be eventually deleted if never used again
- ▶ Additional advantage (apart from efficient retraction): speed up of analysis of multiple hypothetical situations

Assumption-Based TMS (ATMS)

- ▶ In a JTMS, only one state of the world is represented at a time
- ▶ Idea of ATMS: label each sentence with a set of **assumption sets** that would make it true \Rightarrow sentence holds if all assumptions in one of the assumption sets hold
- ▶ Way of providing explanations, which may also include assumptions (including contradictory ones)
- ▶ Idea: tag sentence “false” with all sets of contradictory assumptions
- ▶ ATMS does not strive to reach a state of mutually consistent assumptions, all possibilities are kept in parallel (no backtracking necessary)

Example

- ▶ Suppose we have assumptions a_1 to a_5 and sentences A and B with the following assumption sets:
 - ▶ A : $\{\{a_1, a_2\}, \{a_2, a_5\}\}$
 - ▶ B : $\{\{a_1\}, \{a_2, a_3\}, \{a_4\}\}$
- ▶ “false: $\{\{a_4, a_5\}\}$ ” indicates that a_4 and a_5 contradict each other
- ▶ Assume we are adding new sentence $A \wedge B \Rightarrow C$, what is the correct set of assumptions?

Knowledge in Learning – EBL

- ▶ In our account of inductive learning (decision trees, version spaces) we didn't make use of prior knowledge
- ▶ Basic advantage of using prior knowledge: narrowing down the hypothesis space
 - ▶ Entailment constraint of pure inductive learning:

$$\text{Hypothesis} \wedge \text{Descriptions} \models \text{Classification}$$
 - ▶ Entailment constraint with background knowledge in **explanation-based learning (EBL)**:

$$\text{Hypothesis} \wedge \text{Descriptions} \models \text{Classification}$$

$$\text{Background} \models \text{Hypothesis}$$
- ▶ Agent could have derived hypothesis from background knowledge (instance does not add anything factually new)
- ▶ However, EBL is a useful method to derive special-purpose knowledge from first-principle theories

Example

1. Create cross-product (all pairwise combinations) of assumption sets of A and B :

$$\{\{a_1, a_2\}, \{a_1, a_2, a_3\}, \{a_1, a_2, a_4\}, \{a_1, a_2, a_5\}, \{a_2, a_3, a_5\}, \{a_2, a_4, a_5\}\}$$
2. Remove those that contain superfluous assumptions:

$$\{\{a_1, a_2\}, \{a_2, a_3, a_5\}\}$$
3. If a label exists for C already, take union of the two labels and delete redundant assumptions (no contradiction testing necessary)
4. If label for C changed, propagate changes to those sentences whose labels depend on C
5. If all labels of C contain contradictions, add these to the label of “false” (and delete those members or supersets thereof from all other nodes)

Explanation-Based Learning

- ▶ Intuition: Explaining why something is a good idea is much easier than coming up with the idea in the first place
- ▶ Two-step process:
 1. Construct an explanation of the observation using prior knowledge
 2. Establish a definition of the class of cases for which explanation can be used
- ▶ Crucial step: to identify the necessary condition for the steps used in explanation to apply to another case

Example

- Suppose we want to simplify the arithmetic expression $1 \times (0 + X)$
- The following set of rules is given for a backward-chaining reasoner:

$Rewrite(u, v) \wedge Simplify(v, w) \Rightarrow Simplify(u, w)$

$Primitive(u) \Rightarrow Simplify(u, u)$

$ArithmeticUnknown(u) \Rightarrow Primitive(u)$

$Number(u) \Rightarrow Primitive(u)$

$Rewrite(1 \times u, u) \quad Rewrite(0 + u, u)$

- Construct two proof trees in parallel, one with all constants replaced by variables

Example

- Collect leaf nodes from generalised proof tree to construct a rule for the goal predicate:

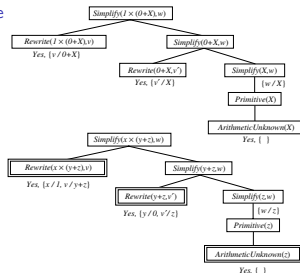
$Rewrite(1 \times (0 + z), 0 + z) \wedge Rewrite(0 + z, z) \wedge ArithmeticUnknown(z) \Rightarrow Simplify(1 \times (0 + z), z)$

- First two conditions don't depend on value of z , this yields simpler rule

$ArithmeticUnknown(z) \Rightarrow Simplify(1 \times (0 + z), z)$

- More generally, all conditions can be dropped that don't impose rules on values of variables on the RHS of the rule

Example



EBL – Procedure

- Construct a proof that the goal predicate applies to the example using available background knowledge.
- In parallel, construct a generalised proof tree for variabilised goal using the same inference steps as in 1.
- Construct a new rule whose LHS consists of the leaves of the proof tree and whose RHS is the variabilised goal (while applying appropriate bindings).
- Drop any conditions that are true regardless of the values of the variables in the goal.

Critique

- ▶ As mentioned, nothing actually “new” is learned using the new example, the knowledge is merely “re-formulated”
- ▶ Trade-off between generality and specificity of rules:
 - ▶ The more general, the more applicable will it be to new cases
 - ▶ The more specific, the easier it is to apply (and the less often will it be tried out in vain)
- ▶ In practice, EBL is about optimising the choice of appropriate rules with experience (keep different ones and decide empirically which have proven most useful)

Summary

- ▶ Discussed some methods that can be used for automating knowledge evolution
- ▶ Reasoning maintenance systems: revising beliefs efficiently
- ▶ Knowledge in learning: using explanations to reduce hypothesis space
- ▶ Explanation learning: deriving special-purpose knowledge from general principles
- ▶ **Next time: More “knowledge in learning”** (case-based reasoning and/or inductive Logic Programming)