Computer Programming: Skills & Concepts (CP1)
Intro to Practical 3:
Travelling Salesman Problem

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Travelling Salesman Problem (TSP)

A well-known theoretical and practical problem:

- a salesman has to visit a number of cities
- what is the shortest route to visit all cities and return home?

Properties of the problem:

- hard to solve for large number of cities
- instance of a *NP-complete* problem
Complexity of problems

We have already encountered problems with different complexity:

- search through unsorted array: linear (ie, $O(n)$)
- binary search through sorted array: log (ie, $O(\lg(n))$)
- BubbleSort: $O(n^2)$
- MergeSort: $O(n \lg(n))$
NP-complete?

- For some problems, no polynomial time solution is known — $O(n^c)$ for some constant $c$. One class of these problems is called NP-complete (NP = non-polynomial).
- There may be polynomial solutions, but nobody found them so far.
- If *efficient* solution of a problem is not possible, we resort to *heuristics* that give us approximate solutions.
Other NP-hard problems

- Knapsack problem: given a set of whole numbers $a_1, \ldots, a_n$, and an upper bound $K$ find a subset of the numbers whose sum is of maximum value, subject to being no more than $K$.
  
  E.g., for 2, 4, 9, 11, 14 and $K = 25$, the subset is $\{2, 9, 14\}$

- Minesweeper: is a given configuration "possible"?
Example TSP: Romania
Simplified: Euclidean TSP

All connections are straight lines. How do we find the shortest path?
Greedy heuristic

- start at some point
- go to closest not visited city
Greedy heuristic: result
Improving the solution

- Swap neighboring cities, if it shortens path
Locally Optimal solution
Other improvements?

What other improvements can be made?
Practical 3

- Part A: capture positions of cities (from mouse clicks), and store them all in an array. Write a function to compute the length of a given tour.
- Part B: implement swap heuristic.
- Part C: implement 2-opt heuristic (more powerful).
- Part D: implement greedy heuristic.
- Part E: do better, with almost no extra work?