Computer Programming: Skills & Concepts (CP) Searching and sorting

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Monday 13 November 2017

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Searching an array

typedef enum {FALSE, TRUE} Bool_t;

```
Bool_t LinearSearch(int n, int a[], int sKey)
/* Returns TRUE iff (if and only if) sKey is contained in
 * the array, i.e., there exists an index i with 0 \le i \le n
 * such that a[i] == sKey.
 */
ł
  int i;
  for (i = 0; i < n; ++i) {
      if (a[i] == sKey) return TRUE;
  }
   return FALSE;
}
```

variant:

Could use return type int with #DEFINE for TRUE, FALSE (see BinarySearch) CP Lect 17 - slide 2 - Monday 13 November 2017

Sometimes we quickly want to find an entry in an array. It helps if the array is sorted.

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How do you search for a name in a telephone book?

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Repeatedly chop the array in half to close in on where the element must be. E.g., to search for 17 in:

2 3 5 7 11 13 17 19 23 29

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Find the mid-point: 17 > 11, so narrow to right half:

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Find the mid-point: $17 \leq 19$, so narrow to left half:

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(yes, we could stop here because we've found it...)

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Find the mid-point: 17 > 13, so narrow to right half:

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Find the mid-point: $17 \leq 17$, so narrow to left half:

(yes, we could stop here because we've found it...)

Find the mid-point: 17 > 13, so narrow to right half:

Now we're left with an array of size 1, so either its element is 17 and we've found it, or 17 isn't there.

int BinarySearch(int n, int a[], int sKey)

/* Assumes: elements of array a are in ascending order.

* Returns TRUE iff sKey is contained in the array, i.e.,

* there exists an index i with 0 <= i < n and a[i] == sKey.
*/</pre>

i = 0;

ſ

j = n - 1;

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```
/* Invariant just before (re-)entering loop: i <= j AND
 * if sKey is in a[0:n-1] then sKey is in a[i:j] */
while (i < j) {
 m = (i + j)/2;
 if (sKey <= a[m]) {
   j = m;
 }
 else {
    i = m + 1;
 }
}
/* After exiting loop:
 * (i \ge j), by i, j updates, means (i == j).
 * now EITHER a[i] == sKey OR sKey is not in a[0:n-1] */
return a[i] == sKey;
```

Note how we return true/false ...

}

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Running time

The *(worst-case)* running time of a function (or *algorithm*) is defined to be the maximum number of steps that might be performed by the program as a function of the *input size*.

- ▶ For functions which take an array (of some basic type) as the input, the length of the array (n in lots of our examples) is usually taken to represent size.
- ► The running time of Linear Search proportional to n (i.e., around c · n for some constant c), and the running time of Binary Search is proportional to lg(n).

Measuring running time on a machine

```
#include <time.h>
Bool_t flag = FALSE;
int a[24000000];
clock_t start, stop;
double t;
. . .
start = clock();
flag = LinearSearch(a, 24000000, -5);
stop = clock();
t = ((double)(stop-start))/CLOCKS_PER_SEC;
printf("Time spent by Linear Search was %lf seconds.\n", t);
. . .
```

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Measuring running time on a machine

```
#include <time.h>
Bool_t flag = FALSE;
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clock_t start, stop;
double t;
. . .
start = clock();
flag = LinearSearch(a, 24000000, -5);
stop = clock();
t = ((double)(stop-start))/CLOCKS_PER_SEC;
printf("Time spent by Linear Search was %lf seconds.\n", t);
. . .
```

On my laptop:

Time spent by LinearSearch was 0.069064 seconds. Time spent by BinarySearch was 0.000001 seconds.

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Sorting

Given an array of integers (or any *comparable* type), re-arrange the array so that the items appear in increasing order.

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Bubble sort

'Pseudo-code'

for (i = n - 1; i >= 1; i--) {
 /* Rearrange the contents of
 * array elements a[0], ..., a[i],
 * so that the largest value appears
 * in element a[i].
 */
}

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Bubble sort

'Pseudo-code'

```
for (i = n - 1; i >= 1; i--) {
    /* Rearrange the contents of
    * array elements a[0], ..., a[i],
    * so that the largest value appears
    * in element a[i].
    */
}
```

'Method':

- Find the largest item, and move it to the end;
- repeat for 2nd largest item, and so on ...

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Bubble sort (cont'd)

The task of rearranging the contents of array elements a[0], a[1], ..., a[i] so that the largest value appears in element a[i], may be handled by the following simple loop:

```
for (j = 0; j < i; j++) {
    if (a[j] > a[j+1]) {
        swap(&a[j], &a[j+1]);
    }
}
```

(The largest value supposedly 'bubbles' up the array into its appropriate position.)

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Bubble sort code

```
/* Sorts a[0], a[1], ..., a[n-1] into ascending order. */
void BubbleSort(int a[], int n) {
   int i, j;
   for (i = n - 1; i \ge 1; i--) {
      /* Invariant: The values in locations to the right of
       * a[i] are in their correct resting places: they are
       * the (n - i - 1)-largest elements arranged in
       * positions (i+1), ..., (n-1), in non-descending order
      for (j = 0; j < i; j++) {
         if (a[j] > a[j+1]) {
            swap(&a[j], &a[j+1]);
         }
      }
   }
```

The swap function used above is the (correct) one from lab 5.

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Running time of Bubble Sort

The (worst case) running time of Bubble Sort is proportional to n^2 . why?

There are better sorting algorithms ... for example MergeSort or HeapSort run in time proportional to $n \lg(n)$.

For general purpose sorting, often use *QuickSort*, which runs in time around $n \lg n$ in most cases, though in bad cases (which?) it can take n^2 . Standard C systems provide QuickSort as qsort. Occasionally you might know that BubbleSort would be quicker in your application, and want to program it. Anything else is probably specialist.

More about Bubble-Sort can be found in Section 6.7 of 'A Book on C'.

Understanding your loops

These slides are logically small and green: for the mathematically and logically inclined only!

- How can you show that a program is correct?
- One way is to show that certain statements are true at all times in the program (*invariants*)
- In particular, to understand a complex while/for-loop, it's useful to know what remains true every time you go through it.
- For functions (or other blocks of code) we have *preconditions* (things *assumed* be true before) and *postconditions* (things which *will* be true afterwards given the preconditions).

We'll do a simple example now; then look (in your own time) at the comments in the searching and sorting code, and try to understand what they're saying about invariants.

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Power of a number

```
int Power(int n, int k)
/* Pre-condition: k \ge 0. */
/* On-exit: returns n^k (n raised to the power k). */
ſ
   int p = 1, i = k;
   /* Invariant before (re-)entering:
    * i >= 0 AND p * n^i == n^k */
   while (i > 0) {
      p *= n;
     --i:
  }
   /* After exiting loop: i <= 0 AND p = n^k */</pre>
   return p;
}
```

Warning: n^k in the comments is maths notation, not C notation. In C, the [^] symbol is the bitwise exclusive-or operator, something entirely different! CP Lect 17 - slide 14 - Monday 13 November 2017

Example: n = 3, k = 4. The answer should be $3^4 = 81$. The computation progresses as follows. Initially, i = k and p = 1. Note that $p \times n^i$ is invariant!

/* Invariant before (re-)entering: i >= 0 AND p * n^i == n^k */ while (i > 0) { p *= n; --i; } /* After exiting loop: i <= 0 AND p = n^k */ return p;

	i	р	$p imes n^i$
Initial	4	1	$1 \times 3^4 = 81$
Iteration 1	3	3	$3 \times 3^3 = 81$
Iteration 2	2	9	$9 \times 3^2 = 81$
Iteration 3	1	27	$27 \times 3^1 = 81$
Iteration 4	0	81	$81 \times 3^0 = 81$

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Reading material

Sections of 'A Book on C' that are relevant are:

- A good idea to refresh your memory of arrays (early sections of Chapter 6).
- Section 6.7 has a discussion of BubbleSort.

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