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**informatics**

# Embedded Systems

## Lecture 9: Reliability & Fault Tolerance

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# Overview

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- Definitions
- System Reliability
- Fault Tolerance

# Sources and Detection of Errors

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Stage	Error Sources	Error Detection
Specification & Design	Algorithm Design Formal Specification	Consistency Checks Simulation
Prototype	Algorithm Design Wiring & Assembly Timing Component Failure	Stimulus/Response Testing
Manufacture	Wiring & Assembly Component Failure	System Testing Diagnostics
Installation	Assembly Component Failure	System Testing Diagnostics
Field Operation	Component Failure Operator Errors Environmental Factors	Diagnostics

# Definitions

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- **Reliability:** Survival Probability
  - When function is critical during the mission time.
- **Availability:** The fraction of time a system meets its specification.
  - Good when continuous service is important but it can be delayed or denied
- **Failsafe:** System fails to a known safe state
- **Dependability:** Generalisation - System does the right thing at right time

# System Reliability

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- The reliability,  $R_F(t)$  of a system is the probability that no fault of the class  $F$  occurs (i.e. system survives) during time  $t$ .

$$R_F(t) = P(t_{init} \leq t < t_f \forall f \in F)$$

where  $t_{init}$  is time of introduction of the system to service,  
 $t_f$  is time of occurrence of the first failure  $f$  drawn from  $F$ .

- Failure Probability,  $Q_F(t)$  is complementary to  $R_F(t)$

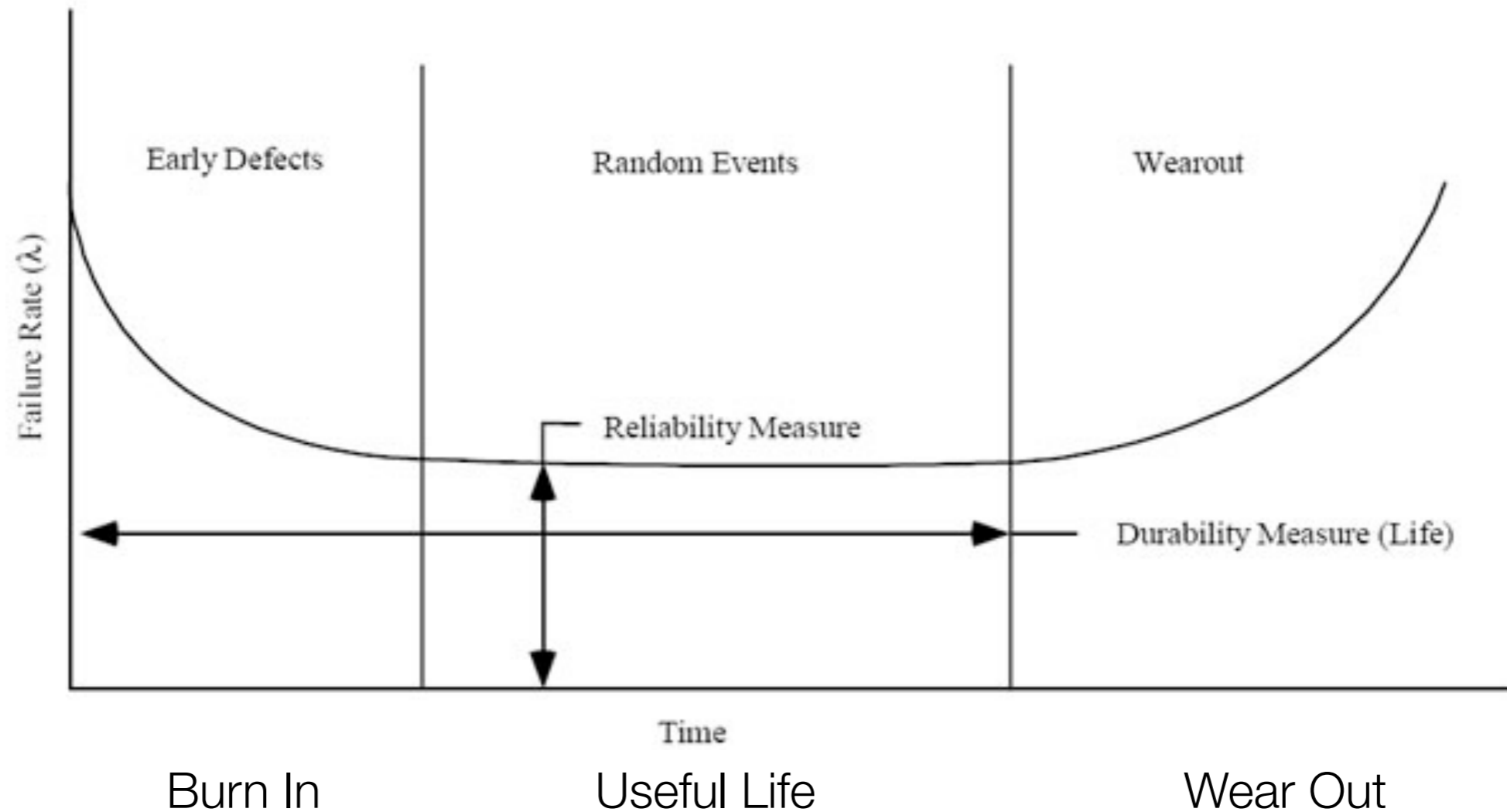
$$R_F(t) + Q_F(t) = 1$$

- We can take off the  $F$  subscript from  $R_F(t)$  and  $Q_F(t)$

- When the lifetime of a system is exponentially distributed, the reliability of the system is:  $R(t) = e^{-\lambda t}$  where the parameter  $\lambda$  is called the failure rate

# Component Reliability Model

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During useful life, components exhibit a constant failure rate  $\lambda$ . Reliability of a device can be modelled using an exponential distribution  $R(t) = e^{-\lambda t}$

# Component Failure Rate

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- Failure rates often expressed in failures / million operating hours

Automotive Embedded System Component	Failure Rate $\lambda$
Military Microprocessor	0.022
Typical Automotive Microprocessor	0.12
Electric Motor Lead/Acid battery	16.9
Oil Pump	37.3
Automotive Wiring Harness (luxury)	775

# MTTF: Mean Time To Failure

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- **MTTF:** Mean Time to Failure or Expected Life
- **MTTF:** Mean Time To (first) Failure is defined as the expected value of  $t_f$

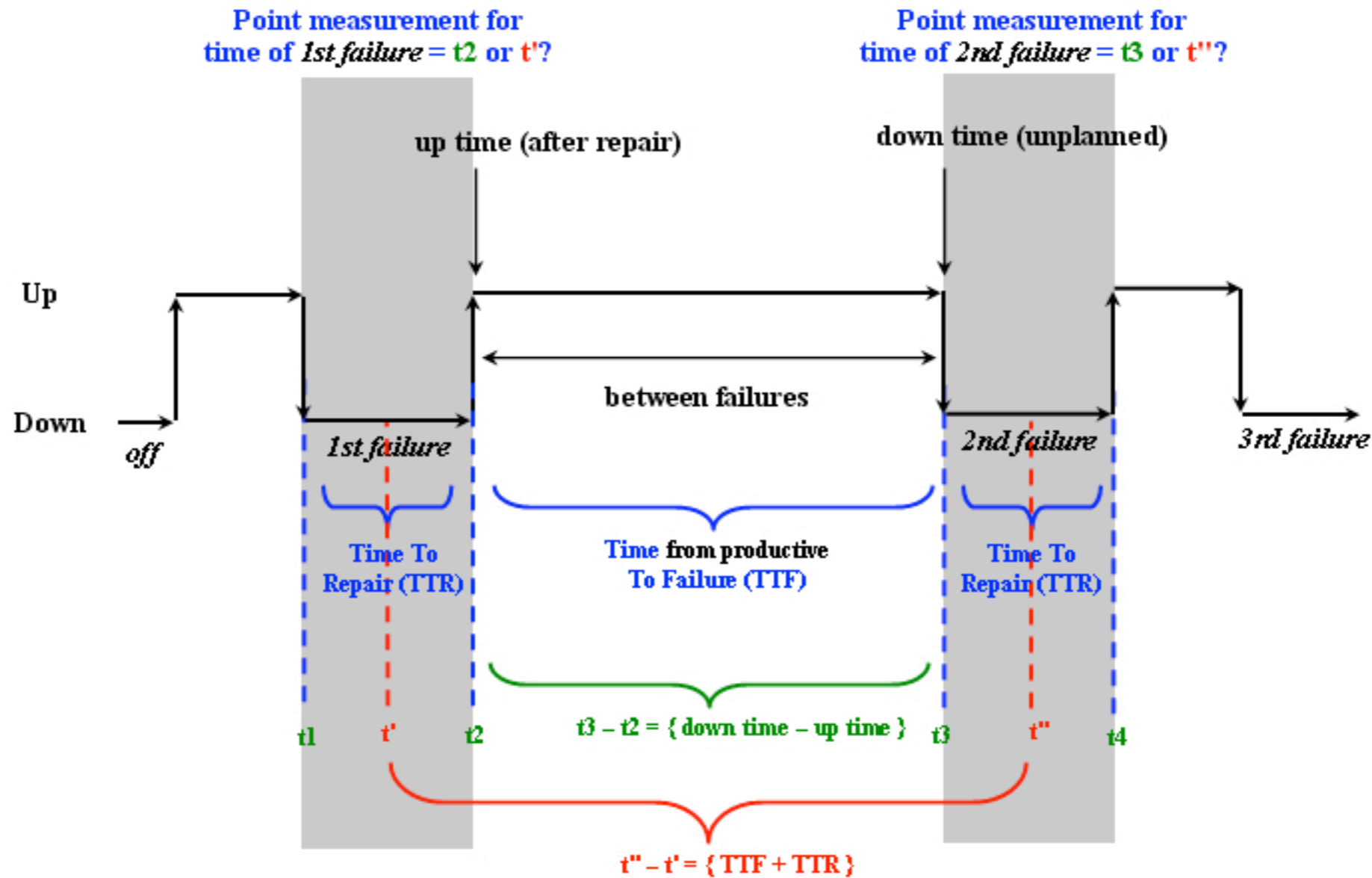
$$MTTF = E(t_f) = \int_0^{\infty} R(t) dt = \frac{1}{\lambda}$$

where  $\lambda$  is the failure rate.

- **MTTF** of a system is the expected time of the first failure in a sample of identical initially perfect systems.
- **MTTR:** Mean Time To Repair is defined as the expected time for repair.
- **MTBF:** Mean Time Between Failure



# MTTF - MTTR - MTBF



Time Between Failures = Time between 1st failure and 2nd failure

**Availability =**  
**MTBF / (MTBF + MTTR)**

= (time of 2nd failure) - (time of 1st failure)  
 =  $t_3 - t_2$  ?  
 =  $t'' - t'$  ?

# Serial System Reliability

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- Serially Connected Components

- $R_k(t)$  is the reliability of a single component  $k$ :  $R_k(t) = e^{-\lambda_k t}$

- Assuming the failure rates of components are statistically independent.

- The overall system reliability  $R_{ser}(t)$

$$R_{ser}(t) = R_1(t) \times R_2(t) \times R_3(t) \times \dots \times R_n(t)$$

$$R_{ser}(t) = \prod_{i=1}^n R_i(t)$$

- No redundancy: Overall system reliability depends on the proper working of each component

$$R_{ser}(t) = e^{-t(\sum_{i=1}^n \lambda_i)}$$

- Serial failure rate

$$\lambda_{ser} = \sum_{i=1}^n \lambda_i$$

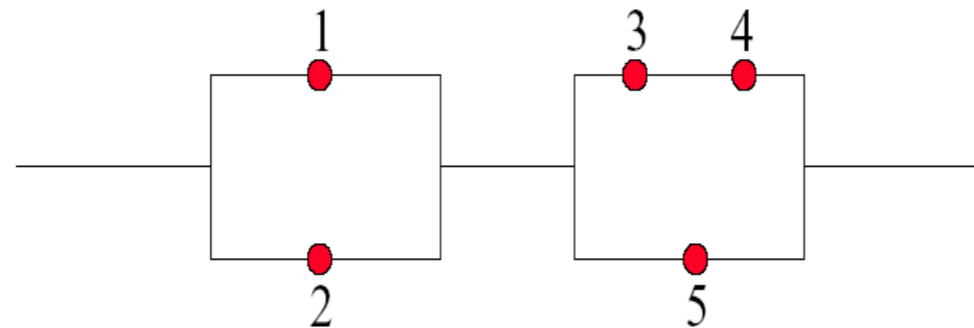
# System Reliability

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- Building a reliable serial system is extraordinarily difficult and expensive.
- For example: if one is to build a serial system with 100 components each of which had a reliability of 0.999, the overall system reliability would be

$$0.999^{100} = 0.905$$

- Reliability of System of Components



- Minimal Path Set:  
Minimal set of components whose functioning ensures the functioning of the system: {1,3,4} {2,3,4} {1,5} {2,5}

# Parallel System Reliability

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- Parallel Connected Components

- $Q_k(t)$  is  $1 - R_k(t)$ :  $Q_k(t) = 1 - e^{-\lambda_k t}$

- Assuming the failure rates of components are statistically independent.

$$Q_{par}(t) = \prod_{i=1}^n Q_i(t)$$

- Overall system reliability:  $R_{par}(t) = 1 - \prod_{i=1}^n (1 - R_i(t))$

# Example

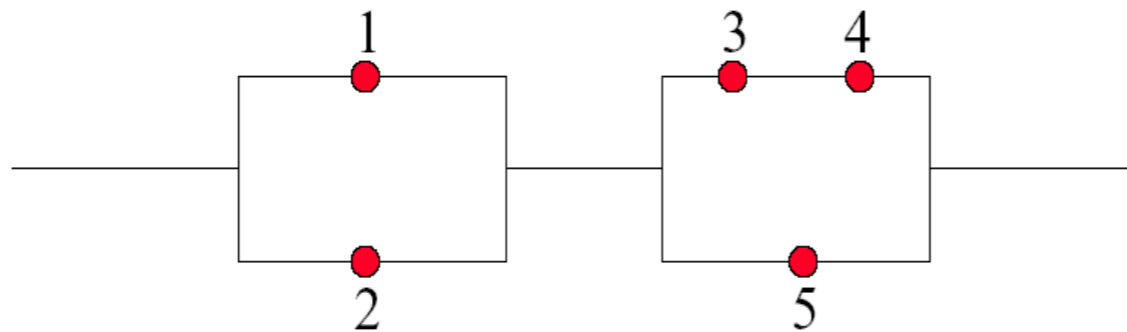
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- Consider 4 identical modules are connected in parallel
- System will operate correctly provided at least one module is operational. If the reliability of each module is 0.95.
- The overall system reliability is  $1 - (1 - 0.95)^4 = 0.99999375$

# Parallel-Serial Reliability

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- Parallel and Serial Connected Components



- Total reliability is the reliability of the first half, in serial with the second half.
- Given  $R_1=0.9$ ,  $R_2=0.9$ ,  $R_3=0.99$ ,  $R_4=0.99$ ,  $R_5=0.87$
- $R_t = (1 - (1 - 0.9)(1 - 0.9))(1 - (1 - 0.87)(1 - (0.99 \times 0.99))) = 0.987$

# Faults and Their Sources

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- What is a fault?

Fault is an erroneous state of software or hardware resulting from failures of its components

- Fault Sources

- Design errors

- Manufacturing Problems

- External disturbances

- Harsh environmental conditions

- System Misuse

# Fault Sources

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- Mechanical -- “wears out”
  - Deterioration: wear, fatigue, corrosion
  - Shock: fractures, overload, etc.
- Electronic Hardware -- “bad fabrication; wears out”
  - Latent manufacturing defects
  - Operating environment: noise, heat, ESD, electro-migration
  - Design defects
- Software -- “bad design”
  - Design defects
  - “Code rot” -- accumulated run-time faults
- People
  - Can take a whole lecture content...



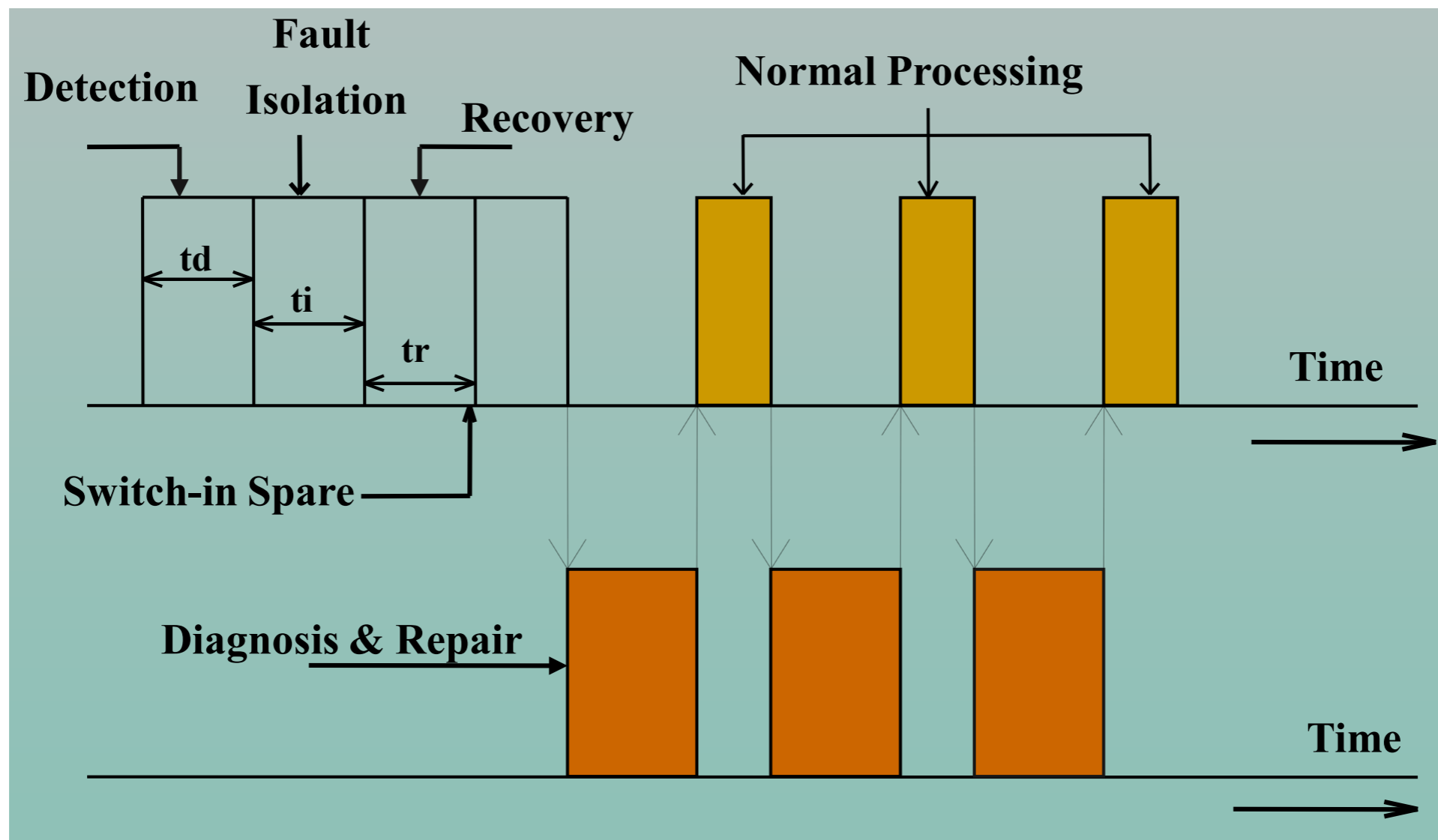
# Fault and Classifications

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- **Failure:** Component does not provide service
- **Fault:** A defect within a system
- **Error:** A deviation from the required operation of the system or subsystem
- **Extent:** Local (independent) or Distributed (related)
- **Value:**
  - Determinate
  - Indeterminate (varying values)
- **Duration:**
  - Transient
  - Intermittent
  - Permanent

# Fault-Tolerant Computing

- Main aspects of Fault Tolerant Computing (FTC): Fault detection, Fault isolation and containment, System recovery, Fault Diagnosis Repair



# Tolerating Faults

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- There is four-fold categorisation to deal with the system faults and increase system reliability and/or availability.
- Methods for Minimising Faults
  - **Fault Avoidance:** How to prevent the fault occurrence. Increase reliability by conservative design and use high reliability components.
  - **Fault Tolerance:** How to provide the service complying with the specification in spite of faults having occurred or occurring.
  - **Fault Removal:** How to minimise the presence of faults.
  - **Fault Forecasting:** How to estimate the presence, occurrence, and the consequences of faults.
- Fault-Tolerance is the ability of a computer system to survive in the presence of faults.

# Fault-Tolerance Techniques

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- Hardware Fault Tolerance
- Software Fault Tolerance

# Hardware Fault-Tolerance Techniques

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- Fault Detection
- Redundancy (masking, dynamic)
  - Use of extra components to mask the effect of a faulty component. (Static and Dynamic)
  - Redundancy alone does not guarantee fault tolerance. It guarantee higher fault arrival rates (extra hardware).
- Redundancy Management is Important
  - A fault tolerant computer can end up spending as much as 50% of its throughput in managing redundancy.

# Hardware Fault-Tolerance: Fault Detection

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- Detection of a failure is a challenge
  - Many faults are latent that show up later
- Fault detection gives warning when a fault occurs.
  - Duplication: Two identical copies of hardware run the same computation and compare each other results. When the results do not match a fault is declared.
  - Error Detecting Codes: They utilise information redundancy

# Hardware Fault-Tolerance: Redundancy

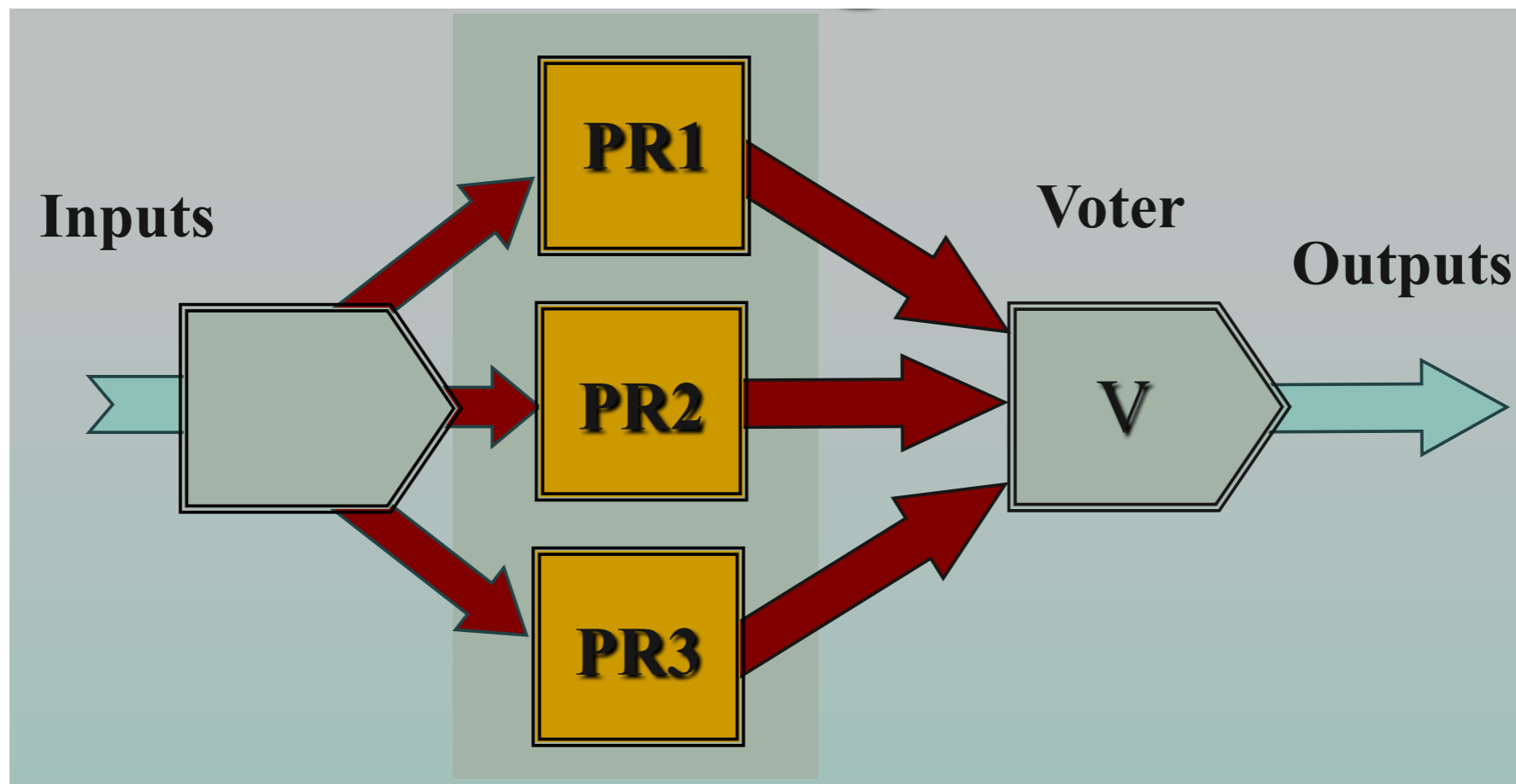
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- Static and Dynamic Redundancy
- Extra components mask the effect of a faulty component.
- Masking Redundancy  
Static redundancy as once the redundant copies of an element are installed, their interconnection remains fixed e.g. N-tuple modular redundancy (nMR), ECC, TMR (Triple Modular Redundancy) 3 identical copies of modules provide separate results to a voter that produces a majority vote at its output.
- Dynamic Redundancy System configuration is changed in response to faults. Its success largely depends upon fault detection ability.

# TMR Configuration

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- PR1, PR2 and PR3 processors execute different versions of the code for the same application.
- Voter compares the results and forward the majority vote of results (two out of three).





# Software Fault-Tolerance

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- Hardware based fault-tolerance provides tolerance against physical i.e. hardware faults.
- How to tolerate design/software faults?  
It is virtually impossible to produce fully correct software.
- We need something:
  - To prevent software bugs from causing system disasters. To mask out software bugs.
  - Tolerating unanticipated design faults is much more difficult than tolerating anticipated physical faults.
- Software Fault Tolerance is needed as:
  - Software bugs will occur no matter what we do. No fully dependable way of eliminating these bugs. These bugs have to be tolerated.

# Tolerating Software Failures

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- How to Tolerate Software Faults?

Software fault-tolerance uses design redundancy to mask residual design faults of software programs.

- Software Fault Tolerance Strategy

- Defensive Programming

- If you can not be sure that what you are doing is correct.
- Do it in many ways.
- Review and test the software.
- Verify the software.
- Execute the specifications.
- Produce programs automatically.

# SW Fault-Tolerance Techniques

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- Software Fault-tolerance is based on HW Fault-tolerance
- Software Fault Detection is a bigger challenge
  - Many software faults are of latent type that shows up later.
  - Can use a watchdog to figure out if the program is crashed
- Change the specification to provide low level of service
- Write new versions of the software
  - Throw the original version away. Use all the versions and vote the results.  
N-version Programming (NVP)
- Use an on-line acceptance test to determine which version to believe.  
Recovery Block Scheme.

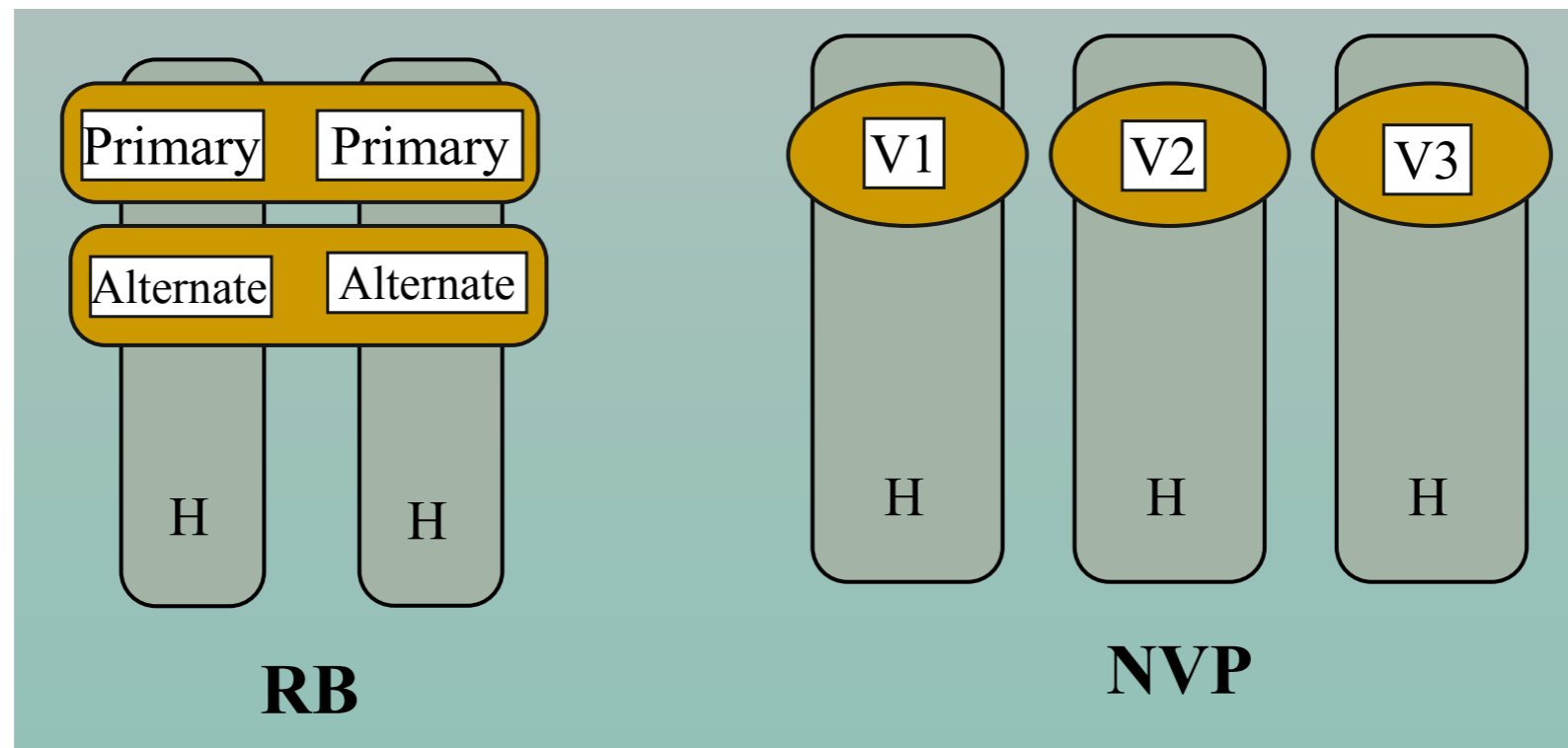
# Fault-tolerant Software Design Techniques

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- Recovery block scheme (RB)  
Dynamic redundancy
- N-version programming scheme (NVP)  
n-modular redundancy
- Hardware redundancy is needed to implement the above Software Fault-tolerance techniques.

# Fault-tolerant Software Design Techniques

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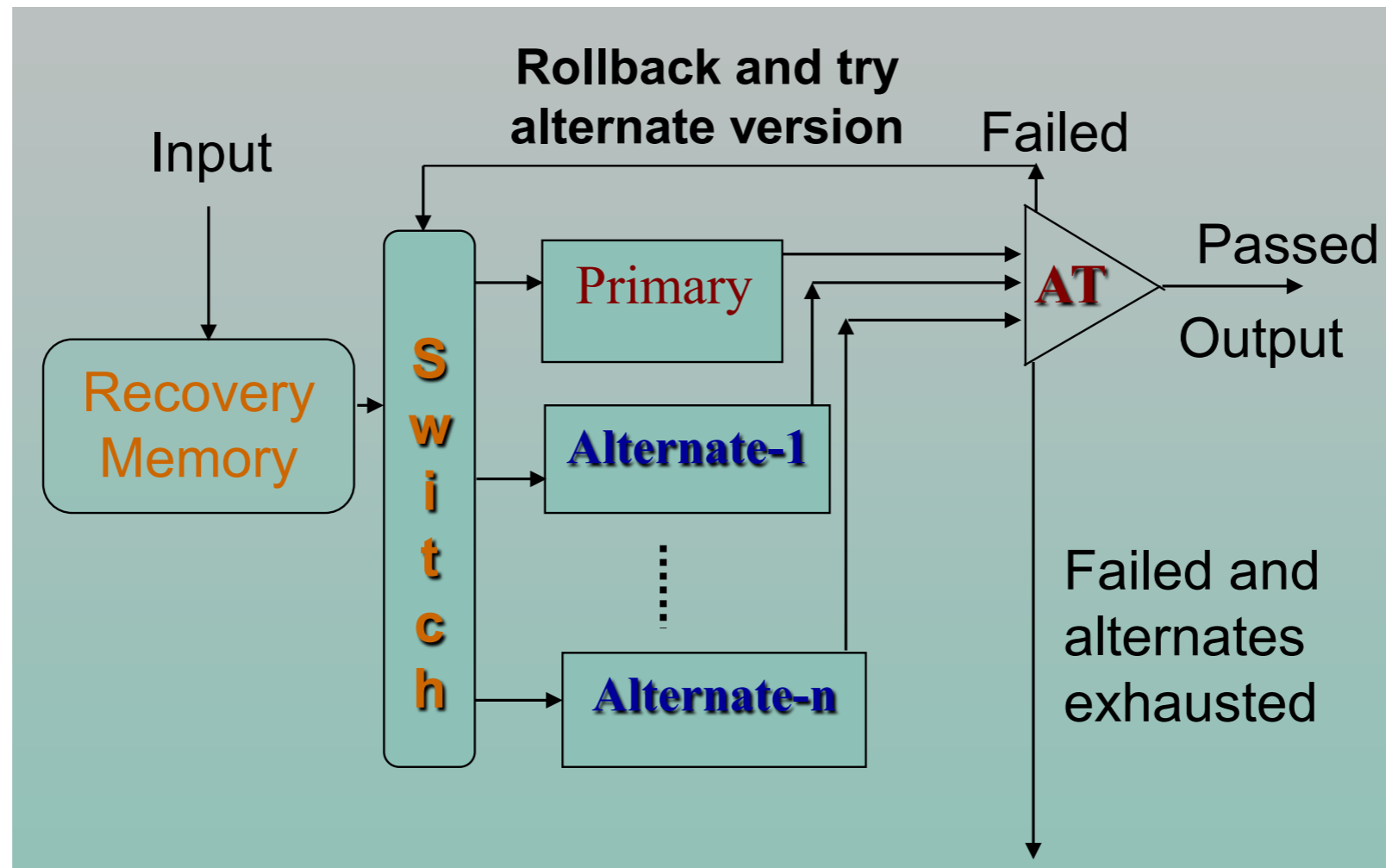


RB Scheme comprises of three elements:  
A primary module to execute critical software functions.  
Acceptance test for the output of primary module. Alternate modules perform the same functions as of primary.

N-independent program variants execute in parallel on the identical input. Results are obtained by voting upon the output of individual programs

# Recovery Block Scheme

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RB uses diverse versions.  
Attempt to prevent residual software faults

# Fault Recovery

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- Fault recovery technique's success depends on the detection of faults accurately and as early as possible.
- Three classes of recovery procedures:
  - Full Recovery  
It requires all the aspects of fault tolerant computing.
  - Degraded recovery: Also referred as graceful degradation. Similar to full recovery but no subsystem is switched-in.
    - Defective component is taken out of service.
    - Suited for multiprocessors.
  - Safe Shutdown

# Fault Recovery

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- Two Basic Approaches:
  - Forward Recovery
    - Produces correct results through continuation of normal processing.
    - Highly application dependent
  - Backward Recovery
    - Some redundant process and state information is recorded with the progress of computation.
    - Rollback the interrupted process to a point for which the correct information is available.
    - e.g. Retry, Checkpointing, Journaling



# Summary

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- Reliability
  - Serial Reliability, Parallel Reliability, System Reliability
- Fault Tolerance
  - Hardware, Software

# Preview

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- Scheduling Theory
  - Priority Inversion
  - Priority Inheritance Protocol