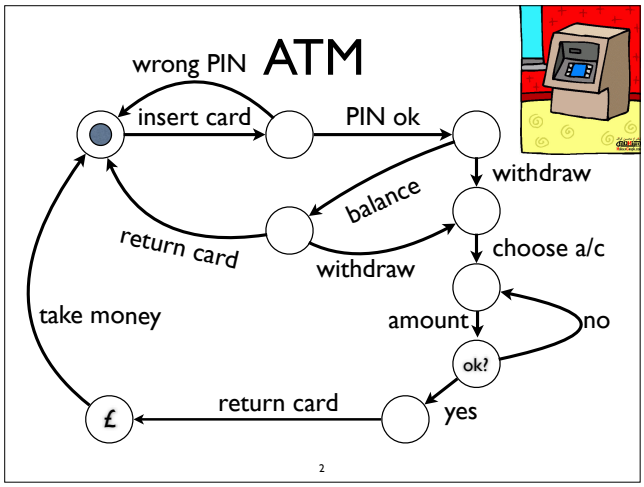
Finite-State Machines (Automata) lecture 11

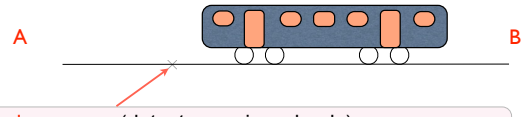
CI

- a simple form of computation
- used widely
- one way to find patterns

- with thanks to Gérard Berry


ATM
wrong PIN
insert card
PIN ok
withdraw
balance
return card
withdraw
choose a/c
take money
amount
no
ok?
£
return card
yes
2

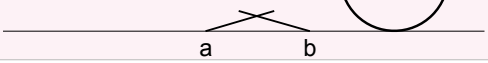
Counting trains



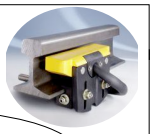
axle sensor (detects passing wheels)

from-a-to-b : a↓ ; b↓ ; a↑ ; b↑

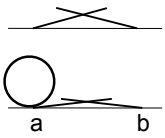
from-b-to-a : b↓ ; a↓ ; b↑ ; a↑



Finite-state machines

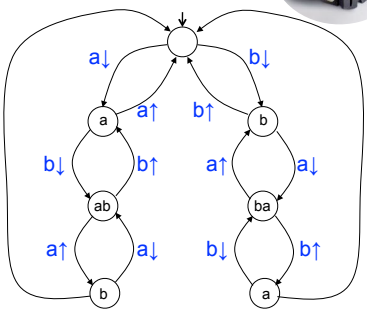


axle sensor



inputs :
a↑, a↓, b↑, b↓

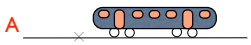
outputs :
from-a-to-b,
from-b-to-a



b↑ / from-a-to-b

a↑ / from-b-to-a

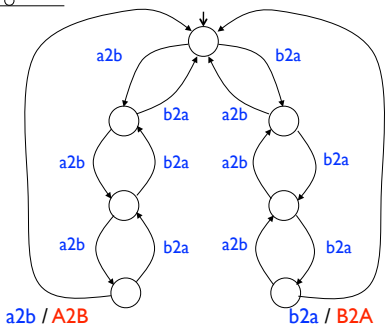
Hierarchical FSMs



carriage counter

inputs :
a2b, b2a

outputs :
A2B, B2A



a2b / A2B

b2a / B2A

a2b = from-a-to-b

Application Fields

Industry

- real-time control, vending machines, cash dispensers, etc.

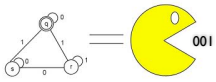
Electronic circuits

- data path / control path
- memory / cache handling
- protocols, USB, etc.

Communication protocols

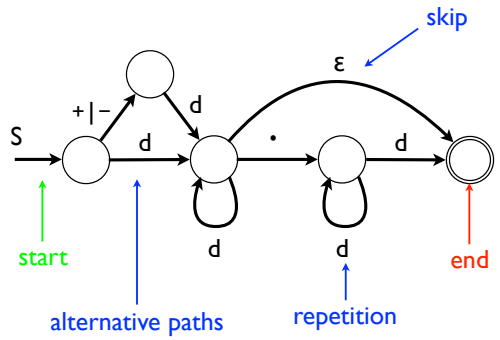
- initiation and maintenance of communication links
- error detection and handling, packet retransmission

Language analysis

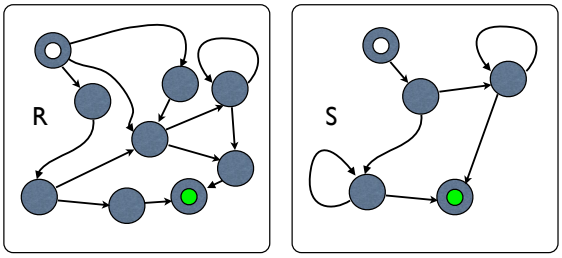


- natural languages
- programming languages
- search engines

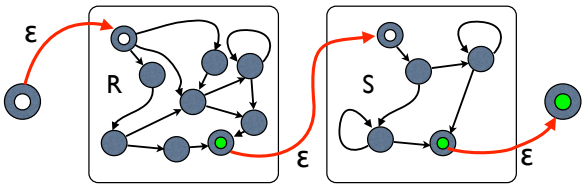
A Decimal Number



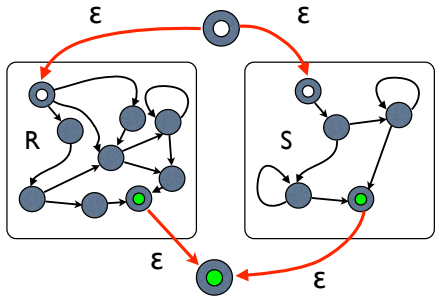
finite state machines



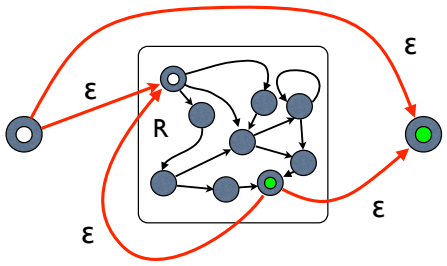
sequence
RS



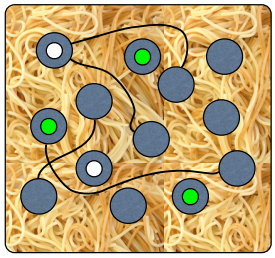
alternation
R|S



iteration
R*

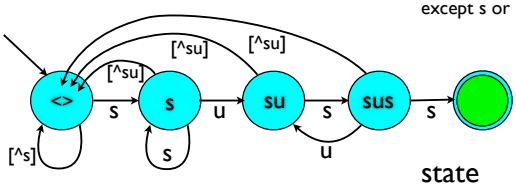


finite state spaghetti



suss this?

[^su] stands for any character except s or u



FSAs can be represented as:
- transition tables as well as
- graphs

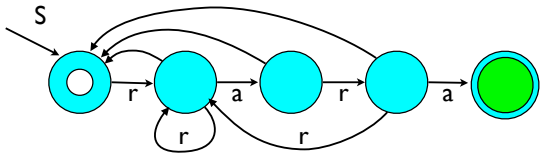
If you're in state s and you're looking at a u, go to state su

[^su] stands for any character except s or u

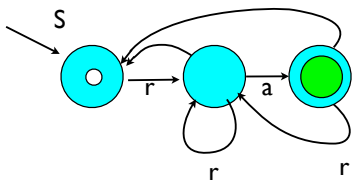
state

input	[]	s	su	sus	●
s	s	s	sus	●	
u	[]	su	[]	su	
[^su]	[]	[]	[]	[]	

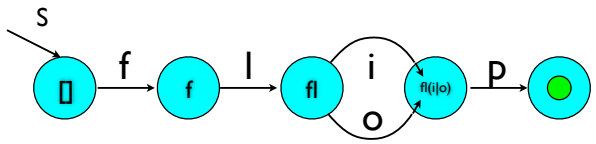
rara



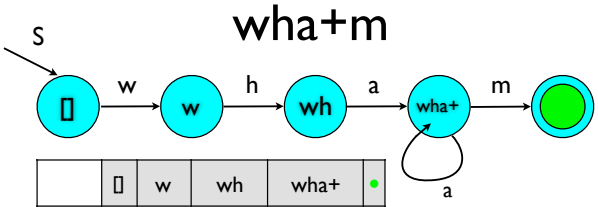
ra(ra)*



(flip)|(flop) = fl(i|o)p



wha+m



	▯	w	wh	wha+	•
w	w	▯	▯	▯	
h	▯	wh	▯	▯	
a	▯	▯	wha+	wha+	
m	▯	▯	▯	•	