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# Speculative Parallelisation

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## Course Structure

- 5 lectures on high level restructuring for parallelism
- Dependence Analysis
- Program Transformations
- Automatic vectorisation
- Automatic parallelisation
- Speculative Parallelisation

## Lecture Overview

- Based on LPRD test: Speculative Run-time Parallelisation of loops with privatization and reduction parallelism
  - Lawrence Rachwerger PLDI 1995
  - Expect you to read and understand this paper. Many follow up papers
- Types of parallel loops
- Irregular parallelism
- LPRD test and examples

## Parallel Loop : DOALL Implementation

|                                                           |                                                      |                                                                                                                                                                |
|-----------------------------------------------------------|------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <pre>Do i = 1 , N   A(i) = B(i)   C(i) = A(i) Enddo</pre> | <pre>p = get_num_proc() fork (x_sub, p) join()</pre> | <pre>SUBROUTINE x_sub() p = get_num_proc() z = my_id() ilo = N/p * (z-1) +1 ihi = min(N, ilo+N/p) Do i = ilo , ihi   A(i) = B(i)   C(i) = A(i) Enddo END</pre> |
|-----------------------------------------------------------|------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------|

- Generate p independent threads of work
  - Each has private local variables, z, ilo, ihi
  - Access shared arrays A,B and C

## Privatisation

|                                                                         |                                                                                            |
|-------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|
| <pre>Do i = 1 , N   temp = A(i)   A(i) = B(i)   B(i) = temp Enddo</pre> | <pre>DO i = ilo , ihi   private temp   temp = A(i)   A(i) = B(i)   B(i) = temp Enddo</pre> |
|-------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|

- Temp is used as temporary storage on each iteration
  - Its value is never used on subsequent iterations
  - However there is a cross iteration ant-dependence and output dependence.
  - Each local iteration of  $i$  happens in order
  - Could scalar expand - but increase storage :  $O(1)$  to  $O(N)$
  - Alternatively each processor has a private copy:  $O(p)$  cost.  $p \ll N$

## Reduction Parallelism

|                                               |                                                                                                                                            |
|-----------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------|
| <pre>Do i = 1 to N   a = a + B(i) Enddo</pre> | <pre>pa(z) = 0 Do i = ilo, ihi   pa(z) = pa(z) + B(i) Enddo call barrier_sync() if (z .EQ. 1) Do x = 1,p   a = a + pa(x) Enddo endif</pre> |
|-----------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------|

- Output flow and anti dependence
  - But can perform partial sums in parallel and merge
  - Works for associative and commutative operators

## Irregular Parallelism

Do  $i = 1$  to  $N$

$A(X(i)) = A(Y(i)) + B(i)$

Enddo

- Cross iteration Output dependent if any  $X(i_1) = X(i_2)$   $i_1 \neq i_2$
- Cross iterating Flow/anti dependent if any  $X(i_1) = Y(i_2)$   $i_1 \neq i_2$
- Dependence depends on values of  $X$  and  $Y$  - not compile-time knowable
- More than half scientific programs are irregular - sparse arrays

## Runtime Parallelisation: The idea

```
Do i = 1 , N
  A(i+k) = A(i) + B(i)
Enddo
```

```
if (-N < K < N)
  Do i = 1 , N
    A(i+k) = A(i) + B(i)
  Enddo
else
  Doall i = 1 , N
    A(i+k) = A(i) + B(i)
  Enddo
```

- Select dynamically between pre-optimised versions of the code
  - Analysis at runtime
  - Here check simple but can be more complex



## Runtime Parallelisation: Irregular Applications

|                                                                                                  |                                                                                                                                                                            |
|--------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <pre>Do i = 1 , N   A(w(i)) = A(r(i)) + B(i) Enddo  Assume parallel then  fallback if fail</pre> | <pre>DOALL i = 1 , N   trace (w(i), r(i))   A(w(i)) = A(r(i)) + B(i) Enddo Analyse if (fail) // Sequential   DO i = 1 , N     A(w(i)) = A(r(i)) + B(i)   Enddo endif</pre> |
|--------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Loop not parallel if any  $r(i_1) = w(i_2)$ ,  $i_1 \neq i_2$

Collect data access pattern and verify if dependence could occur

## Speculative Doall Marking and Analysis

- Record all accesses to shadows - one per processor. Check afterwards
- Parallel speculative execution
  - Mark read and write operations into different private shadow arrays, marking write implies clear read mark
  - Increment private write counter ( $\#$  write operations)
- Post speculation analysis
  - Merge private shadow arrays to global shadow arrays
  - Count elements marked write
  - (write shadow  $\&\&$  read shadow  $\neq 0$ ) implies anti/flow dependence
  - ( $\# \bmod \text{elems} < \# \text{write ops}$ ) implies output deps

## LRPD test Example

|                                                                                                                |                                                                           |
|----------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------|
| <pre>A(4), B(5), K(5), L(5) Do i = 1,5   z = A(K(i))   if B(i) then     A(L(i)) = z + C(i)   endif Enddo</pre> | <pre>B(1:5) = (1,0,1,0,1) K(1:5) = (1,2,3,4,1) L(1:5) = (2,2,4,4,2)</pre> |
|----------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------|

Unsafe if  $A(K(i_1)) = A(L(i_2))$ ,  $i_1 \neq i_2$

## LRPD test Marking phase

- Allocate shadow arrays  $A_w$ ,  $A_r$ ,  $A_{np}$  one per processor.  $O(np)$  overhead. Speculatively privatise  $A$  and execute in parallel. Record accesses to data under test in shadows
- Mark write()
  - increment  $tw\_A$  (write counter)
  - If first time  $A(i)$  written in iter, mark  $A_w(i)$ , clear  $A_r(i)$
  - (Only concerned with cross-it deps)
- Mark read  $A(i)$ :
  - If  $A(i)$  not already written in iter, mark  $A_r(i)$  and mark  $A_{np}(i)$
  - Note  $A_{np}(i)$  not cleared by MarkWrite.  $np$ =not privatisable

## LRPD test Marking phase

```
A(4), B(5),K(5), L(5)
```

```
Doall i = 1,5
```

```
  z = A(K(i))
```

```
  if B(i) then
```

```
    markread(K(i))
```

```
    markwrite(L(i))
```

```
    A(L(i)) = z + C(i)
```

```
  endif
```

```
Enddo
```

- Note markread occurs inside conditional
  - Read to A only considered if z accessed.
  - Otherwise ignore

## LRPD test Results after marking

|                                                                                                                                                                                |                                                                                                                                                                                                                                                                                                                                                                                                                                                                |   |   |   |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |        |   |   |   |   |         |   |   |   |   |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---|---|---|---|---|---------|---|---|---|---|---------|---|---|---|---|----------|---|---|---|---|--------|---|---|---|---|---------|---|---|---|---|
| <pre>A(4), B(5), K(5), L(5) Do i = 1,5   z = A(K(i))   if B(i) then     A(L(i)) = z + C(i)   endif Enddo  B(1:5) = (1,0,1,0,1) K(1:5) = (1,2,3,4,1) L(1:5) = (2,2,4,4,2)</pre> | <table border="1"><tr><td></td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>Aw(1:4)</td><td>0</td><td>1</td><td>0</td><td>1</td></tr><tr><td>Ar(1:4)</td><td>1</td><td>0</td><td>1</td><td>0</td></tr><tr><td>Anp(1:4)</td><td>1</td><td>0</td><td>1</td><td>0</td></tr><tr><td>Aw&amp;&amp;Ar</td><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>Aw&amp;&amp;Anp</td><td>0</td><td>0</td><td>0</td><td>0</td></tr></table> <p>tw =3, tm = 2</p> |   | 1 | 2 | 3 | 4 | Aw(1:4) | 0 | 1 | 0 | 1 | Ar(1:4) | 1 | 0 | 1 | 0 | Anp(1:4) | 1 | 0 | 1 | 0 | Aw&&Ar | 0 | 0 | 0 | 0 | Aw&&Anp | 0 | 0 | 0 | 0 |
|                                                                                                                                                                                | 1                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 2 | 3 | 4 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |        |   |   |   |   |         |   |   |   |   |
| Aw(1:4)                                                                                                                                                                        | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 1 | 0 | 1 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |        |   |   |   |   |         |   |   |   |   |
| Ar(1:4)                                                                                                                                                                        | 1                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 0 | 1 | 0 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |        |   |   |   |   |         |   |   |   |   |
| Anp(1:4)                                                                                                                                                                       | 1                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 0 | 1 | 0 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |        |   |   |   |   |         |   |   |   |   |
| Aw&&Ar                                                                                                                                                                         | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 0 | 0 | 0 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |        |   |   |   |   |         |   |   |   |   |
| Aw&&Anp                                                                                                                                                                        | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 0 | 0 | 0 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |        |   |   |   |   |         |   |   |   |   |

where  $tm(A) = \text{sum over } Aw$

Total number of distinct elements written

## LRPD test Analysis phase

- if  $A_w \ \&\& \ A_r$  then NOT doall – read and write in diff iterations to same elem
- else if  $t_w = t_m$  then was a DOALL – unique iterator writes
- else if  $A_w \ \&\& \ A_{np}$  then NOT doall
- otherwise loop privatisation valid, DOALL

$A_w \ \&\& \ A_r = 0$  : Fail

$t_w \neq t_m$  : Fail

$A_w \ \&\& \ A_{np} = 0$  : Fail

Overall privatise - remove output dependence

## LRPD test Marking phase: Handling reductions

- Allocate shadow arrays  $A_{nx}$  one per processor.  $O(np)$  overhead.
- Record accesses to data under test in shadows
- Mark Redux ()
  - mark  $A(i)$  if element is NOT valid reference in reduction statement - not a reduction variable



## LRPD test Marking phase

|                                                                                                     |                                                                                                                                                                             |
|-----------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <pre>A(4), K(4), L(4), R(4) Do i = 1,4   A(k(i)) =     = A(L(i))   A(r(i)) = A(r(i)+exp Enddo</pre> | <pre>Doall i = 1,4   markwrite(k(i))   markredux(k(i))   A(k(i)) =   markread(L(i))   markredux(L(i))     = A(L(i))   markwrite(r(i))   A(r(i)) = A(r(i)+exp Enddoall</pre> |
|-----------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Note markredux on those accesses not forming reduction

## LRPD test Reduction shadow arrays

|                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                           |   |   |   |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |          |   |   |   |   |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---|---|---|---|---|---------|---|---|---|---|---------|---|---|---|---|----------|---|---|---|---|----------|---|---|---|---|
| <pre>Doall i = 1,4   markwrite(k(i))   markredux(k(i))   A(k(i)) =   markread(L(i))   markredux(L(i))     = A(L(i))   markread(r(i))   markwrite(r(i))   A(r(i)) = A(r(i))+exp Enddoall</pre> | <pre>k(1:4) = (3,4,3,4) L(1:4) = (3,4,3,4) R(1:5) = (1,2,1,2)</pre> <table border="1"><tr><td></td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>Aw(1:4)</td><td>1</td><td>1</td><td>1</td><td>1</td></tr><tr><td>Ar(1:4)</td><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>Anp(1:4)</td><td>1</td><td>1</td><td>0</td><td>0</td></tr><tr><td>Anx(1:4)</td><td>0</td><td>0</td><td>1</td><td>1</td></tr></table> <pre>tw = 8 , tm = 4</pre> |   | 1 | 2 | 3 | 4 | Aw(1:4) | 1 | 1 | 1 | 1 | Ar(1:4) | 0 | 0 | 0 | 0 | Anp(1:4) | 1 | 1 | 0 | 0 | Anx(1:4) | 0 | 0 | 1 | 1 |
|                                                                                                                                                                                               | 1                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 2 | 3 | 4 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |          |   |   |   |   |
| Aw(1:4)                                                                                                                                                                                       | 1                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 1 | 1 | 1 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |          |   |   |   |   |
| Ar(1:4)                                                                                                                                                                                       | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 0 | 0 | 0 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |          |   |   |   |   |
| Anp(1:4)                                                                                                                                                                                      | 1                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 1 | 0 | 0 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |          |   |   |   |   |
| Anx(1:4)                                                                                                                                                                                      | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 0 | 1 | 1 |   |   |         |   |   |   |   |         |   |   |   |   |          |   |   |   |   |          |   |   |   |   |

where  $tm(A) = \text{sum over } Aw$ .

markread((r(i))) missing from original paper. Needed to mark Anp(i)

## LRPD test Reduction Analysis phase

Follows on from previous tests - two more added

- else  $A_w \ \&\& \ A_n \ \&\& \ A_x$  then NOT doall
- otherwise loop privatisation valid, reduction parallelism

$A_w \ \&\& \ A_r = 0$  : Fail

$t_w \neq t_m$  : Fail

BUT

$A_w \ \&\& \ A_n \ \&\& \ A_x = 0$  : Fail

So reduction parallelism

## LRPD test Improvements

- One dependence can invalidate speculative parallelisation
  - Partial parallelism not exploited
  - Transform so that up till first dependence parallel
  - Reapply on the remaining iterators.
- Large overheads
  - Adaptive data structures to reduce shadow array overhead
- Large amount of work in speculative parallelisation
  - Hardware support for TLS, transactional memory
  - Compiler :Combined with static analysis

## Summary

- Summary of parallelisation idioms
- Irregular accesses
- Shadow arrays
- Marking and analysis for doall and reductions
- Last lecture on parallelism. Next on adaptive compilation