

Introduction to Matlab

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1 Introduction

MATLAB is a programming language that grew out of the need to process matrices. It is used extensively in science and engineering. It now has many features and toolboxes to support numerical programming (including machine learning) and visualization. Here you will meet only a fraction of MATLAB features. **Important:** Data analysis, programming, and mathematics are not spectator sports! You can only learn to munge data by doing it. Unless you spend a reasonable amount of time per lecture (around 2hrs) reproducing the material for yourself, you won't really understand it.

1.1 Getting started

Open the terminal and type:

```
s1263191@chatton: matlab
```

This will bring up the main working window of MATLAB which includes the following elements:

- **Current Folder** - Access your files.
- **Command Window** - Enter commands at the command line, indicated by the prompt (>>).
- **Workspace** - Explore data that you create or import from files.

You can type MATLAB expressions to the >> prompt, eg:

```
>> 57*64.3           % multiply two numbers
ans =
    3.6651e+03
>> power(10, pi/2)  % call a function
ans =
    37.2217
```

The second of these makes use of a built-in function, `power`, and a predefined constant `pi`. If you want to see what a MATLAB function does you can go to the help window and find it using the index, the contents, or by searching. (You can also type `>> help power` at the command line.) The MATLAB help system is very good, and worth exploring.

MATLAB handles complex numbers (using the symbol `j`) so it is possible to do things such as:

```
>> exp(j*pi)        % using complex numbers
ans =
   -1.0000 + 0.0000i
```

We can set up some variables in MATLAB and perform some computations:

```
>> x = 3.4;      % defining x and initializing it with a value
>> y = 5.7;
>> z = x*y;
>> z
z =
    19.3800
>> a = 2; b = 7; % multiple assignments on the same line
```

Variables `x`, `y` and `z` persist in the MATLAB workspace until they are changed. Note that a semicolon (`;`) at the end of a line prevents the result of an expression being printed to the screen, useful when dealing with big vectors and matrices.

If you forgot the variables you can type `who` at the command line. The `who` command displays all the variable names you have used.

2 Vectors

In MATLAB 1D arrays don't really exist. A vector is actually a 2D array or matrix. MATLAB allows creating two types of vectors: 1) row vectors and 2) column vectors.

A **row** vector is defined by placing a sequence of numbers within square braces:

```
v = [5, 1, 8, 5, 4]; % The commas are optional
v = [5 1 8 5 4];    % Same as above

>> v                % v is a row vector, 1x5
v =
     5     1     8     5     4
```

To create a **column** vector you could use the transpose operator `'`:

```
>> v'
ans =
     5
     1
     8
     5
     4
```

or you can explicitly create a column vector by using semicolon(`;`) to delimit the elements:

```
>> v = [5; 1; 8; 5; 4]; % semicolon(;) signifies where rows break
```

We can get the size of the vector by typing:

```
>> size(v)          % size of column vector
ans =
     5     1
>> size(v')        % size of row vector
ans =
     1     5
```

Useful vector operations include:

Vector sum $v+w$

Vector difference $v-w$

Multiplication by a scalar $10*v$

Scalar dot (inner) product $\text{dot}(v, w)$

Vector cross product $\text{cross}(v, w)$

Vector magnitude (norm) $\text{norm}(v)$

Vector **sum** example:

```
>> v = [5 1 8 5 4];
>> w = [2 3 4 5 6];
>> v+w      % add two vectors
ans =
     7     4    12    10    10
```

Some operations on vectors work on the elements one-by-one, returning the answer as a vector of the same dimension:

```
>> sqrt([1 2 3 4]) % take the square root of vector elements
ans =
     1.0000     1.4142     1.7321     2.0000
```

The colon (':') operator generates equally-spaced points between its first and last inputs:

```
>> 1:4      % gap is 1 (default)
ans =
     1     2     3     4
>> 1:0.5:2  % gap is 0.5
ans =
     1.0000     1.5000     2.0000
>> 4:-1:1   % gap is -1
ans =
     4     3     2     1
```

When there are three arguments, the second one specifies the gap between the outputs (defaults to 1 when there are only two arguments).

If we want to look only at the first three elements of a vector:

```
>> v(1:3)   % take the first 3 element of 'v'
ans =
     5     1     8
```

2.1 Exercise

Create a vector `vec`, e.g. `vec = [1 5 6 2 3 9]`.

Then evaluate `vec+vec`, `vec/2`, `vec+3`, `vec.*vec`, `vec.^2` etc. Some operators (`+`, `-`) and most functions (`exp`, `log`, `sin`, etc.) work element-wise on all the numbers in the array. `*` and `/` work elementwise with scalars, but for matrices do matrix multiplication (and division). For elementwise versions of multiplication, division, and raising to the power, use `.*`, `./` and `.^` (**note the dots are important**).

3 Matrices

MATLAB really comes into its own when you want to do computations with matrices, such as for machine learning and pattern recognition. Most variables in Matlab are matrices of double floating point numbers. If you write `x=1` you will get a 1x1 matrix of doubles containing a 1.0.

Defining a matrix is similar to defining a vector. To define a matrix, you can treat it like a column of row vectors (note that the spaces are required!):

```
>> m = [1 2 3; 4 5 6; 7 8 9] % create 3x3 matrix
m =
     1     2     3
     4     5     6
     7     8     9

>> size(m) % get the size of the matrix which is 3x3
ans =
     3     3
```

Semi-colon (`;`) is used to separate rows.

Here is another matrix:

```
>> n = [1 0 0; 0 1 0; 0 0 1] % this is the identity matrix I
n =
     1     0     0
     0     1     0
     0     0     1
```

And we can do the usual matrix operations of add and multiply:

```
>> m+n % matrix addition
ans =
     2     2     3
     4     6     6
     7     8    10

>> m*n % matrix multiplication
ans =
     1     2     3
     4     5     6
     7     8     9
```

Note that n is the 3x3 identity matrix. An easier way to generate an identity matrix is to use the MATLAB command `eye`:

```
>> eye(3) % matlab function to create identity matrices
ans =
     1     0     0
     0     1     0
     0     0     1
```

MATLAB overloads its operators (when it is not ambiguous). For example, **add 1** to each matrix element:

```
>> m+1 % add 1 to each element of the matrix
ans =
     2     3     4
     5     6     7
     8     9    10
```

MATLAB can distinguish between matrix operations and element-by-element operations. The **dot** syntax is used for element-by-element operations. For example, the following multiplies corresponding elements of two matrices:

```
>> m.*n % multiply element-wise
ans =
     1     0     0
     0     5     0
     0     0     9
```

You should be careful when doing matrix operations, since your matrices need to have the right size!

```
>> m*[1 2; 3 4] % m is 3x3 matrix and is multiplied with a 2x2
matrix
Error using *
Inner matrix dimensions must agree.
```

Other useful functions include `zeros(i,j)` which generates an $i \times j$ zero matrix, and `ones` to generate a matrix of ones. The `size` command returns the dimensions of a matrix:

```
>> zeros(3,2) % create a 3x2matrix of 0s
ans =
     0     0
     0     0
     0     0
>> o = ones(2,3) % create a 2x3 matrix of 1s
o =
     1     1     1
     1     1     1
>> [rw, cl] = size(o) % return the matrix size
rw =
     2
cl =
     3
```

And of course it is possible to combine functions:

```
>> [rw, cl] = size(ones(2,3)) % get the size of a 2x3 matrix
rw =
     2
cl =
     3
```

To access the i, j th element of a matrix m , use $m(i, j)$.

```
>> m(2,3)
ans =
     6
```

The colon operator `:` can be used to select a submatrix. For example to select a submatrix containing rows 2 and 3 and columns 1 and 2 of m :

```
>> m(2:3,1:2)
ans =
     4     5
     7     8
```

A colon on its own selects all rows (or columns):

```
>> m(1,:)
ans =
     1     2     3
>> m(:, :)
ans =
     1     2     3
     4     5     6
     7     8     9
```

Finally, a colon on its own turns a matrix into a 1D column vector, working column by column:

```
>> m(:)
ans =
     1
     4
     7
     2
     5
     8
     3
     6
     9
```

Relation operators such as `<` and `>` work with matrices too, e.g.:

```
>> m > 5 % which elements are bigger than 5 (returns boolean)
ans =
     0     0     0
     0     0     1
     1     1     1
```

These are not elements of m , but **boolean** values (MATLAB calls them logical indices) which indicate the positions where the test is true. To access the actual elements that are greater than 5:

```
>> m.*(m > 5)
ans =
     0     0     0
     0     0     6
     7     8     9
```

We can also use these logical indices to extract just those values that obey the condition:

```
>> m(m > 5)
ans =
     7
     8
     6
     9
```

Note that the result is a vector containing only those values that obey the condition. See also the function `find` (look at the help pages, i.e. type `help find`).

3.1 Other matrix operations

Once you are able to create and manipulate a matrix, you can perform many standard operations on it. MATLAB has all the matrix operations you might expect. However, you should be careful, since the operations are numerical manipulations done on digital computers!

Given a matrix a :

```
>> a = [ 1 4 2 ; 4 2 -1 ; 2 -1 3] % 3x3 matrix
a =
     1     4     2
     4     2    -1
     2    -1     3
```

we can take its transpose a' , compute the matrix norm `norm(a)`, the determinant `det(a)` and the matrix inverse `inv(a)`:

```
>> a' % matrix transpose
ans =
     1     4     2
     4     2    -1
     2    -1     3

>> inv(a) % matrix inverse
ans =
 -0.0746    0.2090    0.1194
  0.2090    0.0149   -0.1343
  0.1194   -0.1343    0.2090

>> det(a) % matrix determinant
ans =
 -67
```

```
>> norm(a) % matrix L2-norm
ans =
    5.6866
```

There are also routines that let you find solutions to linear equations. For example, if $\mathbf{Ax} = \mathbf{b}$ and you want to find \mathbf{x} , a slow way to find \mathbf{x} is to simply invert \mathbf{A} and perform a left multiply on both sides. However, this approach is not efficient and unstable (another approach is to perform the L/U decomposition with pivoting, for example). Matlab has special commands that will do this for you using the `\` operator:

```
>> b = [1 ; 2; 3] % vector containing the right sides of the linear
      equation
b =
     1
     2
     3
>> x = a\b % denotes the solution to the matrix equation Ax = b
x =
    0.7015
   -0.1642
    0.4776
>> a*x % confirm that Ax = b
ans =
    1.0000
    2.0000
    3.0000
```

Some other very useful commands are `sum` which computes the sum of each column, and `mean` which computes the mean of each column:

```
>> sum(m) % compute the sum of each column
ans =
    12    15    18
>> mean(m) % compute the mean of each column
ans =
     4     5     6
```

How to take the mean of each *row*? One way would be to compute the transpose:

```
>> mean(m') % compute the mean of each row of matrix m
ans =
     2     5     8
```

Another way would be to read the Help documentation on `mean` and find that it takes an optional second argument:

```
>> mean(m, 2) % compute the mean of each row of matrix m
ans =
     2
     5
     8
```


Note that here the answer is a column vector.

And `reshape(m, r, c)` reshapes matrix (or vector) `m` to have `r` rows and `c` columns:

```
>> reshape(m, 1, 9) % reshape matrix m to 1x9 vector
ans =
     1     4     7     2     5     8     3     6     9
```

4 Control structures

MATLAB has the usual set of control structures: `for`, `if-else`, etc.

The `for` loop allows us to repeat certain commands. All of the loop structures in matlab are started with the keyword `for` and they all end with the word `end`. A `for` loop requires a vector of loop variable values, eg:

```
>> for (i=1:5) % repeat 5 times
      i       % print the iteration in the console
end
i =
     1
i =
     2
i =
     3
i =
     4
i =
     5
```

or

```
>> points = [3 5 7 9 11];
>> for i = points % iterate over the values of 'points'
      i         % print the value of 'points' in ith iteration
end
i =
     3
i =
     5
i =
     7
i =
     9
i =
    11
```

Use the help system to find out more.

To control the sequence of your program, the `if-else` control structure can be used. The way to do that is to put the code within an `if` statement (and possibly in an `else` statement) and finish with the `end` statement. For example:

```
>> k = 4; m = 7;
>> if k > m % if k > m print -1
    j = -1
    else % else if k < m print 1
    j = 1
end
j =
    1
```

5 Next lab session

In the next lab, we will continue with some more sophisticated matrix operations, we will learn how to program in MATLAB using scripts and functions. Also, we will go through data visualization using plots and how to handle text files.

If you want to clear the command window you can type:

```
>> clc % clear commands shown in 'Command Window'
```

and if you want to clear all your data and files that are stored in the workspace, you can use the `clear` command. Be careful though, it does not ask you for a second opinion!

```
>> clear % clear data stored in 'Workspace'
```