# Discrete Mathematics & Mathematical Reasoning Course Overview

Colin Stirling

Informatics

Colin Stirling (Informatics)

**Discrete Mathematics** 

Today 1/24

# Teaching staff

#### Lecturers:

- Colin Stirling, first half of course
- Kousha Etessami, second half of course

### Course Secretary (ITO):

• Kendall Reid (kreid5@staffmail.ed.ac.uk)

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### Course web page on Learn and at

http://www.inf.ed.ac.uk/teaching/courses/dmmr/

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## Course web page on Learn and at

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#### Contains important links to

- Lecture schedule and slides
- Study guide (textbook reading)
- Weekly tutorial exercises
- Coursework
- Tutorial groups
- Discussion forum (piazza) not yet available
- Course organization
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### Lectures

- Monday 16.10-17.00 Here
- Tuesday 10.00-10.50 David Hume Tower, Lecture Theatre C
- Thursday 16.10-17.00 Here

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- 10 weeks of lectures in two halves of 5 weeks
- Lecture schedule and slides (like this one) on web page
- Study guide (textbook reading)

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### Textbook

- Kenneth Rosen, **Discrete Mathematics and its Applications**, 7th Edition, (Global Edition) McGraw-Hill, 2012
- Available at Blackwells
- For additional material see the course webpage

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- You will pick up your marked scripts from the ITO once marked

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- To pass course need 40% or more overall
- No separate exam/coursework hurdle

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  - 2 hours per week on coursework

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- Extra help at INFBASE

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### Questions about course administration?

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# Syllabus

- mathematical reasoning
- combinatorial analysis
- discrete structures
- algorithmic thinking
- applications and modelling

# Foundations: proof

- Rudimentary predicate (first-order) logic: existential and universal quantification, basic algebraic laws of quantified logic (duality of existential and universal quantification)
- The structure of a well-reasoned mathematical proof; proof strategies: proofs by contradiction, proof by cases; examples of incorrect proofs (to build intuition about correct mathematical reasoning)

## Foundations: sets, functions and relations

- Sets (naive): operations on sets: union, intersection, set difference, the powerset operation, examples of finite and infinite sets (the natural numbers). Ordered pairs, n-tuples, and Cartesian products of sets
- Relations: (unary, binary, and n-ary) properties of binary relations (symmetry, reflexivity, transitivity).
- Functions: injective, surjective, and bijective functions, inverse functions, composition of functions
- Rudimentary counting: size of the Cartesian product of two finite sets, number of subsets of a finite set, (number of n-bit sequences), number of functions from one finite set to another

## Induction and recursion

- Principle of mathematical induction (for positive integers)
- Examples of proofs by (weak and strong) induction

## Basic number theory and some cryptography

- Integers and elementary number theory (divisibility, GCDs and the Euclidean algorithm, prime decomposition and the fundamental theorem of arithmetic)
- Modular arithmetic (congruences, Fermat's little theorem, the Chinese remainder theorem)
- Applications: public-key cryptography

# Counting

- Basics of counting
- Pigeon-hole principle
- Permutations and combinations
- Binomial coefficients, binomial theorem, and basic identities on binomial coefficients
- Generalizations of permutations and combinations (e.g., combinations with repetition/replacement)
- Stirling's approximation of the factorial function

# Graphs

- Directed and undirected graph: definitions and examples in Informatics
- Adjacency matrix representation
- Terminology: degree (indegree, outdegree), and special graphs: bipartite, complete, acyclic, ...
- Isomorphism of graphs; subgraphs
- Paths, cycles, and (strong) connectivity
- Euler paths/circuits, Hamiltonian paths (brief)
- Weighted graphs, and shortest paths (Dijkstra's algorithm)
- Bipartite matching: Hall's marriage theorem

### Trees

- Rooted and unrooted trees
- Ordered and unordered trees
- (Complete) binary (k-ary) tree
- Subtrees
- Examples in Informatics
- Spanning trees (Kruskal's algorithm, Prim's algorithm.)

## **Discrete probability**

- Discrete (finite or countable) probability spaces
- Events
- Basic axioms of discrete probability
- Independence and conditional probability
- Bayes' theorem
- Random variables
- Expectation; linearity of expectation
- Basic examples of discrete probability distributions, the birthday paradox and other subtle examples in probability
- The probabilistic method: a proof technique

Questions about course syllabus?

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Discrete Mathematics

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# My proof

Colin's proof that 1=2 a = b Premise a<sup>2</sup> = a.b Multiply both sides by a  $a^2 - b^2 = ab - b^2$  Subtract  $b^2$  from both sides. (a-b)(a+b) = b(a-b) Algebra a+b = bDivide both sides by a-E 2b = bReplace a by b because a=b 2 = Divide both sides by b

#### Given the following two premises

- All students in this class understand logic
- Colin is a student in this class

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### Does it follow that

Colin understands logic

#### Given the following two premises

- Every computer science student takes discrete mathematics
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### Does it follow that

• Helen is a computer science student

### Given the following three premises

- All hummingbirds are richly coloured
- No large birds live on honey
- Birds that do not live on honey are dull in colour

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### Does it follow that

• Hummingbirds are small