

# IVR: Visual Servoing

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**informatics**

- Model-based control
- Visual servoing task
- What is a Jacobian?
- Visual servoing task
- Implications for robot control

PROBLEM: Guiding a robot to a target based on images

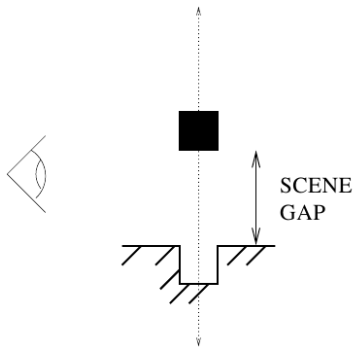
APPLICATIONS:

- Assembly robotics: Component insertion
- Mobile robotics: Docking

⇒ VISUAL SERVOING THEORY

# QUESTION

If only vertical robot motion possible (and sufficient) to reduce the gap:



How to get peg exactly into hole?

# APPROACH 1: MODEL DRIVEN

KNOWN:

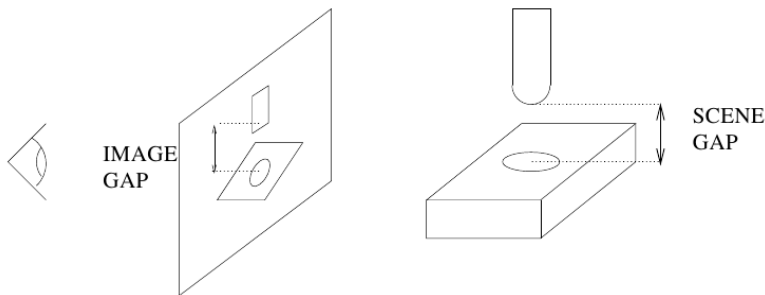
- Robot manipulation model
- Part & robot position known
- Target model
- Camera calibrated

BUT: errors exist and combine - noise, unknowns, gear backlash

SO: need very accurate calibration & mechanisms

# TRY 2: VISUAL SERVOING

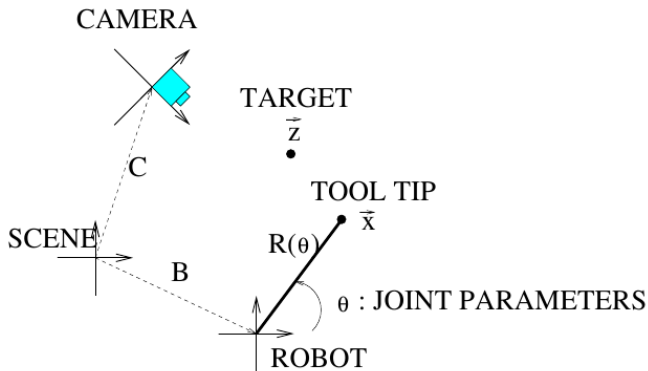
Move so that observed positions directly link to task distances



- Incrementally move to reduce image gap
- Don't know exact positions

# MORE FORMAL MODEL

CONSIDER:



# VARIOUS QUANTITIES

$B$  - ROBOT POSITION WRT SCENE

$C$  - CAMERA POSITION WRT SCENE

$P$  - CAMERA PROJECTION MODEL

$\vec{\theta}$  - ROBOT JOINT PARAMETERS

$R(\vec{\theta})$  - TOOL POSITION WRT ROBOT



# LINKING EQUATION

IF:

- $\vec{x}$  - TOOL TIP WRT TOOL
- $\vec{z}$  - TARGET WRT SCENE
- $\vec{a}$  - IMAGE OF TOOL TIP
- $\vec{b}$  - IMAGE OF TARGET

THEN (as a concatenation of appropriate transformations):

- $\vec{a} = PC^{-1}BR(\theta)\vec{x}$
- $\vec{b} = PC^{-1}\vec{z}$

# APPROACH 1: MODEL DRIVEN

Calibrate  $P, C, B, R(\vec{\theta})$  accurately

SOLVE:  $\vec{\theta} = \vec{f}(\vec{z}, \vec{x}, P, C, B)$

Hard analytics

Not always solvable

# APPROACH 2: VISUAL SERVOING

How much to move joints ( $\Delta\vec{\theta}$ ) to reduce target error  
 $\vec{\Delta} = \vec{a} - \vec{b}$  ?

Visually estimate  $\vec{f}(\dots)$  such that  $\Delta\vec{\theta} \doteq \vec{f}(\vec{\Delta})$

Use  $\Delta\vec{\theta}$  to partially approach target and recompute  $\vec{\theta}$

Iterate

# ESTIMATING $\vec{f}()$

Move robot joint  $i$  slightly from  $\theta_i$  to  $\theta_i + \varepsilon$

Observe tool tip moves slightly from  $\vec{a}$  to  $\vec{a} + \vec{\delta}_i$

Compute:

$$\frac{\partial \vec{a}}{\partial \theta_i} \doteq \frac{(\vec{a} + \vec{\delta}_i) - \vec{a}}{(\theta_i + \varepsilon) - \theta_i} = \frac{\vec{\delta}_i}{\varepsilon}$$

Repeat for all  $i$  to estimate JACOBIAN matrix

$$J = \frac{1}{\varepsilon} [\vec{\delta}_1, \dots, \vec{\delta}_N]$$

for  $N$  joints.

# USING THE JACOBIAN

Linear theory:

$$\vec{\Delta} \doteq J\Delta\vec{\theta}$$

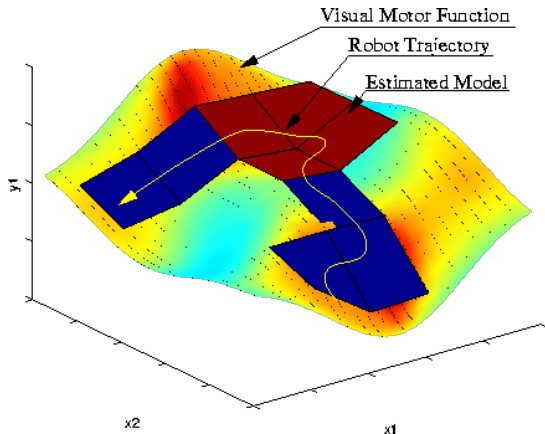
$J$  is  $2 \times N$ , so use pseudo-inverse

$$\Delta\vec{\theta} = (J^T J)^{-1} J^T \vec{\Delta}$$

But  $J$  is only approximate and not true inverse?

So, move  $\alpha\Delta\vec{\theta}$  and iterate ( $\alpha < 1$ )

# SERVOING ALGORITHM



see Perceptual Actions: Vision Based Uncalibrated Robot Control by Martin Jägersand

# SERVOING ALGORITHM

DO

    Compute  $\vec{\Delta}$

    Estimate  $J$

    Compute  $\Delta\vec{\theta}$

    Move joints  $\alpha\Delta\vec{\theta}$  where  $0 < \alpha < 1$

WHILE  $\|\vec{\Delta}\| > \tau$  pixels

$\tau > 1$ ? Maybe robot is 'shakey'

# CONVERGENCE?

If  $\alpha$  small enough, should always be reducing  $\Delta$

As  $J$  is linear, moving  $\alpha\Delta\vec{\theta}$  should reduce position error by approximately  $\alpha\vec{\Delta}$



# CONVERGENCE

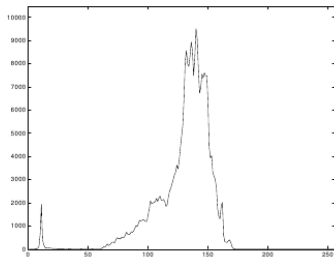
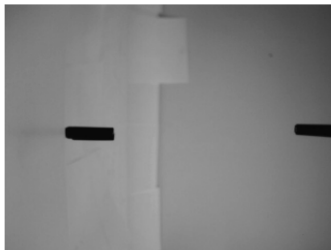
STEP	MOVEMENT	REMAINDER
1	$\alpha \ \vec{\Delta}\ $	$(1 - \alpha) \ \vec{\Delta}\ $
2	$(1 - \alpha) \alpha \ \vec{\Delta}\ $	$(1 - \alpha)^2 \ \vec{\Delta}\ $
	$\dots$	
n	$(1 - \alpha)^{n-1} \alpha \ \vec{\Delta}\ $	$(1 - \alpha)^n \ \vec{\Delta}\ $

Total movement:

$$\sum_{n=1}^{\infty} (1 - \alpha)^{n-1} \alpha \|\vec{\Delta}\| = \frac{1}{1 - (1 - \alpha)} \alpha \|\vec{\Delta}\| = \|\vec{\Delta}\|$$

# VISUAL SERVOING RESULTS 1

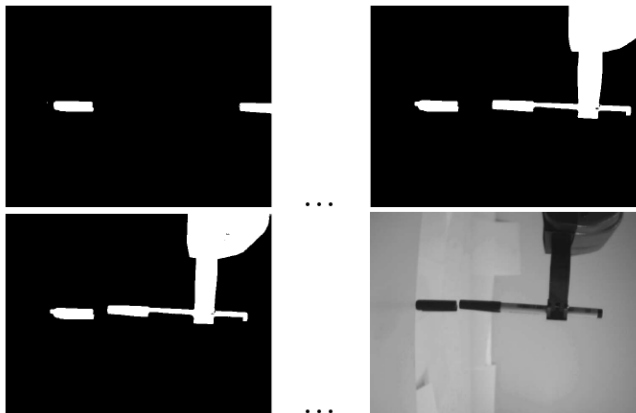
Initial position and histogram (#pixels per gray level)



Camera on side

# VISUAL SERVOING RESULTS 2

Note: changing binary images



5 iterations

- Usually more cameras (image-based visual servoing)
- If the pose of the robot can be estimated based on a robot model a single camera may be sufficient (position-based visual servoing)
- Precision is improved by combination with force feedback
- Camera movements and other sources of errors
- Related problem: Camera positioning; track following in autonomous robots

# Summary on visual servoing

- Servoing versus model based control
- Basics of visual servoing
- Linear approximations are usually safe if small steps are taken
- What about efficiency, dynamics, inertia, friction?  
⇒ control theory

Java-based Visual Servo Simulator:

<http://www.robot.uji.es/research/projects/javiss>

Further reading:

S. Hutchinson, G. D. Hager, P. I. Corke (1996) A tutorial on visual servo control. *IEEE Transactions on Robotics and Automation* **12**:5, 651-670.