INSTRUCTIONS TO CANDIDATES

• Note that ALL QUESTIONS ARE COMPULSORY.

• DIFFERENT QUESTIONS MAY HAVE DIFFERENT NUMBERS OF TOTAL MARKS. Take note of this in allocating time to questions.

• WRITE YOUR ANSWERS ON THE EXAM PAPER ITSELF. Write as legibly as possible.

• In the answer to any part of any question, you may use any function specified in an earlier part of that question. You may do this whether or not you actually provided a definition for the earlier part; nor will you be penalized in a later part if your answer to an earlier part is incorrect.

• Unless otherwise stated, you may use any function from the standard prelude, including the libraries Char, List, and Maybe. You need not write import declarations.

• As an aid to memory, some functions from the standard prelude that you may wish to use are listed on the next page. You need not use all the functions.

PLEASE INSERT YOUR NAME AND MATRICULATION NUMBER IN THE SPACE BELOW:

<table>
<thead>
<tr>
<th>MATRICULATION NUMBER</th>
<th>NAME</th>
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</thead>
</table>
div, mod :: Integral a => a -> a -> a
even, odd :: Integral a => a -> Bool
(+), (*), (-), (/) :: Num a => a -> a -> a
(<), (<=), (>, (>=) :: Ord => a -> a -> Bool
(==), (/=) :: Eq a => a -> a -> Bool
not :: Bool -> Bool
max, min :: Ord a => a -> a -> a
isAlpha, isAlphaNum, isLower, isUpper, isDigit :: Char -> Bool
toLower, toUpper :: Char -> Char
ord :: Char -> Int
chr :: Int -> Char

Figure 1: Basic functions

div, mod :: Integral a => a -> a -> a
even, odd :: Integral a => a -> Bool
(+), (*), (-), (/) :: Num a => a -> a -> a
(<), (<=), (>, (>=) :: Ord => a -> a -> Bool
(==), (/=) :: Eq a => a -> a -> Bool
not :: Bool -> Bool
max, min :: Ord a => a -> a -> a
isAlpha, isAlphaNum, isLower, isUpper, isDigit :: Char -> Bool
toLower, toUpper :: Char -> Char
ord :: Char -> Int
chr :: Int -> Char

Figure 1: Basic functions

sum, product :: (Num a) => [a] -> a and, or :: [Bool] -> Bool
sum [1.0,2.0,3.0] = 6.0 and [True,False,True] = False
product [1,2,3,4] = 24 or [True,False,True] = True

maximum, minimum :: (Ord a) => [a] -> a reverse :: [a] -> [a]
maximum [3,1,4,2] = 4 reverse "goodbye" = "eybdoog"
minimum [3,1,4,2] = 1

concat :: [[a]] -> [a] (+++) :: [a] -> [a] -> [a]
concat ["go","od","bye"] = "goodbye" "good" ++ "bye" = "goodbye"

(!!) :: [a] -> Int -> a length :: [a] -> Int
[9,7,5] !! 1 = 7 length [9,7,5] = 3

head :: [a] -> a tail :: [a] -> [a]
head "goodbye" = 'g' tail "goodbye" = "oodbye"

init :: [a] -> [a] last :: [a] -> a
init "goodbye" = "goodby" last "goodbye" = 'e'

takeWhile :: (a->Bool) -> [a] -> [a] take :: Int -> [a] -> [a]
takeWhile isLower "goodBye" = "good" take 4 "goodbye" = "good"
dropWhile :: (a->Bool) -> [a] -> [a] drop :: Int -> [a] -> [a]
dropWhile isLower "goodBye" = "Bye" drop 4 "goodbye" = "bye"

elem :: (Eq a) => a -> [a] -> Bool replicate :: Int -> a -> [a]
elem 'd' "goodbye" = True replicate 5 '*’' = "*****"

zip :: [a] -> [b] -> [(a,b)]
zip [1,2,3,4] [1,4,9] = [(1,1),(2,4),(3,9)]

Figure 2: Library functions
1. (a) Write a function \( f \) :: \texttt{Char} -> \texttt{Bool} that determines whether or not an alphabetic character is in the first half of the alphabet (letters before \texttt{M}, inclusive) or not. It should work for both upper and lower case letters. For example,

\[
\begin{align*}
f \ 'e' &= \text{True} & f \ 'P' &= \text{False} & f \ 'q' &= \text{False} \\f \ 'G' &= \text{True} & f \ 'n' &= \text{False} & f \ 'M' &= \text{True}
\end{align*}
\]

For any character that is not an alphabetic character, \( f \) should return an error.

\[15 \text{ marks}\]

(b) Using \( f \), define a function \( g \) :: \texttt{String} -> \texttt{Bool} that given a string returns \texttt{True} if the string contains more letters in the first half of the alphabet than in the second half, ignoring any character that is not an alphabetic character. For example,

\[
\begin{align*}
g \ "SyzYGy" &= \text{False} & g \ "aB7L!e" &= \text{True} & g \ "" &= \text{False} \\g \ "Aardvark" &= \text{True} & g \ "emnity" &= \text{False}
\end{align*}
\]

Your definition may use \textit{basic functions}, \textit{list comprehension}, and \textit{library functions}, but not recursion.

\[20 \text{ marks}\]

(c) Again using \( f \), define a function \( h \) :: \texttt{String} -> \texttt{Bool} that behaves identically to \( g \), this time using \textit{basic functions} and \textit{recursion}, but not list comprehension or library functions.

\[20 \text{ marks}\]
2. (a) Write a function \( c : \mathbb{[Int]} \to \mathbb{[Int]} \) that returns a list containing all of the elements in the argument list that occur twice in succession. If an element occurs \( n \) times in succession, for \( n \geq 2 \), then it should appear \( n - 1 \) times in succession in the result. The value of the function applied to the empty list need not be defined.

\[
\begin{align*}
  c \ [3,1,1,3,3,5] & \quad = \quad [1,3] \\
  c \ [4,1,1,1,4,4] & \quad = \quad [1,1,4] \\
  c \ [2,2,2,2,2] & \quad = \quad [2,2,2,2] \\
  c \ [2,1,4,1,2] & \quad = \quad [] \\
  c \ [3,3,1,3,1] & \quad = \quad [3] \\
  c \ [42] & \quad = \quad []
\end{align*}
\]

Your definition may use \textit{basic functions}, \textit{list comprehension}, and \textit{library functions}, but not recursion.

[20 marks]

(b) Define a second function \( d : \mathbb{[Int]} \to \mathbb{[Int]} \) that behaves identically to \( c \), this time using \textit{basic functions} and \textit{recursion}, but not list comprehension or other library functions.

[20 marks]

(c) Write a QuickCheck property \( \text{prop\_cd} \) to confirm that \( c \) and \( d \) behave identically. Give the type signature of \( \text{prop\_cd} \) and its definition.

[5 marks]