

Search Strategies

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Outline

- Uninformed search strategies use only information in problem definition
- · Breadth-first search
- · Depth-first search
- Depth-limited and Iterative deepening search

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Search strategies

- A search strategy is defined by picking the order of node expansion nodes are taken from the *frontier*
- · Strategies are evaluated along the following dimensions:
 - completeness: does it always find a solution if one exists?
 - time complexity: number of nodes generated
 - space complexity: maximum number of nodes in memory
 - optimality: does it always find a least-cost solution?
- · Time and space complexity are measured in terms of
 - b: maximum branching factor of the search tree
 - d: depth of the least-cost solution
 - m: maximum depth of the state space (may be ∞)

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function TREE-SEARCH(*problem*) returns a solution, or failure initialize the frontier using the initial state of *problem* loop do

if the frontier is empty then return failure

- choose a leaf node and remove it from the frontier
- if the node contains a goal state **then return** the corresponding solution expand the chosen node, adding the resulting nodes to the frontier



Repeated states

Failure to detect repeated states can turn a linear problem into an exponential one!



- Expand shallowest unexpanded node
- Implementation:
- frontier is a FIFO queue, i.e., new successors go at end

Breadth-first search



Graph search

function GRAPH-SEARCH(problem) returns a solution, or failure
initialize the frontier using the initial state of problem
initialize the explored set to be empty
loop do
if the frontier is empty then return failure
choose a leaf node and remove it from the frontier
if the node contains a goal state then return the corresponding solution
add the node to the explored set
expand the chosen node, adding the resulting nodes to the frontier
only if not in the frontier or explored set

Augment TREE-SEARCH with a new data-structure:

the explored set (closed list), which remembers every expanded node
newly expanded nodes already in explored set are discarded

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Breadth-first search

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Breadth-first search



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Breadth-first search algorithm

function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure node ← a node with STATE = problem.INITIAL-STATE, PATH-COST = 0 if problem.GOAL-TEST(node.STATE) then return SOLUTION(node) frontier ← a FIFO queue with node as the only element explored ← an empty set loop do if EMPTY?(frontier) then return failure node ← POP(frontier) /* chooses the shallowest node in frontier */ add node.STATE to explored for each action in problem.ACTIONS(node.STATE) do child ← CHILD-NODE(problem, node, action) if child.STATE is not in explored or frontier then if problem.GOAL-TEST(child.STATE) then return SOLUTION(child) frontier ← INSERT(child, frontier)

Breadth-first search



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Properties of breadth-first search

- Complete? Yes (if b is finite)
- Time? $b+b^2+b^3+...+b^d = O(b^d)$ (worst-case)
- Space? O(b^d) (keeps every node in memory)
- Optimal? Yes (if cost = 1 per step)

Space is the bigger problem (more than time)

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Depth-first search



- Implementation:
 - frontier = LIFO queue, i.e., put successors at front





Depth-first search

- Expand deepest unexpanded node
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Properties of depth-first search

- Complete? No: fails in infinite-depth spaces, spaces with loops
 - Modify to avoid repeated states along path
 - · complete in finite spaces
- Time? O(b^m): terrible if m is much larger than d
 - but if solutions are dense, may be much faster than breadth-first

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- Space? O(bm), i.e., linear space!
- Optimal? No



• Compare breadth-first and depth-first search.

Mid-Lecture Exercise

- When would breadth-first be preferable?
- When would depth-first be preferable?

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Solution

- Breadth-First:
 - When completeness is important.
 - When optimal solutions are important.
- Depth-First:
 - When solutions are dense and low-cost is important, especially space costs.



This is depth-first search with depth limit *l*, i.e., nodes at depth *l* have no successors

Recursive implementation:







• Number of nodes generated in an iterative deepening search to depth *d* with branching factor *b*:

 $N_{IDS} = (d)b + (d-1)b^2 + ... + (2)b^{d-1} + (1)b^d$

- Some cost associated with generating upper levels multiple times
- Example: For *b* = 10, *d* = 5,
 - N_{BFS} = 10 + 100 + 3,000 + 10,000 + 100,000 = 111,110
 - N_{IDS} = 50 + 400 + 3,000 + 20,000 + 100,000 = 123,450
- Overhead = (123,450 111,110)/111,110 = 11%

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Summary of algorithms

Criterion	Breadth-	Uniform-	Depth-	Depth-	lterative
	First	Cost	First	Limited	Deepening
Complete? Time	Yes $O(b^d$)	$\operatorname{Yes}_{O(b^{\lceil C^*/\epsilon\rceil})}$	$No O(b^m)$	$No O(b^l)$	Yes $O(b^d)$
Space	$O(b^d$)	$O(b^{\lceil C^*/\epsilon \rceil})$	O(bm)	O(bl)	O(bd)
Optimal?	Yes	Yes	No	No	Yes

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Properties of iterative deepening search

- Complete? Yes
- Time? $(d)b + (d-1)b^2 + ... + (1)b^d = O(b^d)$
- Space? O(bd)
- Optimal? Yes, if step cost = 1

Summary



- Variety of uninformed search strategies: – breadth-first, depth-first, iterative deepening
- Iterative deepening search uses only linear space and not much more time than other uninformed algorithms

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