## Introduction to MATLAB

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## Hello!

- Informal lab / lecture session
- Assumes no prior programming experience
- Two hours, with a 10 minute break
- One-third talking and two-thirds practical work
- Feel free to ask us questions, at any time
- Feel free to help each other and discuss the exercises


## Purpose

- This is an introduction to MATLAB
- This will help you get familiar with MATLAB and some general computer programming concepts
- Exploration is encouraged - try the examples given, and anything else that occurs to you!


## Failure

- Computer programming involves lots of failure
- Usually you have to fail several times to succeed once
- This is ok and happens to everyone
- Most of the time there will be an error message, which will give you a clue to the solution for the problem


## Keyboard practicalities

- Go to System Preferences -> Language and Region
- Choose Keyboard Preferences
- Click on +, and add "British-PC"
- Close this window
- At the top-right of the screen, click on the flag and make sure "British-PC" is selected


## Even so ....

- One key is transposed on some machines!
- This is the key with:

- It's swapped with the very top-left key, which is next to 1


## MATLAB

- Open MATLAB (in Applications -> Science)



## The MATLAB prompt

- From now on, whenever you see this:
>>
it indicates something that you can type in to MATLAB
- Some of the things you type in will produce error messages
- Some of the things I tell you to type in will produce error messages


## Saying hello to MATLAB

- Try this:
>> 'hello'


## MATLAB as a calculator

$$
\left.\begin{array}{l}
\text { >> } 2+2 \\
\gg 2-20 \\
\gg 6 * 3 \\
\gg 1 / 10 \\
\gg 10^{\wedge} 3 \\
\gg \\
\gg \\
\gg
\end{array} 2^{*}(3)+4+4\right)
$$

## Numbers

- This last answer is in "floating point" notation

$$
\begin{aligned}
2.5 \mathrm{e}-4 & =2.5 \times 10^{-4} \\
& =2.5 \times 0.0001 \\
& =0.00025
\end{aligned}
$$

- Try these:
>> 8e3
>> $4.5 e 2$
>> lel


## Numbers

- There are also some "special" values you might see. MATLAB still regards these as numbers. For example:
>> 1/0
- You may also see:
- NaN ("Not a Number")
- i (or j) for the square root of -1


## Variables

- We can create a variable using =
>> my_number = 3
- A variable is like a box for a value
- The variable name is the label on the box
- MATLAB will remember the value we give:
>> my_number



## Variables

- You can use a variable with a number in it wherever you would use a number
>> my_number + 5
- You can put the result of such a calculation into another variable
>> another_number = my_number + 5


## Variables

$\gg a=3$
$\gg \mathrm{a}$
$\gg b=14$
$\gg a+b$
>> you_can_use_long_names = 5000
$\gg d=a+20$
>> i_dont_exist

## Variables

-What can you use as a variable name?
>> a = 12
>> $A=0.7$
>> 1number = 43
>> _things = 10
>> word count $=20$
>> end $=-40000$

## Variable names

- Variable names must start with a letter, and can contain letters, numbers and underscores
- Names are case sensitive
- They can't contain spaces, so what if you want to have multiple words in your variable name?
>> numberofthings $=12$
>> numberOfThings $=12$
>> number_of_things $=12$


## More variables

- There are other kinds of values in MATLAB, for example, text:
>> some text $=$ 'a line of text'
$\gg$ text $\overline{2}=$ ' and some more text'
>> text3 $=$ strcat(some_text, text2)
- or true/false values
>> is_ready = true


## Types

- These different kinds of values are referred to as types
- Numbers - floating point

0 -1200 5.0e20 0.0001 Inf NaN

- Text - string
'hello' '1000' 'this is a text'
- True or False - Boolean or logical true (1), false (0)


## Different ways to get results

- Functions and operators



## Different ways to get results

- Despite being written differently, these do a very similar thing!
- In both cases, there are values going in, something is done with them, and there's one value going out.
- Names for the values going in: arguments, parameters, operands


## This looks familiar!

- This is similar to running a command line program
- Program name, with parameters: cp file1 file2
- Operator, with parameters: $3+4$
- Function name, with parameters: strcat('hello ',text2)


## This looks familiar! (part 2)

- The MATLAB prompt keeps track of your previous commands
- You can use the up arrow to go back through this history
- You can edit a line and run it again, or just run it again as-is
- This is exactly the same as the Unix shell


## Comments

- Anything you write after a \% is a comment
- This can be used to document the intent behind a piece of code
- For example, if you're doing something based on a paper, you could add a citation \% as per Mendel, 1865


## Comments

- Try it!
>> \% this will be ignored
>> $\mathrm{a}=12$ \% here is my comment ... and you can check that this fails without \%:
>> $a=12$ here is my comment


## Comments

- This can be used to temporarily disable code (more useful in code files, which we'll see later)

$$
\begin{aligned}
& a=16 \\
& \% a=16
\end{aligned}
$$

- This is referred to as "commenting out" code


## Getting help

- If you see a function you don't know, either ....
- put the cursor on its name and press F1, or
- right-click and choose "Help on Selection", or >> doc function_name
- The only function we know so far is strcat
- Try one of these methods, to see the help for strcat
(you may have to wait a moment!)


## Getting help

- More generally, press F1, click on the help icon, or use the search box to see documentation



## Getting help

- Plus, you can always ask the internet!
- The usual caveat applies: the person giving advice might have a different system to you


## Showing results

- To show (print) a value in MATLAB we can just write it
>> result $=97$
>> result
- This shows the variable name and the value


## Not showing results

- To do something without showing a value, use a semicolon ';' at the end of the line >> result = 97;
- This still runs
- The variable 'result' will be set to 97
... but nothing is shown on the screen.


## Printing results, disp

- Note that this also prints the variable name (or if there is none, a default "ans =")
- To print a value without this, use disp()
- Try these and compare:
>> 10004
>> disp(10004)
>> 'hello!'
>> disp('hello!')


## fprintf

- If we want more control of how values are printed we can use the fprintf function
- fprintf can print one value:
>> a = 20;
>> fprintf('The value of a is \%d.\n',a)
- or many:
>> b = 18.0015
>> fprintf('a is \%d, b is \%f.\n',a,b)
- or none:
>> fprintf('Good afternoon!\n')


## fprintf

- The first argument to fprintf is a format string
- This can contain a number of special codes starting with \%
- This code specifies how to print the value


## Format strings

- Format strings print the values they are given
- Special codes starting with \% in the string are replaced with these values, in order
>> things = 8
>> fprintf('number of things: \%d\n',things)
>> $\mathrm{a}=6$
>> b = 14
>> fprintf('some numbers: \%d and \%d\n',a,b)



## Format codes

- These codes starting with \% are also called format specifiers
- There are many of these, and they correspond to the type of the value being shown:
- \%d means "a whole number"
- \%f means "a floating-point number" (i.e. a number with a decimal point)


## Format codes

- Sometimes a value can be shown in more than one way
- E.g. if the value is 18 , we can print this as a whole number or a floating-point number:
fprintf('\%f or \%d ....\n',18,18)


## Newlines

- In the format string, 'In' means newline
- Try this:
fprintf('over\nseveral\nlines\n');


## Exercise 1

- Create two variables, room and seats and give each a value (whole numbers only)
>> year = 2014;
>> students = 85;
- Now use the 'fprintf' function to print out these numbers in a sentence.
- Your output should look like this:

In 2014, 85 people studied maths

## I just want some output!

- If this seems a little complicated you can always use disp()
- disp() doesn't need you to give format codes or a newline at the end
- You can only print one thing
>> disp(3.001)
>> disp('Good afternoon')


## Matrices

- A matrix is a rectangular grid containing numbers
- These can come in all sizes

$$
3 \times 1
$$

(or '3 by 1')
$4 \times 3$

| 49.1 |
| :---: |
| -18.6 |
| -80.2 |


| 7 | 12 | -3 |
| :---: | :---: | :---: |
| 4 | 6 | 8 |
| -8 | 0 | 1 |
| -21 | 2 | 19 |


| 4 | 3 | 1 | 2 |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  | $7 \times 1$ |  |  |
|  |  | 7 |  |

## Matrix sizes

- The size of an matrix is specified by the number of rows first, then the number of columns e.g. $5 \times 3$ (or '5 by 3')

3 columns

| 5 rows | 124 | -893 | 540 |
| :---: | :---: | :---: | :---: |
|  | 6 | 45 | -100 |
|  | 712 | 38 | 464 |
|  | 0 | 202 |  |
| 118 | -71 | 42 |  |

## Arrays

- You'll sometimes see these referred to as "arrays" as well
- The individual numbers in the array are referred to as "elements"


## Matrices in MATLAB

- Create a matrix using square brackets: >> $B=$ [7 12; $46 ;-80 ;-212]$



## Matrices in MATLAB

- Some more examples:
>> example_matrix $=\left[\begin{array}{lll}1 & 2 & 3 ; 4\end{array} 5\right.$ 6]
$\gg C=\left[\begin{array}{lll}8 & 7 & 6\end{array}\right]$
>> $D=[0 ; 4 ; 18 ; 22]$
- To make them simpler to type all these examples use whole numbers; but they don't have to!
>> $E=[0.00003$ 14.8; 12.7 1.8e2]


## Writing matrices

- A semicolon indicates a new row of the matrix
- Within a row, the elements can be separated by a comma or a space
>> $B=[7$ 12; $46 ;-80 ;-212]$ is equivalent to
$\gg B=[7,12 ; 4,6 ;-8,0 ;-21,2]$


## Matrices in MATLAB

- Each of these examples creates a new variable
- Our previous variables contained a single number, or some text
- These ones contain matrices


## Matrix size

- Now ask MATLAB what size of an array is >> size(B)
- This is specified as the number of rows, then the number of columns


## Exercise 2

- Create a new variable called $Z$ containing a matrix that looks like this:

| 24 | -83 | 54 |
| :---: | :---: | :---: |
| 6 | 45 | -10 |

- This is a $2 \times 3$ matrix
- Use size() to check this


## Vectors

- In MATLAB a vector is represented by a matrix which has either:
- only one row (a row vector) or
- only one column (a column vector)

Column vector

$$
\begin{gathered}
49.1 \\
-18.6 \\
-80.2
\end{gathered}
$$

Row vector


## Scalars

- A scalar is a single value
- In MATLAB, a scalar is treated as a $1 \times 1$ matrix

$$
\begin{aligned}
& \gg n=3 \\
& \gg \text { size }(n)
\end{aligned}
$$

- This is a $1 \times 1$ matrix, 1 row and 1 column


## Getting values out of a matrix

- We index a matrix by giving the row number, then the column number, of the element we want

$$
\begin{aligned}
& \text { >> } M=\left[\begin{array}{lllllllllll}
7 & 12 & -3 ; ~ & 6 & 8 ; & -8 & 0 & 1 ; ~-21 & 2 & 19
\end{array}\right] \\
& \gg M(2,3)
\end{aligned}
$$

| 7 | 12 | -3 | 1 |
| :---: | :---: | :---: | :---: |
| 4 | 6 | 8 | 2 |
| -8 | 0 | 1 | 3 |
| -21 | 2 | 19 | 4 |
| 1 | 2 | 3 |  |

## Exercise 3

- Work out the correct indexes to find the following numbers in the matrix M
- For example: to find -8
>> $M(3,1)$
- Now repeat this for 12, 19, and 0
- Remember if you want to see what M looks like, you can type:
>> disp(M)
or just
>> M


## Setting individual elements

- We can set an individual element of a matrix in a similar way
>> disp(M)
$\gg M(2,3)=1200$
>> disp(M)
and set it back again:
>> $M(2,3)=8$
>> disp(M)


## Indexing

- We can get more than one value out of a matrix (this is still called indexing)
- When it's used as an index, ':' means 'select all'
- Try these:
>> M(2,:)
>> M(: 3 )
- What's happening here?


## Selecting rows and columns

- 2,: means "second row, all columns", and
- :,3 means "all rows, third column"

| 7 | 12 | -3 | 1 |
| :---: | :---: | :---: | :---: |
| 4 | 6 | 8 | 2 |
| -8 | 0 | 1 | 3 |
| -21 | 2 | 19 | 4 |
| 1 | 2 | 3 |  |

## Exercise 4

- For M, how would you select this row?:

712 -3

- Again for M, select this column:

12
6
0
2

## Ranges in indexing

- You can also use : to select a range
- For example, try:

$$
\gg M(2,2: 3)
$$

## Ranges in indexing

- $M(2,2: 3)$ selects row 2 , and columns 2 to 3

| 7 | 12 | -3 | 1 |
| :---: | :---: | :---: | :---: |
| 4 | 6 | 8 | 2 |
| -8 | 0 | 1 | 3 |
| -21 | 2 | 19 | 4 |
| 1 | 2 | 3 |  |
|  |  |  |  |

- What we get is the part of row 2 in columns 2 and 3


## Ranges in indexing

- We can do this for columns and rows
>> M(2:4,1:2)

| 7 | 12 | -3 | 1 |
| :---: | :---: | :---: | :---: |
| 4 | 6 | 8 | 2 |
| -8 | 0 | 1 | 3 |
| -21 | 2 | 19 | 4 |
| 1 | 2 | 3 |  |

## Exercise 5

- For M, use this kind of indexing to select
$\begin{array}{rr}7 & 12 \\ 4 & 6\end{array}$ and then

$$
\begin{array}{rrr}
4 & 6 & 8 \\
-8 & 0 & 1
\end{array}
$$

## Comparison, True and False

- You can use == to compare numbers

$$
\begin{aligned}
& >2==2 \\
& >2==3
\end{aligned}
$$

- This is like asking a question, for example, "is 2 equal to 2?"
- The answer is given as 1 (true) or 0 (false)


## = VS. ==

- Setting a variable:
>> $n=2$ is a command:
"make n contain number 2"
- Comparison:
>> n == 2
asks a question:
"does n contain the number 2?"


## Comparison

- Conversely, ~= means "not equal to"
>> 61 ~= 61
>> 48 ~= - 99
- Wherever we use a number, we could also use a variable containing a number

$$
\begin{array}{ll}
\gg n=8 & \% \text { set } n \text { to } 8 \\
\gg n=40 & \% \text { does } n \text { equal } 40 ? \\
\gg n \sim=12 & \text { \% does } n \text { not equal } 12 ? \\
\gg n==8 & \% \text { does } n \text { equal } 8 ?
\end{array}
$$

## Comparison

- Similarly:

$$
\begin{aligned}
& \gg n=8 \quad \text { o set } n \text { to } 8 \\
& \ggg \ggg 12 \\
& \gg n<12 \\
& \gg n>=10 \\
& \ggg=8
\end{aligned}
$$

## Comparison

- The resulting True or False value can be stored, in the same way that we store the result of any other calculation
>> count $=15$
>> limit = 12
>> limit_passed = (count > limit)


## Exercise 6

- Use a comparison to check whether 299 times 134 is greater than 40000
- Now do the same, but first put the numbers into variables
>> $a=134 ;$
$\gg b=299 ;$
>> limit = 40000;


## Condition

- In general, a piece of code that tests something to see if it's true or false is referred to as a condition
- What can we use this for?


## if

- Assuming that 'a', 'b', and 'limit' are still defined from Exercise 6
- Type this:

$$
\begin{aligned}
& \text { >> if a*b > limit } \\
& \text { disp('over the limit!') } \\
& \text { end }
\end{aligned}
$$

- Note: you can press Return after the first line, MATLAB will realise that you have more to say

```
if a*b > limit
    disp('over the limit!')
end
```

- The value of the expression after the 'if' is computed a*b > limit
- If this condition is true, then the code between 'if' and 'end' is run
- Otherwise, we jump straight to the code after 'end'


## if

- Let's check what happens in the other case, when the condition is false
- Change something so that a*b > limit
is false
(for example, you could set 'limit' to 50000)
- Now run the 'if' code again:
if a*b > limit
disp('over the limit!')
end


## Code files

- So far we've only typed code in to the MATLAB prompt
- You can also type a sequence of commands into a file to make a MATLAB program
- This stores the instructions so you can edit them, and run them more than once
- Let's do that now ....


## .m file - Create

- Click on "New Script" in the top left of your MATLAB window
- In the window that appears, click "Save" (again, top left) and give the file a name ending in .m (as always, no spaces in the filename!)
- Notice that this window doesn't have the '>>' prompt
- In contrast to code typed on the prompt, the code you type in here won't run immediately


## .m files - Edit

- Now you're ready to edit your first MATLAB script
- When a script is run, all its lines of code are run in order
- This is the same as if you'd typed them all in again


## .m files - Edit

- Copy some simple code we've already run. Note: You don't need the prompt >> characters in the .m file!

```
a = 134;
b = 299;
limit = 40000;
if a*b > limit
    disp('over the limit!')
    end
```

- Click on "Save" to save the code


## .m files - Run

- To run the .m file, click "Run" (the green triangle icon at the top)
- The output from running the .m file will appear in the prompt window


## Running .m files

- Click on 'Run', and the name of the .m file (without .m extension) appears at the prompt
- The .m file can be run by typing this name at the prompt
- E.g. if your file was called limit_exercise.m, you could type:
>> limit_exercise
- Try it!


## Flow of control

- To be clear about what's happening, we can always add code to output some text
- Add a new line just before the 'if', like this: disp('starting') and another new line just after the 'end': disp('finishing')


## Testing

- Now run the program, and look at the output
- Change one of the inputs so that the condition will be false - for example, you could change the value of 'b' to zero
- Run it again and note how the output changes
- It's always worth testing every 'path' (possibility) in your code like this


## if-else

- Optionally, we can use 'else' to give some code to be run if the condition is false.

```
if a*b > limit
    disp('over the limit!')
else
    disp('under the limit!')
end
```

- Either
- 'a' times 'b' is greater than 'limit', and the first bit of code is run, or
- it is not, and the second is run.


## Another 'if' example

- Open a new code file, and save it under a different name to the first
- Type the following:

```
balance = 120;
if balance > 0
    fprintf('I owe you %d.\n',balance)
else
    fprintf('You owe me %d.\n',balance)
end
```

- Run the code
- Try changing the value of 'balance' and running it again (include some negative values for 'balance')


## Exercise 7

- What's wrong with the code, in particular when 'balance' is a negative number?
- What do you think could be done to correct it?
- Are there any values of 'balance' that the code doesn't deal with correctly?


## elseif

- What if you want to test more than one condition?

```
if balance > 0
    fprintf('I owe you %d.\n',balance)
else
    fprintf('You owe me %d.\n',balance)
end
```

- This doesn't behave correctly when balance is exactly zero ....


## elseif

- Change your code to read:
if balance == 0
fprintf('I owe you nothing\n')
elseif balance > 0
fprintf('I owe you \%d.\n',balance)
else
fprintf('You owe me \%d.\n',-balance) end


## elseif

- In general:
- Each of the conditions after the 'if' and subsequent 'elseif's are tested in order
- If one of them is true, then the corresponding code is run
- If none of these are true, the code after 'else' is run


## Combining conditions, and

- We can apply more than one condition at once with logical operators
- \& means 'and'
$\gg n=20$
$\gg m=-14$
$\gg n>10 \& m<0$
$\gg n>40 \& m<0$
$\gg \mathrm{n}>40 \& \mathrm{~m}==8$
- Both sides must be true for the result to be true


## Combining conditions, or

- | means 'or'
- This is the 'pipe' character
- This is either on the key next to 'z' or the key next to '1'
$\gg \mathrm{n}>10 \mid \mathrm{m}<0$
$\gg n>40 \mid m<0$
$\gg \mathrm{n}>40 \mid \mathrm{m}==8$
- If either side is true (or both) the result is true


## Combining conditions, not

- ~ means 'not'
- The tilde character is on the key next to Return
- Unlike the others, this only works on one value
$\gg n<0$
$\gg \sim(n<0)$
- It inverts the value (true to false, false to true)
- Why doesn't this do what we expect?
$\gg \sim n<0$


## Exercise 8

- In a new code file, write:
current_time = 14
- This is the hour ( 24 h clock, from 0 to 23 )
- Write something which displays:
- 'Good morning' if the time is between 3 and 12
- 'Good afternoon' if the time is between 13 and 18
- 'Good evening' if the time is between 19 and 22
- 'Good night' if the time is $0,1,2$, or 23
- Run this with a few different values of current_time


## Exercise 8, continued

- At the top of your file, add weekday $=4$
- This is the day of the week as a number
- 1 is Monday, 7 is Sunday
- Now change your program so that:
- On Saturday, we're informal and just say 'Hi' all day
- On Sunday, we don't say 'Good afternoon' until 14


## for

- 'if' allows us to choose between different code blocks
- What if we want to run the same code many times?
- We can use 'for' - try this at the prompt:
>> for $n=1: 10$
disp(n)
end


## for

- So, we know we can run for on a range of integers
-What else can we do?
- Try this again, but using different first lines:
for $n=10: 20$
for $n=\left[\begin{array}{llll}-20 & 49 & 62 & 1000\end{array}\right]$
for $n=0: 0.05: 1$


## 'for' loops

- This is a kind of loop
- The code inside the loop - in this case, just disp(n)
is run repeatedly, for each value given


## 'for' loops

- We could have any amount of code in the loop, though, e.g. (no need to type this):
for $n=1: 10$
$\mathrm{m}=\mathrm{n}+2$
fprintf('n is: \%d, m is: \%d\n',n,m)
end


## A digression about ranges

- This part of the 'for' code specifies a range:

1:10

- This isn't special code just used in 'for'
- It means 'an array with the numbers 1 to 10'


## A digression about ranges

- In general, a range looks like this: start:stop OR start:spacing:stop
- So for example, you could type: >> 0:2:10
which gives you an array, or
>> my_range = 0:2:10
to put this array into a variable


## Ranges and indexing

- This connects up with what we saw in indexing

D (1, 5:10) means 'the first row, columns five to ten' of $D$

## Exercise 9

- Show a nine times table (i.e. the first 12 multiples of 9)
- Use a 'for' loop, the * operator, and the disp() function


## MATLAB hates loops

- Most things we can do in a loop, we can just do to a whole array
- How do you think you might multiply the numbers 1 to 10 by 9, if not using a loop?


## MATLAB hates loops

- Try this:

$$
\begin{aligned}
& \gg X=1: 10 \\
& \gg X * 9
\end{aligned}
$$

- What happens when you try this:

$$
\text { >> 1:10* } 9
$$

- Why do you think this gives a different result?
-What can we do to correct it?


## MATLAB doesn't really hate loops

## but ....

- Avoiding loops can make code more concise
- Your intent is usually clearer, too


## Matrix operations

- As this shows, we can do maths on whole matrices
- Let's try this out with a small example:
$\gg B=\left[\begin{array}{lll}-2 & -8 ; & 4\end{array}\right]$
$\gg B+1$
$\gg B+10$
> B + 100


## Matrix operations

- As you can see, this adds the number you give to each of the elements of $Y$
- This works for other mathematical operations:
$\gg B-20$
$\gg \mathrm{B} . * 5$
>> B ./ 10
- We use .* and ./ here because * and / are reserved for other uses!


## Transpose

- A matrix can be transposed using an apostrophe ' after its name:
>> $B^{\prime}$
- Transposing flips the matrix so that the rows become columns (and the columns become rows)
- Note that the ' must be just after the matrix, without any spaces


## Transpose

- This is more obvious in non-square matrices:
$\gg G=\left[\begin{array}{lllllll}1 & 2 & 3 & 4 ; & 6 & 7 & 8\end{array}\right]$
>> G'
- Even without looking at the actual matrix, you can also see the effect on the size.
- The counts of rows and columns are swapped:
>> size(G)
>> size(G')


## Working with matrices

- We can also perform calculations with two matrices

$$
\begin{aligned}
& >A=[12 ; 31] \\
& >C=A+B
\end{aligned}
$$

- The equivalent mathematical notation:

$$
\left(\begin{array}{ll}
1 & 2 \\
3 & 4
\end{array}\right)+\left(\begin{array}{cc}
-2 & -8 \\
9 & 4
\end{array}\right)=\left(\begin{array}{cc}
-1 & -6 \\
12 & 8
\end{array}\right)
$$

## Maths with two matrices

- Similarly, for subtraction:

$$
\begin{aligned}
>D= & A-B \\
& \left(\begin{array}{ll}
1 & 2 \\
3 & 4
\end{array}\right)-\left(\begin{array}{cc}
-2 & -8 \\
9 & 4
\end{array}\right)=\left(\begin{array}{cc}
3 & 10 \\
-6 & 0
\end{array}\right)
\end{aligned}
$$

## Matrix multiplication

- Careful with *
- . means "multiply individual elements" (referred to as elementwise multiplication)
$>\mathrm{E}=\mathrm{A} . * \mathrm{~B}$
-     * means "matrix multiplication"
$>P=A * B$


## Matrix "division"

- Similarly with /
- ./ means "divide individual elements" (elementwise division)
- There's no such thing as matrix "division", but:
> A / B matrix-multiplies $A$ by the inverse of $B$
- In MATLAB we would write this:
>> A * inv(B)


## Joining matrices together

- We can concatenate matrices the same way we make them from numbers
- Recall that, for example
[1, 2, 3]
puts numbers in a row, and
[1; 2; 3]
puts them in a column


## Joining matrices together

- Try these:
$\gg \mathrm{A}, \mathrm{B}]$
$>$ [A; B]
- As you might expect,
$\gg$ [A, B]
joins (or concatenates) horizontally, and >> [A; B]
joins vertically


## Joining matrices together

- For this to work the matrices must be the right shape
- To join horizontally, they must have the same number of rows
- To join vertically, they must have the same number of columns
- Thinking of matrices as tables, the side on which they are joined must be the same size


## Joining matrices together

- Joining horizontally:

| 24 | -83 | 54 |
| :---: | :---: | :---: |
| 6 | 45 | -10 |$\quad$| -3 | 42 |
| :---: | :---: |
| 16 | 0 |$\rightarrow$| 24 | -83 | 54 | -3 | 42 |
| :---: | :---: | :---: | :---: | :---: |
| 6 | 45 | -10 | 16 | 0 |

but joining these vertically does not work:

$$
\begin{array}{|c|c|c|}
\hline 24 & -83 & 54 \\
\hline 6 & 45 & -10 \\
\hline \begin{array}{|c|c|}
\hline-3 & 42 \\
\hline 16 & 0 \\
\hline
\end{array}
\end{array}
$$

## Exercise 10

- Here are four matrices in MATLAB notation
- Find all the combinations in which they can be joined together vertically or horizontally

$$
\begin{aligned}
& \gg W=[123 ; 456 ; 789 ; 000] \\
& >X=\left[\begin{array}{llll}
24 & -83 & 54 ; & 65
\end{array}\right] \\
& \gg Y=[-342 ; 160] \\
& \text { >> } Z=[N a N ;-I n f]
\end{aligned}
$$

## Matrix functions: diag

- Taking an example $3 \times 3$ matrix:

$$
\text { >> D = [-1 } 43 \text { 37; -10 } 52 \text { 32; } 30 \text {-44 }-67]
$$

- We can take the diagonal of D using diag(): >> diag(D)
- This gives the numbers from the top-left of $D$ in a diagonal line
- To put it another way, it's the same as:

$$
\gg[D(1,1) \quad D(2,2) \quad D(3,3)]
$$

## Matrix functions: triu, tril

- The triu and tril functions return the upper and lower triangular parts of a matrix
>> triu(D)
>> tril(D)
- These give the diagonal plus everything above it (upper) or below it (lower)


## Matrix functions, sum

- The sum() function gives the sum along rows or columns
- Sum of columns:
$\gg \operatorname{sum}(D, 1)$
- Sum of rows:
$\gg \operatorname{sum}(D, 2)$


## Vector dot product

- The $\operatorname{dot}()$ function gives the vector dot product

$$
\begin{aligned}
& \gg U=\left[\begin{array}{lll}
-1 & 43 & 37
\end{array}\right] \\
& \gg V=\left[\begin{array}{lll}
-10 & 52 & 32
\end{array}\right] \\
& \gg \operatorname{dot}(U, V)
\end{aligned}
$$

## Vector dot product

- We can check this using some of what we've already learned:
>> products = U.*V
$\gg$ sum(products, 2)
- Also note that this is the same as:
>> U*V'


## repmat

- The repmat() function replicates a matrix to create a larger one
- It's used like this:
repmat(M,[row col]) where:
- M is the matrix to be replicated
- row is the number of "rows of M "
- col is the number of "columns of M "


## Example

- Try this:
$\gg M=\left[\begin{array}{llll}1 & 4 ; & 16]\end{array}\right.$
>> repmat(M, [2 3])
- You'll see that $M$ is repeated:
- twice vertically (two "rows of M")
- three times horizontally (three "columns of M")


## Exercise 11

- Define the following vectors:
>> $X=$ [1; 2; 3]
$\gg Y=\left[\begin{array}{lll}-4 & -5 & -6\end{array}\right]$
- Using repmat() on $X$, make a 3 by 3 matrix
- Using repmat() on Y, make a 5 by 6 matrix (Remember: if you want can use the size() function to check the size of a matrix, rather than counting rows and columns on the screen)


## Creating matrices

- We already know how to create a matrix with specific, different values in it, e.g.:

$$
\text { >> D = [-1 } 43 \text { 37; -10 } 52 \text { 32; 30 -44 -67] }
$$

- There are some other special functions that allow us to create matrices


## ones

- The "ones" function creates a matrix consisting only of ones
- Following the usual convention, it takes a number of rows, and a number of columns
- e.g. to create a $4 \times 3$ matrix:
>> ones(4,3)


## zeros

- Similar to ones() this creates a matrix consisting only of zeros
- e.g. to create a $2 \times 8$ matrix of zeros: >> zeros(2,8)


## Identity matrix, eye()

- The "eye" function creates an identity matrix
- Identity matrixes are always square, so it only takes one number (which is both the number of rows and of columns)
- e.g. to create a 5 by 5 identity matrix: >> eye(5)


## Exercise 12

- Using the ones() function, and what we've already learned about arithmetic with matrices, how would you quickly create:
- a 6 by 3 matrix
- where every element of the matrix is 12 ?


## Plotting

- We can plot a line simply with the "plot" function
- This takes an array of $X$ values and an array of $Y$ values, e.g.
>> $X=\left[\begin{array}{llll}1 & 2 & 4 & 5\end{array}\right] ;$
>> $Y$ = [-6 8 7 3 -1];
>> figure
>> plot(X, Y)


## Changing plot colours and style

- We can specify the colour and style of the line (or points)
- e.g.

$$
\begin{aligned}
& \text { >> plot }(X, Y, \quad \text { 'r') } \\
& \text { >> plot }\left(X, Y, ~ ' g x^{\prime}\right) \\
& \gg \operatorname{plot}\left(X, Y, ' b-l^{\prime}\right)
\end{aligned}
$$

- There are lots of possibilities
- See the documentation for "plot" for more details


## Adding some annotations

- We can add a title, and labels for the x and y axes
>> title('My example graph')
>> xlabel('time (days)')
>> ylabel('temperature (deg C)')


## Changing the x and y range

- We can use the axis() function to give the limits for the plot
- These are given in a list:
x start, x end, y start, y end
- e.g.
axis([0 $\left.\left.\begin{array}{llll}10 & -9 & 9\end{array}\right]\right)$


## Plotting multiple lines

- You can plot multiple lines on the same chart
- Try this:

$$
\begin{aligned}
& \gg Y 2=\left[\begin{array}{lllll}
2 & 4 & -7 & 6 & 4
\end{array}\right] ; \\
& \gg \text { plot }(X, Y, ' r--', X, Y 2, ' b v ')
\end{aligned}
$$

## Functions

- We can write our own functions, which we can then use just like built-in functions:
- our own functions will take a number of parameters (or none!)
- and can also return (i.e. give back) a value


## Functions

- Functions allow you to store a set of instructions and run them on different values, for example:
function [result] = add_two(n) result = n+2; end


## Function in a .m file

- Functions must be defined in .m files
- The file has the same name as the function
- Open a new .m file, this time by clicking New -> Function
- This opens a template for a function


## Function in a .m file

- Edit the template to look like this: function [result] = add_two(n) result = n+2; end
- Save the file
- You'll find that MATLAB suggests the correct filename, which is the function name (and .m)


## Running your function

- Now run your function:

$$
\begin{aligned}
& \text { >> add_two }(3) \\
& \gg \text { add_two }(-42) \\
& \gg \text { add_two }(0)
\end{aligned}
$$

## Function naming

- The rules for creating names are the same as for variables
- Reminder:
- Names must start with a letter, and can contain letters, numbers and underscores
- Names are case sensitive
- They can't contain spaces


## How a function is defined

- A function definition:

Name of return value
Name of function


Function body

## How a function is called

- Reminder:
- A function is called with its name, followed by the parameters in brackets:
>> add_two (8)


## What happens when a function is called

- The instructions in the function are followed from the top to the end
- Values are then given back (returned) to the point where it was called
- The values returned are the ones specified at the top of the function (in our example above this is "result")


## Function with no return value

- A function doesn't have to return anything
- If it doesn't, then the first line changes
- For example, a function like this:
function [result] = my_function(n) without a return value would be:
function my_function(n)


## Another example function

- Open another .m file with New -> Function
- Edit the template to look like this: function [string_out] = greeting(to_greet)
string_out $=[$ 'Hello ', to_greet]; end
- Save this (as greeting.m)


## An aside on joining strings

- MATLAB treats strings like arrays
- The same way we can do this:
$\left.\begin{array}{l}\text { >> } V=\left[\begin{array}{llll}1 & 2 & 3 & 4\end{array}\right] ; \\ \gg \\ \gg \\ >\end{array}\right]=\left[\begin{array}{llll}5 & 6 & 7 & 8\end{array}\right] ;$
we can also do this:
>> g = 'Hello '
>> n = 'Edinburgh'
>> [ g n]


## Another example function

- Now run the function
>> x = greeting('you');
- What is in x now? Have a look ....
- Try this out with a few values
>> disp(greeting('Edinburgh'));
- Quick exercise: can you give the function a value that causes an error?


## Exercise 13

- Open another .m file, to write another function
- This will take a string as a parameter, like the "greeting" function
- We want our new function to do this:
>> greet_and_count('Anna')
Hello Anna
Your name has 4 letters
>> greet_and_count('Andrew') Hello Andrew
Your name has 6 letters


## Exercise 13, clues

- You can call the greeting() function from your new function
- You'll need fprintf()
- You'll also need the length() function which can measure the length of a string


## Exercise 13, questions

- Are there any input values that cause an error?
- Are there any input values that cause "wrong" (or wrong-looking) output?


## Exercise 14

- Change your function to do something sensible:
- when the input is only one character long
- when the input is empty
- These inputs would look like this:
>> greet_and_count('B') >> greet_and_count('')
- You'll need to use if .... elseif .... end


## Exercise 15

- Start a new function called bars()
- It should take a row vector as input
- For each number in the vector, in order, it should show that number of '*' on a line
- For example:

```
    >> bars([11 6 2 4])
*
******
**
****
```


## Exercise 15, clues

- You'll need to use a for ... end loop to work through the input vector
- You can use repmat to copy strings, e.g.: >> repmat('moo ', [1 20])
(if this seems confusing try it for a few different values)


## Function example

- Download example_function.m from the usual place (short link: http://edin.ac/1y1Pd7K)

```
function [result] = example_function(M)
    tl = M(1,1);
    tr = M(1,end);
    bl = M(end,1);
    br = M(end,end);
    if tl == tr & tl == bl & tl == br
    result = 1;
    else
        result = 0;
    end
end
```


## Indexing note

- As an index, "end" always means the last thing
- So, M(3,end) means the element in the third row, and last column of M
- This can be used in ranges e.g.
>> M(4:6, 2:end)


## Exercise 16

- This is more of a thought exercise!
- It's important to come up with good further questions to ask, as well as answers ....
-What do you think this function does? (feel free to try it out)
- Can you think of a good name for it?


## The "return" keyword

- This stops a function from running any further
- No more instructions in the function are carried out
- The values specified at the top of the function are returned


## Early return

- Let's say we want our function to complain if it's given a matrix with less than 2 rows, or less than 2 columns
- In this case we'll return NaN (this is a common way to say "didn't work" in MATLAB)
- Let's break this problem down a little


## Exercise 17

- Open a code file
- Write this:
function [result] = less_than_2_by_2(M) end
- Add code between these lines, so that:
- if M has less than 2 rows, or less than 2 columns, the function returns 1
- otherwise, it returns 0


## Exercise 18

- Go back to the function in the last exercise
- At the start of the function, add some code to return early (returning NaN ) if the input matrix is smaller than 2 by 2
- Use "f", and the less_than_2_by_2 function


## Even or odd?

- Save this code as even.m function [is_odd] = odd(n) return $\bmod (n, 2)$ end
- This returns 0 if a number is even and 1 if it is odd
- Try it out
(Note: the mod() function calculates remainders - see documentation for details)


## Exercise 19

- Open a new .m file
- Write a function called odd_count() that
- takes a row vector as its only parameter
- returns the number of odd numbers in the vector
- Try it on some examples
>> odd_count([ $\left.\left.\begin{array}{llll}1 & 2 & 3 & 4\end{array}\right]\right)$
>> odd_count([ -12 -9 -7 -5 11066$])$

