

Haskell Refresher

Informatics 2D

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Haskell

- Purely functional! : “Everything is a function”
- Main topics:
 - Recursion
 - Currying
 - Higher-order functions
 - List processing functions such as map, filter, foldl, sortBy, etc
 - The Maybe monad
- More on Haskell: <http://www.haskell.org/haskellwiki/Haskell>

Types

- Unlike other programming languages like Java, Haskell has type inference.
- However, type declarations ensures that you are specific about the input arguments of your function and the output values.
- Example:

`next :: Trace -> [Trace]`

- The **next** function takes an argument of type **Trace** and returns a list of *Traces*

Type Synonyms

```
type Trace = [(Int,Int)]
```

```
type Game = [Int]
```

- The type Trace is a synonym for a list of (Int, Int) tuples.
- For code clarity.

Recursion

- Important role in Haskell.
- Function is recursive when one part of its definition includes the function itself again.
- Always have a termination condition to avoid infinite loop.

```
length :: [a] -> Int
```

```
length [] = 0
```

```
length (x:xs) = 1 + length xs
```

Currying

- The process of creating intermediate functions when feeding arguments into a complex function.
- Note: all functions in Haskell really only take one argument
- Example:
 - 2 * 3 in Haskell:
 - (*) function takes first argument 2, and return an intermediate function (2*)
 - The new function (2*) takes one argument,3, and completes the multiplication
- Applying only one parameter to a function that takes two parameters returns a function that takes one parameter

Higher-Order Functions

- Functions are just like any other value in Haskell.
- Functions can take functions as parameters and also return functions.

```
map :: (a -> b) -> [a] -> [b]
```

```
map _ [] = []
```

```
map f ( x: xs ) = f x : map f xs
```

- Map takes a function and list and applies that function to every element in the list.

List Processing Functions

(map, filter, foldl, etc.)

- **map** : takes a function and list and applies that function to every element in the list.

$$\text{map} :: (a \rightarrow b) \rightarrow [a] \rightarrow [b]$$

- **filter**: takes a predicate (function that returns true or false) and list and then returns the list of all elements that satisfy the predicate.

$$\text{filter} :: (a \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [a]$$

- **foldl**: takes a binary function, an accumulator and a list. It ‘folds’ up the items in the list and return a single value.

$$\text{foldl} :: (a \rightarrow b \rightarrow a) \rightarrow a \rightarrow [b] \rightarrow a$$

List Comprehension

- Build more specific sets out of general sets.
- Example: to create a list of integers that are multiples of 2 and greater than than 20:

```
[x*2 | x <- [1..25] , x*2 >= 20]
```

Output
function



The diagram consists of three labels at the bottom, each with an arrow pointing upwards to a specific part of the list comprehension syntax above. The first label, 'Output function', has an arrow pointing to the 'x*2' part of the expression. The second label, 'Elements bound to x', has an arrow pointing to the 'x <- [1..25]' part. The third label, 'Condition Or Predicate', has an arrow pointing to the ', x*2 >= 20' part.

Elements
bound to x

Condition Or
Predicate

Maybe Monad

- The Maybe monad represents computations which might "go wrong" by not returning a value.
- If a value is returned, it uses **Just a**, where a is the type of the value.
- If no value is available, it returns **Nothing**.
- **Example:**

```
safeDiv :: Double -> Double -> Maybe Double
```

```
safeDiv x y
```

```
  | y == 0    = Nothing
```

```
  | otherwise = Just (x/y)
```

Coursework Overview

- **Trace** type for search problems

type Trace = [(Int,Int)]

- Example :
- A path from (1,1) to (4,2)

[(1,1), (1,2), (2,2), (3,2), (4,2)]

	1	2	3	4	5	6	7	8	9	10
1	x	x								
2		x								
3		x								
4		x								
5										
6										
7										
8										
9										
10										

Successor Function

- The next function returns the possible continuations of the path

next :: Trace -> [Trace]

- Example :
- Suppose we start from are at (4,2)
- Possible continuations generated by **next**
[[(1,1), (1,2), (2,2), (3,2), (4,2), (4,1)],
 [(1,1), (1,2), (2,2), (3,2), (4,2), (3,2)],
 [(1,1), (1,2), (2,2), (3,2), (4,2), (4,3)],
 [(1,1), (1,2), (2,2), (3,2), (4,2), (5,2)]]

	1	2	3	4	5	6	7	8	9	10
1										
2										
3										
4										
5										
6										
7										
8										
9										
10										

Consistency with representation

- Be consistent with your representation of Traces in Haskell

`[(1,1), (1,2), (2,2), (3,2), (4,2)]`

`[(4,2), (3,2), (2,2), (1,2), (1,1)]`

- Both are ok, provided you are consistent with the head and tail of your list.
- Same applies to `[Trace]`

Higher-Order Functions in Coursework

Example:

```
bestFirstSearch :: (Trace -> Bool) -> (Trace -> [Trace]) ->
((Int, Int) -> Int) -> [Trace] -> Maybe Trace
```

- **(Trace → Bool)** is the type of the goal function (same as uninformed search).
- **(Trace → [Trace])** is the type of the next function (same as uninformed search).
- **((Int, Int) → Int)** is the type of the heuristic function, which defines at least an ordering on the nodes in the search agenda.
- **[Trace]** is the search agenda (same as uninformed search).
- **Maybe Trace** is the value the function returns (same as uninformed search).

Game (Tic-Tac-Toe) Representation

- Game represented as a list of Integers
type Game = [Int]
- A new game will be represented as
- [-1,-1,-1,-1,-1,-1,-1,-1,-1]
- Max player is represented by a **1** in the list.
- Min player is represented as **0** in the list.
- An unplayed cell is represented as **-1**

X	O	X
O	X	O
O	O	X

- Types for Cell and Player
type Player = Int
type Cell = (Int,Int)

Game Representation Examples

• New Game: $[-1, -1, -1, -1, -1, -1, -1, -1, -1]$

• Min Move: $[-1, -1, -1, -1, 0, -1, -1, -1, -1]$

	O	

• Max Move: $[1, -1, -1, -1, 0, -1, -1, -1, -1]$

X		
	O	

Lines in Game

- The Line type represents any of the lines on the game board: rows, columns and diagonals.

type Line = [Int]

- Examples of Lines for the game state given:

• Row 1: [1, 0, 1] Row 3: [0, 0, 1]

• Column 1: [1, 0, 0] Diagonal 1: [1, 1, 1]

X	O	X
O	X	O
O	O	X

- To get all lines for a game state, use function:

getLines :: Game -> [Line]

Other useful functions

- maxPlayer function checks if the given player is max, and returns a Boolean.

maxPlayer :: Player -> Bool

- switch function alternates between players.

switch :: Player -> Player

- terminal function checks if the game argument is in a terminal state.

terminal :: Game -> Bool

- isMoveValid checks if a move made in a given game state is a valid one for a given player.

isMoveValid :: Game -> Player -> Cell -> Bool

- playMove makes a move to a cell and returns the new game state. This function is called for human player moves.

playMove :: Game -> Player -> Cell -> Game

- moves function returns a list of possible moves/successor states that a player can make given a game state.

moves :: Game -> Player -> [Game]

- checkWin function checks if the game state is a win for the player argument.

checkWin :: Game -> Player -> Bool