

Earley Parsing

Informatics 2A: Lecture 21

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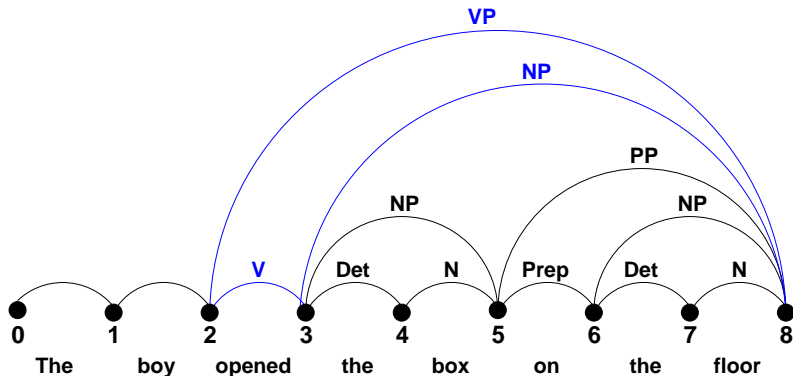
4 November 2015

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 - What's wrong with CYK
 - Adding Prediction to the Chart

- 2 The Earley Parsing Algorithm
 - The PREDICTOR Operator
 - The SCANNER Operator
 - The COMPLETER Operator
 - Earley parsing: example
 - Comparing Earley and CYK

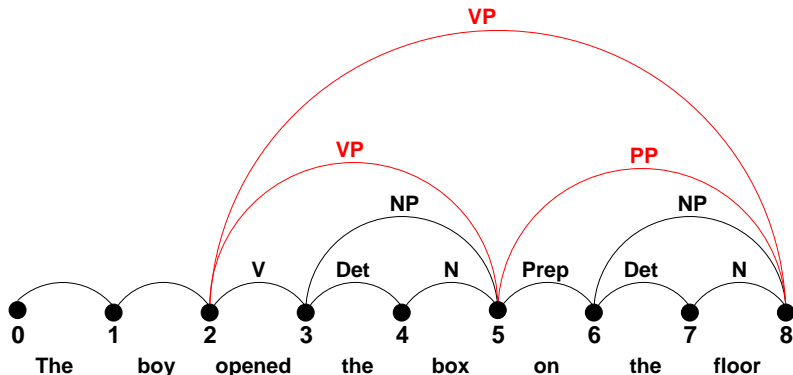
Graph representation

The CYK chart can also be represented as a **graph**. E.g. for a certain grammar containing rules $VP \rightarrow V NP$ and $VP \rightarrow VP PP$:



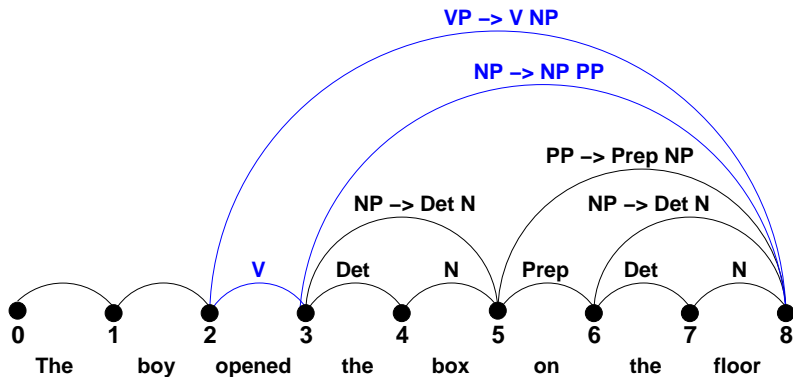
Graph representation

An alternative analysis. Note we don't know which production the VP arc [2, 8] represents: $VP \rightarrow V NP$ or $VP \rightarrow VP PP$.



CYK Chart entries

If the entire **production** were recorded, rather than just its LHS (ie, the constituent that it analyses), then we'd (usually) know.



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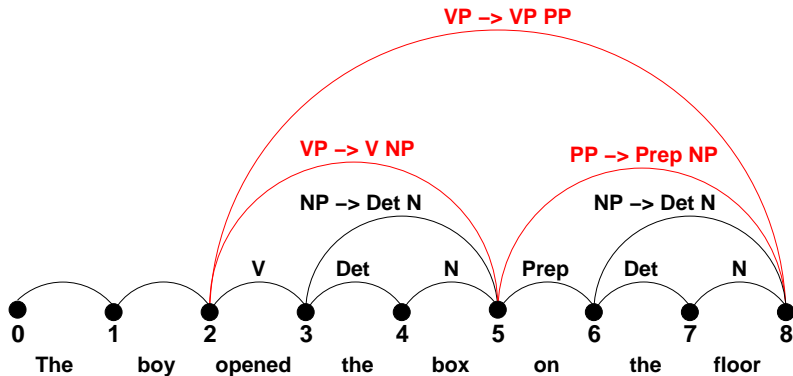
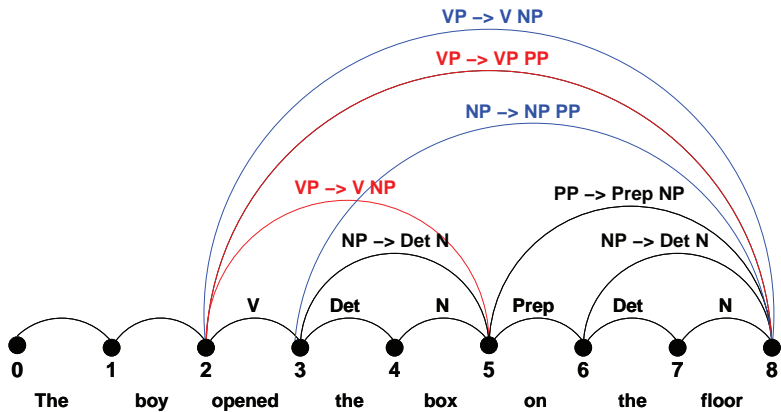


Chart entries: Both analyses



What's good about CYK

But by remembering more of the structure of each analysis, we increase the size of the chart, without improving its ability to support new inferences.

We don't need to know how $\langle 2, VP, 5 \rangle$ was produced when combining it with $\langle 5, PP, 8 \rangle$ to produce $\langle 2, VP, 8 \rangle$.

By remembering only what we need to make new inferences, we save runtime.

What's wrong with CYK

The CYK algorithm avoids redundant work by storing in a chart all the constituents it finds.

But it populates the table with **phantom constituents**, that don't form part of any complete parse. Can be a significant problem in long sentences.

The idea of the *Earley algorithm* is to avoid this, by only building constituents that are compatible with the input read so far.

Key idea: as well as **completed productions** (ones whose entire RHS have been recognized), we also record **incomplete productions** (ones for which there may so far be only partial evidence).

- **Incomplete productions** (aka **incomplete constituents**) are effectively **predictions** about what might come next and what will be learned from finding it.
- **Incomplete constituents** can be represented using an extended form of production rule called a **dotted rule**, e.g.
 $VP \rightarrow V \bullet NP$.
- The **dot** indicates how much of the RHS has already been found. The rest is a prediction of what is to come.

- Allows arbitrary CFGs
- Top-down control
- Fills a table in a single sweep over the input
- Table entries represent:
 - **Completed** constituents and their locations
 - **In-progress** constituents
 - **Predicted** constituents

The table entries are called states and are represented with **dotted-rules**.

$S \rightarrow \bullet VP$ [0,0]

A *VP* is **predicted** at the start of the sentence

$NP \rightarrow Det \bullet Nominal$ [1,2]

An *NP* is **in progress**; seen *Det*, *Nominal* is expected

$VP \rightarrow V NP \bullet$ [0,3]

A *VP* **has been found** starting at 0 and ending at 3

Once chart is populated there should be an *S* the final column that spans from 0 to *N* and is complete: $S \rightarrow \alpha \bullet [0, N]$. If that's the case you're done.

Sketch of Earley Algorithm

- 1 **Predict** all the states you can upfront, working top-down from S
- 2 For each word in the input:
 - 1 **Scan in** the word.
 - 2 **Complete** or extend existing states based on matches.
 - 3 Add new **predictions**.
- 3 When out of words, look at the chart to see if you have a winner.

The algorithm uses three basic operations to process states in the chart: **PREDICTOR** and **COMPLETER** add states to the chart entry being processed; **SCANNER** adds a state to the next chart entry.

- Creates new states representing top-down expectations
- Applied to any state that has a non-terminal (other than a part-of-speech category) immediately to right of dot
- Application results in creation of one new state for each alternative expansion of that non-terminal
- **New states placed into same chart entry as generating state**

| $S \rightarrow \bullet VP, [0,0]$ | | |
|-----------------------------------|-----------------------|---------------------|
| VP | $\rightarrow \bullet$ | $Verb, [0,0]$ |
| VP | $\rightarrow \bullet$ | $Verb NP, [0,0]$ |
| VP | $\rightarrow \bullet$ | $Verb NP PP, [0,0]$ |
| VP | $\rightarrow \bullet$ | $Verb PP, [0,0]$ |
| VP | $\rightarrow \bullet$ | $VP PP, [0,0]$ |

- Applies to states with a part-of-speech category to right of dot
- Incorporates into chart a state corresponding to prediction of a word with particular part-of-speech
- **Creates new state from input state with dot advanced over predicted input category**
- Unlike CYK, only parts-of-speech of a word that are predicted by some existing state will enter the chart (top-down input)

$VP \rightarrow \bullet \textit{Verb NP}, [0,0]$

$VP \rightarrow \textit{book} \bullet \textit{NP}, [0,1]$

- Applied to state when its dot has reached right end of the rule
- This means that parser has successfully discovered a particular grammatical category over some span of the input
- COMPLETER finds and advances all previously created states that were looking for this category at this position in input
- **Creates states copying the older state, advancing dot over expected category, and installing new state in chart**

NP → *Det Nominal* •, [1,3]

finds state

VP → *Verb* • *NP*, [0,1]

finds state

VP → *Verb* • *NP PP*, [0,1]

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NP → *Det Nominal* •, [1,3]

finds state

VP → *Verb* • *NP*, [0,1]

finds state

VP → *Verb* • *NP PP*, [0,1]

adds complete state

VP → *Verb NP* •, [0,3]

adds incomplete state

VP → *Verb NP* • *PP*, [0,3]

We will use the grammar to parse the sentence “*Book that flight*”.

Grammar Rules

$S \rightarrow NP VP$

$S \rightarrow Aux NP VP$

$S \rightarrow VP$

$NP \rightarrow Pronoun$

$NP \rightarrow Proper-Noun$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow Noun$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow Verb$

$VP \rightarrow Verb NP$

$VP \rightarrow Verb NP PP$

$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

$Verb \rightarrow book|include|prefer$

$Noun \rightarrow book|flight|meal$

$Det \rightarrow that|this|these$

Earley parsing: example[0]

| state | rule | start/end | reason |
|-------|--------------------------------------|-----------|-----------|
| S1 | $S \rightarrow \bullet NP VP$ | [0,0] | Predictor |
| S2 | $S \rightarrow \bullet Aux NP VP$ | [0,0] | Predictor |
| S3 | $S \rightarrow \bullet VP$ | [0,0] | Predictor |
| S4 | $NP \rightarrow \bullet Pronoun$ | [0,0] | Predictor |
| S5 | $NP \rightarrow \bullet Proper-Noun$ | [0,0] | Predictor |
| S6 | $NP \rightarrow \bullet Det Nominal$ | [0,0] | Predictor |
| S7 | $VP \rightarrow \bullet Verb$ | [0,0] | Predictor |
| S8 | $VP \rightarrow \bullet Verb NP$ | [0,0] | Predictor |
| S9 | $VP \rightarrow \bullet Verb NP PP$ | [0,0] | Predictor |
| S10 | $VP \rightarrow \bullet Verb PP$ | [0,0] | Predictor |
| S11 | $VP \rightarrow \bullet VP PP$ | [0,0] | Predictor |

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| state | rule | start/end | reason |
|-------|--|-----------|-----------|
| S12 | <i>Verb</i> → <i>book</i> • | [0,1] | Scanner |
| S13 | <i>VP</i> → <i>Verb</i> • | [0,1] | Completer |
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Earley parsing: example[2]

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|-------|---|-----------|-----------|
| S23 | <i>Det</i> → <i>that</i> • | [1,2] | Scanner |
| S24 | <i>NP</i> → <i>Det</i> • <i>Nominal</i> | [1,2] | Completer |
| S25 | <i>Nominal</i> → • <i>Noun</i> | [2,2] | Predictor |
| S26 | <i>Nominal</i> → • <i>Nominal Noun</i> | [2,2] | Predictor |
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| state | rule | start/end | reason |
|-------|---|-----------|-----------|
| S23 | <i>Det</i> → <i>that</i> • | [1,2] | Scanner |
| S24 | <i>NP</i> → <i>Det</i> • <i>Nominal</i> | [1,2] | Completer |
| S25 | <i>Nominal</i> → • <i>Noun</i> | [2,2] | Predictor |
| S26 | <i>Nominal</i> → • <i>Nominal Noun</i> | [2,2] | Predictor |
| S27 | <i>Nominal</i> → • <i>Nominal PP</i> | [2,2] | Predictor |

Earley parsing: example[2]

| state | rule | start/end | reason |
|-------|---|-----------|-----------|
| S23 | <i>Det</i> → <i>that</i> • | [1,2] | Scanner |
| S24 | <i>NP</i> → <i>Det</i> • <i>Nominal</i> | [1,2] | Completer |
| S25 | <i>Nominal</i> → • <i>Noun</i> | [2,2] | Predictor |
| S26 | <i>Nominal</i> → • <i>Nominal Noun</i> | [2,2] | Predictor |
| S27 | <i>Nominal</i> → • <i>Nominal PP</i> | [2,2] | Predictor |

Earley parsing: example[3]

| state | rule | start/end | reason |
|-------|---|-----------|-----------|
| S28 | <i>Noun</i> → <i>flight</i> • | [2,3] | Scanner |
| S29 | <i>Nominal</i> → <i>Noun</i> • | [2,3] | Completer |
| S30 | <i>NP</i> → <i>Det Nominal</i> • | [1,3] | Completer |
| S31 | <i>Nominal</i> → <i>Nominal</i> • <i>Noun</i> | [2,3] | Completer |
| S32 | <i>Nominal</i> → <i>Nominal</i> • <i>PP</i> | [2,3] | Completer |
| S33 | <i>VP</i> → <i>Verb NP</i> • | [0,3] | Completer |
| S34 | <i>VP</i> → <i>Verb NP</i> • <i>PP</i> | [0,3] | Completer |
| S35 | <i>PP</i> → <i>Prep</i> • <i>NP</i> | [3,3] | Predictor |
| S36 | <i>S</i> → <i>VP</i> • | [0,3] | Completer |
| S37 | <i>VP</i> → <i>VP</i> • <i>PP</i> | [0,3] | Completer |

Earley parsing: example[3]

| state | rule | start/end | reason |
|-------|---|-----------|-----------|
| S28 | <i>Noun</i> → <i>flight</i> • | [2,3] | Scanner |
| S29 | <i>Nominal</i> → <i>Noun</i> • | [2,3] | Completer |
| S30 | <i>NP</i> → <i>Det Nominal</i> • | [1,3] | Completer |
| S31 | <i>Nominal</i> → <i>Nominal</i> • <i>Noun</i> | [2,3] | Completer |
| S32 | <i>Nominal</i> → <i>Nominal</i> • <i>PP</i> | [2,3] | Completer |
| S33 | <i>VP</i> → <i>Verb NP</i> • | [0,3] | Completer |
| S34 | <i>VP</i> → <i>Verb NP</i> • <i>PP</i> | [0,3] | Completer |
| S35 | <i>PP</i> → <i>Prep</i> • <i>NP</i> | [3,3] | Predictor |
| S36 | <i>S</i> → <i>VP</i> • | [0,3] | Completer |
| S37 | <i>VP</i> → <i>VP</i> • <i>PP</i> | [0,3] | Completer |

Earley parsing: example[3]

| state | rule | start/end | reason |
|-------|---|-----------|-----------|
| S28 | <i>Noun</i> → <i>flight</i> • | [2,3] | Scanner |
| S29 | <i>Nominal</i> → <i>Noun</i> • | [2,3] | Completer |
| S30 | <i>NP</i> → <i>Det Nominal</i> • | [1,3] | Completer |
| S31 | <i>Nominal</i> → <i>Nominal</i> • <i>Noun</i> | [2,3] | Completer |
| S32 | <i>Nominal</i> → <i>Nominal</i> • <i>PP</i> | [2,3] | Completer |
| S33 | <i>VP</i> → <i>Verb NP</i> • | [0,3] | Completer |
| S34 | <i>VP</i> → <i>Verb NP</i> • <i>PP</i> | [0,3] | Completer |
| S35 | <i>PP</i> → <i>Prep</i> • <i>NP</i> | [3,3] | Predictor |
| S36 | <i>S</i> → <i>VP</i> • | [0,3] | Completer |
| S37 | <i>VP</i> → <i>VP</i> • <i>PP</i> | [0,3] | Completer |

Earley parsing: example[3]

| state | rule | start/end | reason |
|-------|---|-----------|-----------|
| S28 | <i>Noun</i> → <i>flight</i> • | [2,3] | Scanner |
| S29 | <i>Nominal</i> → <i>Noun</i> • | [2,3] | Completer |
| S30 | <i>NP</i> → <i>Det Nominal</i> • | [1,3] | Completer |
| S31 | <i>Nominal</i> → <i>Nominal</i> • <i>Noun</i> | [2,3] | Completer |
| S32 | <i>Nominal</i> → <i>Nominal</i> • <i>PP</i> | [2,3] | Completer |
| S33 | <i>VP</i> → <i>Verb NP</i> • | [0,3] | Completer |
| S34 | <i>VP</i> → <i>Verb NP</i> • <i>PP</i> | [0,3] | Completer |
| S35 | <i>PP</i> → <i>Prep</i> • <i>NP</i> | [3,3] | Predictor |
| S36 | <i>S</i> → <i>VP</i> • | [0,3] | Completer |
| S37 | <i>VP</i> → <i>VP</i> • <i>PP</i> | [0,3] | Completer |

The Earley Algorithm

```
function EARLEY-PARSE(words, grammar) returns chart

  ENQUEUE( $(\gamma \rightarrow \bullet S, [0, 0])$ , chart[0])
  for  $i \leftarrow$  from 0 to LENGTH(words) do
    for each state in chart[ $i$ ] do
      if INCOMPLETE?(state) and
        NEXT-CAT(state) is not a part of speech then
          PREDICTOR(state)
      elseif INCOMPLETE?(state) and
        NEXT-CAT(state) is a part of speech then
          SCANNER(state)
      else
        COMPLETER(state)
    end
  end
  return(chart)
```

The Earley Algorithm

```
procedure PREDICTOR( $(A \rightarrow \alpha \bullet B \beta, [i, j])$ )  
  for each  $(B \rightarrow \gamma)$  in GRAMMAR-RULES-FOR( $B, grammar$ ) do  
    ENQUEUE( $(B \rightarrow \bullet \gamma, [j, j])$ ,  $chart[j]$ )  
  end  
  
procedure SCANNER( $(A \rightarrow \alpha \bullet B \beta, [i, j])$ )  
  if  $B \subset PARTS-OF-SPEECH(word[j])$  then  
    ENQUEUE( $(B \rightarrow word[j], [j, j+1])$ ,  $chart[j+1]$ )  
  
procedure COMPLETER( $(B \rightarrow \gamma \bullet, [j, k])$ )  
  for each  $(A \rightarrow \alpha \bullet B \beta, [i, j])$  in  $chart[j]$  do  
    ENQUEUE( $(A \rightarrow \alpha B \bullet \beta, [i, k])$ ,  $chart[k]$ )  
  end
```

Parsing the Input

As with CYK we have formulated a **recognizer**. We can change it to a **parser** by adding backpointers so that each state knows where it came from.

| | | | | |
|----------|-----|----------------------------------|-------|------------|
| Chart[1] | S12 | <i>Verb</i> → <i>book</i> • | [0,1] | Scanner |
| Chart[2] | S23 | <i>Det</i> → <i>that</i> • | [1,2] | Scanner |
| Chart[3] | S28 | <i>Noun</i> → <i>flight</i> • | [2,3] | Scanner |
| | S29 | <i>Nominal</i> → <i>Noun</i> • | [2,3] | (S28) |
| | S30 | <i>NP</i> → <i>Det Nominal</i> • | [1,3] | (S23, S29) |
| | S33 | <i>VP</i> → <i>Verb NP</i> • | [0,3] | (S12, S30) |
| | S36 | <i>S</i> → <i>VP</i> • | [0,3] | (S33) |

Comparing Earley and CYK

- For such a simple example, there seems to be a lot of useless stuff in the chart.
- We are predicting phrases that aren't there at all!
- That's the flipside to the CYK problem.

Comparing Earley and CYK

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Did we solve ambiguity?

Comparing Earley and CYK

- For such a simple example, there seems to be a lot of useless stuff in the chart.
- We are predicting phrases that aren't there at all!
- That's the flipside to the CYK problem.

Did we solve ambiguity? Both CYK and Earley may result in multiple S structures for the $[0, N]$ table entry. Of course, neither can tell us which one is 'right'.

The Asymptotic Complexity of Earley and CKY

- Both algorithms are cubic in n (length of string)
- CKY needs to construct $O(n^2)$ elements in the chart (in the worst-case), and processing each element to create it is $O(n)$, so it is $O(n^3)$ in total
- Earley also needs to construct $O(n^2)$ elements, and the `COMPLETE` operation takes $O(n)$ time. It could potentially run on $O(n^2)$ elements, so the complexity is again $O(n^3)$

More about Asymptotic Complexity of Earley

- The `COMPLETER` operation really takes $O(i^2)$ at iteration i
- For unambiguous grammars, Earley shows that the `COMPLETER` operation can take at most $O(i)$ time
- This means that the complexity for unambiguous grammars is $O(n^2)$
- There are also some specialised grammars for which the Earley algorithm takes $O(n)$ time

Connection between the Earley Algorithm and CKY

What happens if we run the Earley algorithm on a grammar in Chomsky normal form?

- This is essentially CKY with top-down filtering
- It will only create (completed) elements in the chart, if there is a left-most derivation that leads to that constituent

- The Earley algorithm uses dynamic programming to implement a **top-down** search strategy.
- Single left to right pass that fills chart with entries.
- Dotted rule represents progress in recognizing RHS of rule.
- Algorithm always moves forward, never backtracks to previous chart entry, once it has moved on.
- States are processed using PREDICTOR, COMPLETER, SCANNER operations.

Reading: Same as for Lecture 17

Next lecture: Resolving ambiguity using statistical parsing.