Embedded Systems
Lecture 9: Reliability & Fault Tolerance

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Overview

- Definitions
- System Reliability
- Fault Tolerance
# Sources and Detection of Errors

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Definitions

• **Reliability**: Survival Probability
  
  - When function is critical during the mission time.

• **Availability**: The fraction of time a system meets its specification.
  
  - Good when continuous service is important but it can be delayed or denied

• **Failsafe**: System fails to a known safe state

• **Dependability**: Generalisation - System does the right thing at right time
System Reliability

- The reliability, $R_F(t)$ of a system is the probability that no fault of the class $F$ occurs (i.e. system survives) during time $t$.

$$R_F(t) = P(t_{\text{init}} \leq t < t_f \forall f \in F)$$

where $t_{\text{init}}$ is time of introduction of the system to service, $t_f$ is time of occurrence of the first failure $f$ drawn from $F$.

- Failure Probability, $Q_F(t)$ is complementary to $R_F(t)$

$$R_F(t) + Q_F(t) = 1$$

- We can take off the $F$ subscript from $R_F(t)$ and $Q_F(t)$

- When the lifetime of a system is exponentially distributed, the reliability of the system is: $R(t) = e^{-\lambda t}$ where the parameter $\lambda$ is called the failure rate
Component Reliability Model

During useful life, components exhibit a constant failure rate $\lambda$. Reliability of a device can be modelled using an exponential distribution $R(t) = e^{-\lambda t}$.
## Component Failure Rate

- Failure rates often expressed in failures / million operating hours

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<th>Automotive Embedded System Component</th>
<th>Failure Rate $\lambda$</th>
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<td>Military Microprocessor</td>
<td>0.022</td>
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<td>Typical Automotive Microprocessor</td>
<td>0.12</td>
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<tr>
<td>Electric Motor Lead/Acid battery</td>
<td>16.9</td>
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<tr>
<td>Oil Pump</td>
<td>37.3</td>
</tr>
<tr>
<td>Automotive Wiring Harness (luxury)</td>
<td>775</td>
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MTTF: Mean Time To Failure

- **MTTF**: Mean Time to Failure or Expected Life

- **MTTF**: Mean Time To (first) Failure is defined as the expected value of $t_f$ where $\lambda$ is the failure rate.

$$MTTF = E(t_f) = \int_0^\infty R(t)dt = \frac{1}{\lambda}$$

where $\lambda$ is the failure rate.

- **MTTF** of a system is the expected time of the first failure in a sample of identical initially perfect systems.

- **MTTR**: Mean Time To Repair is defined as the expected time for repair.

- **MTBF**: Mean Time Between Failure
MTTF - MTTR - MTBF

Availability = \frac{MTBF}{MTBF + MTTR}

= (\text{time of 2nd failure}) - (\text{time of 1st failure})
= t_3 - t_2 \ ?
= t'' - t' \ ?
Serial System Reliability

• Serially Connected Components

\( R_k(t) \) is the reliability of a single component \( k \): 
\[
R_k(t) = e^{-\lambda_k t}
\]

• Assuming the failure rates of components are statistically independent.

• The overall system reliability \( R_{ser}(t) \)

\[
R_{ser}(t) = R_1(t) \times R_2(t) \times R_3(t) \times \ldots \times R_n(t)
\]

\[
R_{ser}(t) = \prod_{i=1}^{n} R_i(t)
\]

• No redundancy: Overall system reliability depends on the proper working of each component

\[
R_{ser}(t) = e^{-t(\sum_{i=1}^{n} \lambda_i)}
\]

• Serial failure rate

\[
\lambda_{ser} = \sum_{i=1}^{n} \lambda_i
\]
System Reliability

• Building a reliable serial system is extraordinarily difficult and expensive.

• For example: if one is to build a serial system with 100 components each of which had a reliability of 0.999, the overall system reliability would be

\[0.999^{100} = 0.905\]

• Reliability of System of Components

• Minimal Path Set:
  Minimal set of components whose functioning ensures the functioning of the system: \{1,3,4\} \{2,3,4\} \{1,5\} \{2,5\}
Parallel System Reliability

- Parallel Connected Components

- $Q_k(t)$ is $1 - R_k(t)$: $Q_k(t) = 1 - e^{-\lambda_k t}$

- Assuming the failure rates of components are statistically independent.

\[
Q_{par}(t) = \prod_{i=1}^{n} Q_i(t)
\]

- Overall system reliability: $R_{par}(t) = 1 - \prod_{i=1}^{n} (1 - R_i(t))$
Example

• Consider 4 identical modules are connected in parallel

• System will operate correctly provided at least one module is operational. If the reliability of each module is 0.95.

• The overall system reliability is $1 - (1 - 0.95)^4 = 0.999999375$
Parallel-Serial Reliability

- Parallel and Serial Connected Components

- Total reliability is the reliability of the first half, in serial with the second half.

- Given $R_1=0.9$, $R_2=0.9$, $R_3=0.99$, $R_4=0.99$, $R_5=0.87$

- $R_t = (1 - (1 - 0.9)(1 - 0.9))(1 - (1 - 0.87)(1 - (0.99 \times 0.99))) = 0.987$
Faults and Their Sources

• What is a fault?
  Fault is an erroneous state of software or hardware resulting from failures of its components

• Fault Sources
  • Design errors
  • Manufacturing Problems
  • External disturbances
    • Harsh environmental conditions
  • System Misuse
Fault Sources

• Mechanical -- “wears out”
  • Deterioration: wear, fatigue, corrosion
  • Shock: fractures, overload, etc.

• Electronic Hardware -- “bad fabrication; wears out”
  • Latent manufacturing defects
  • Operating environment: noise, heat, ESD, electro-migration
  • Design defects

• Software -- “bad design”
  • Design defects
  • “Code rot” -- accumulated run-time faults

• People
  • Can take a whole lecture content...
Fault and Classifications

- **Failure**: Component does not provide service
- **Fault**: A defect within a system
- **Error**: A deviation from the required operation of the system or subsystem
- **Extent**: Local (independent) or Distributed (related)
- **Value**:
  - Determinate
  - Indeterminate (varying values)
- **Duration**:
  - Transient
  - Intermittent
  - Permanent
Fault-Tolerant Computing

Tolerating Faults

- There is four-fold categorisation to deal with the system faults and increase system reliability and/or availability.

- Methods for Minimising Faults

  - **Fault Avoidance**: How to prevent the fault occurrence. Increase reliability by conservative design and use high reliability components.
  
  - **Fault Tolerance**: How to provide the service complying with the specification in spite of faults having occurred or occurring.
  
  - **Fault Removal**: How to minimise the presence of faults.
  
  - **Fault Forecasting**: How to estimate the presence, occurrence, and the consequences of faults.

- Fault-Tolerance is the ability of a computer system to survive in the presence of faults.
Fault-Tolerance Techniques

• Hardware Fault Tolerance

• Software Fault Tolerance
Hardware Fault-Tolerance Techniques

- Fault Detection

- Redundancy (masking, dynamic)
  - Use of extra components to mask the effect of a faulty component. (Static and Dynamic)
  - Redundancy alone does not guarantee fault tolerance. It guarantee higher fault arrival rates (extra hardware).

- Redundancy Management is Important
  - A fault tolerant computer can end up spending as much as 50% of its throughput in managing redundancy.
Hardware Fault-Tolerance: Fault Detection

- Detection of a failure is a challenge
  - Many faults are latent that show up later

- Fault detection gives warning when a fault occurs.
  - Duplication: Two identical copies of hardware run the same computation and compare each other results. When the results do not match a fault is declared.
  - Error Detecting Codes: They utilise information redundancy
Hardware Fault-Tolerance: Redundancy

- Static and Dynamic Redundancy

- Extra components mask the effect of a faulty component.

- Masking Redundancy
  Static redundancy as once the redundant copies of an element are installed, their interconnection remains fixed e.g. N-tuple modular redundancy (nMR), ECC, TMR (Triple Modular Redundancy) 3 identical copies of modules provide separate results to a voter that produces a majority vote at its output.

- Dynamic Redundancy System configuration is changed in response to faults. Its success largely depends upon fault detection ability.
TMR Configuration

• PR1, PR2 and PR3 processors execute different versions of the code for the same application.

• Voter compares the results and forward the majority vote of results (two out of three).
Software Fault-Tolerance

• Hardware based fault-tolerance provides tolerance against physical i.e. hardware faults.

• How to tolerate design/software faults?
  It is virtually impossible to produce fully correct software.

• We need something:
  • To prevent software bugs from causing system disasters. To mask out software bugs.
  • Tolerating unanticipated design faults is much more difficult than tolerating anticipated physical faults.

• Software Fault Tolerance is needed as:
  • Software bugs will occur no matter what we do. No fully dependable way of eliminating these bugs. These bugs have to be tolerated.
Tolerating Software Failures

• How to Tolerate Software Faults?
  Software fault-tolerance uses design redundancy to mask residual design faults of software programs.

• Software Fault Tolerance Strategy

• Defensive Programming
  • If you cannot be sure that what you are doing is correct.
  • Do it in many ways.
  • Review and test the software.
  • Verify the software.
  • Execute the specifications.
  • Produce programs automatically.
SW Fault-Tolerance Techniques

- Software Fault-tolerance is based on HW Fault-tolerance
- Software Fault Detection is a bigger challenge
  - Many software faults are of latent type that shows up later.
  - Can use a watchdog to figure out if the program is crashed
- Change the specification to provide low level of service
- Write new versions of the software
  - Throw the original version away. Use all the versions and vote the results. N-version Programming (NVP)
- Use an on-line acceptance test to determine which version to believe. Recovery Block Scheme.
Fault-tolerant Software Design Techniques

- Recovery block scheme (RB)
  Dynamic redundancy

- N-version programming scheme (NVP)
  n-modular redundancy

- Hardware redundancy is needed to implement the above Software Fault-tolerance techniques.
Fault-tolerant Software Design Techniques

RB Scheme comprises of three elements:
A primary module to execute critical software functions.
Acceptance test for the output of primary module. Alternate modules perform the same functions as of primary.

N-independent program variants execute in parallel on the identical input. Results are obtained by voting upon the output of individual programs.
RB uses diverse versions. Attempt to prevent residual software faults.
Fault Recovery

• Fault recovery technique's success depends on the detection of faults accurately and as early as possible.

• Three classes of recovery procedures:
  
  • Full Recovery
    It requires all the aspects of fault tolerant computing.
  
  • Degraded recovery: Also referred as graceful degradation. Similar to full recovery but no subsystem is switched-in.
    • Defective component is taken out of service.
    • Suited for multiprocessors.
  
  • Safe Shutdown
Fault Recovery

• Two Basic Approaches:
  • Forward Recovery
    • Produces correct results through continuation of normal processing.
    • Highly application dependent
  • Backward Recovery
    • Some redundant process and state information is recorded with the progress of computation.
    • Rollback the interrupted process to a point for which the correct information is available.
  • e.g. Retry, Checkpointing, Journaling
Summary

• Reliability
  • Serial Reliability, Parallel Reliability, System Reliability

• Fault Tolerance
  • Hardware, Software
Preview

• Scheduling Theory

  • Priority Inversion

• Priority Inheritance Protocol