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# Program Transformations

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## Course Structure

- L1 Introduction and Recap, L2 Course Work
- 5 lectures on high level restructuring for parallelism and memory
- Dependence Analysis
- **Program Transformations - loop and arrays**
- Automatic vectorisation, parallelisation
- Speculative Parallelisation

## Lecture Overview

- Classification of program transformations - loop and array
- Role of dependence
- Loop restructuring - changing the number/type of loop
- Iteration reordering - reordering the iterations scanned.
- Array transformations - data layout transformation
- Simplified presentation. Large number of technicalities. Applicability. Worth.

## References

- Loop Distribution with arbitrary control-flow McKinley and Kennedy Supercomputing 1990
- D.F. Bacon, S.L. Graham, and O.J. Sharp. Compiler Transformations for High-Performance Computing. ACM Computing Surveys, 26(4), 1994.
- A Framework for Unifying Reordering Transformations (1993) TR
- On the Complexity of Loop Fusion Alain Darte, PACT 1999
- L. Lamport. The parallel execution of do loops. Communications of the ACM, pages 83–93, February 1974.

## What is a program transformation

- A program transformation is a rewriting of the program such that it has the same semantics
- More conservatively, all data dependences must be preserved
- Previous lectures looked at IR→IR transformations or assembler→assembler transformations
- Focus on transformations in the high level source prog. language: source to source transformations
- Why: Only place where memory reference explicit. Key to restructuring for memory behaviour and large scale parallelism.

## Classification

Ongoing open question on a correct taxonomy

- Loop
  - Structure reordering. Change number of loops
  - Iteration reordering. Reorder loop traversal
  - Linear models. Express transformation as unimodular matrices.
- Array
  - Index reordering
  - Duality with loops. Global vs Local.
- All transformations have an associated legality test though some are always legal.

## Loop Restructuring Index Splitting

Always a legal transformation. No test needed

```
Do i = 1, 100
  a(101 -i) =a(i)
Enddo

Do i = 1, 50
  a(101 -i) =a(i)
Enddo

Do i = 51, 100
  a(101 -i) =a(i)
Enddo
```

A sequential loop with dependence [\*] is transformed into two independent parallel loops. Careful selection of split point.

Neither access in each loop refers to same memory location.

All of first loop must execute before second though - why?

## Loop Restructuring: Loop Unrolling

Used for exploiting Instruction Level Parallelism

Always legal - take care of epilogue using index splitting

```
Do i = 1, 100
  a(i) = i
Enddo

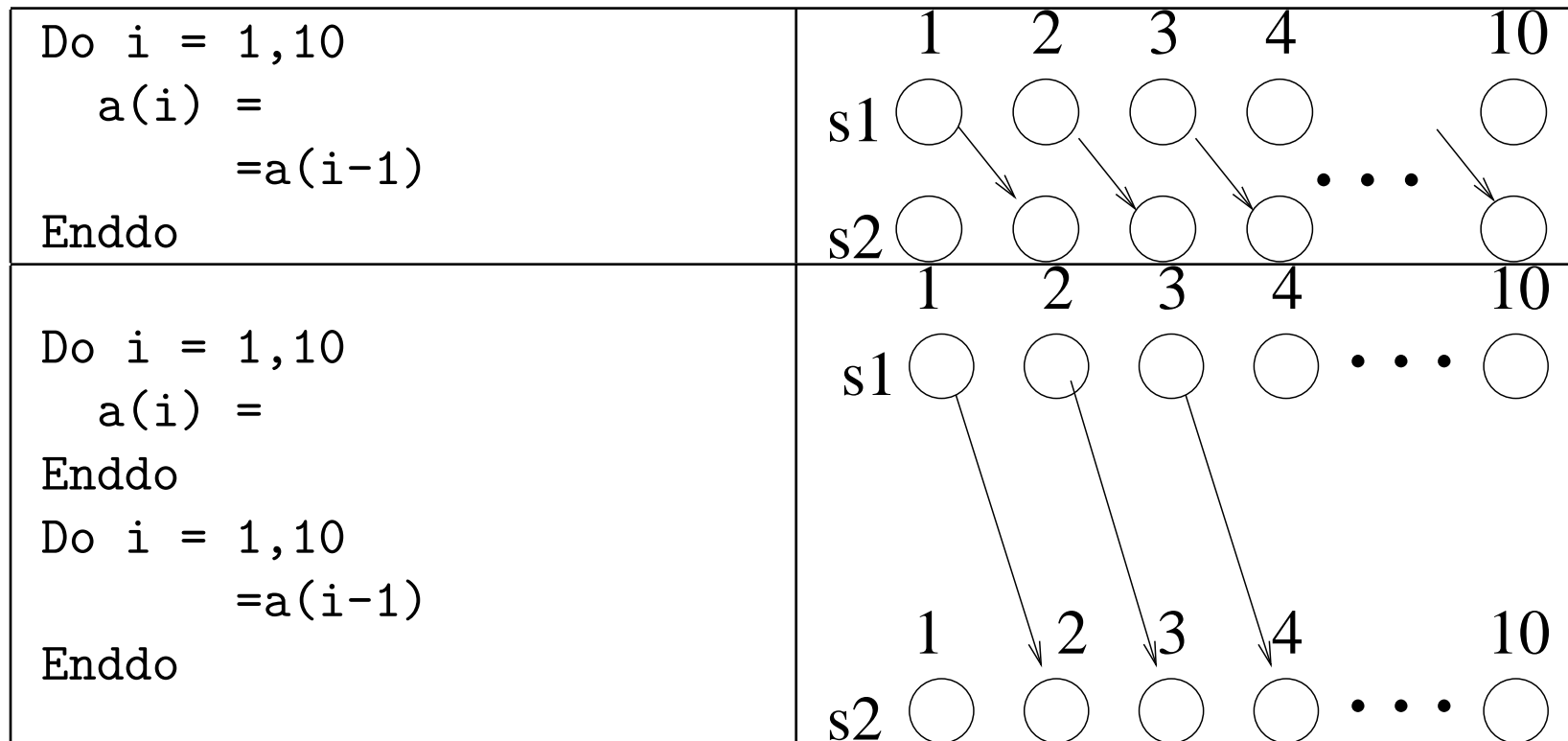
Do i = 1, 100, 3
  a(i) = i
  a(i+1) = i+1
  a(i+2) = i+2
Enddo
```

```
Do i = 100, 100
  a(i) = i
Enddo
```

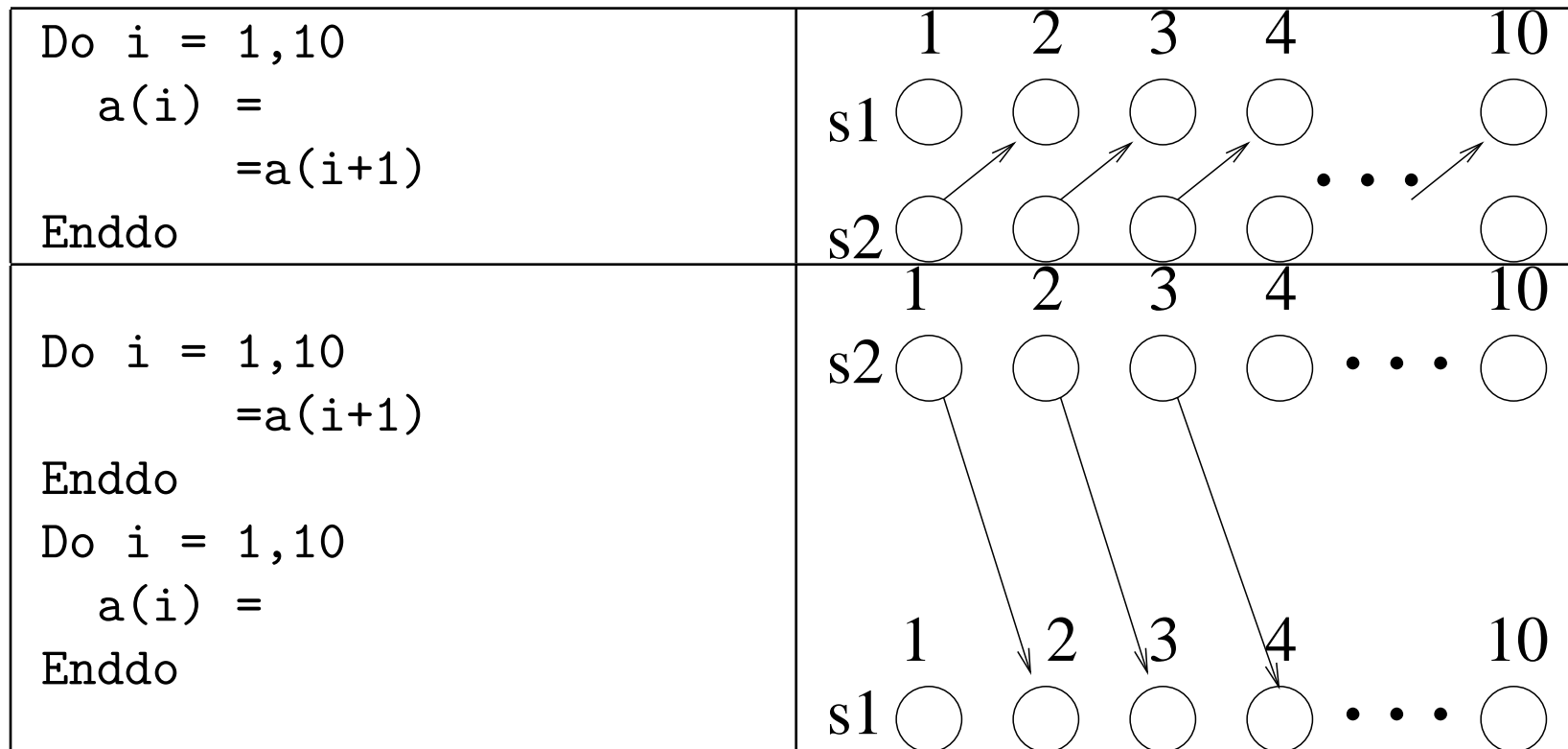
Non-convex iteration space after transformation - steps. Causes difficulties for dependence analysis. Can normalise loop though



## Loop Restructuring: Loop Distribution



## Loop Distribution + Statement Reordering



Anti-dependences honoured.

## Loop Restructuring: Loop Fusion

Inverse of loop distribution - needs conformant loops

<pre>Do i = 1,100   a(i) = Enddo Do j = 1,100   b(j) = Enddo</pre>	<pre>Do i = 1,100   a(i) =   b(i) = Enddo</pre>
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More difficult than distribution. Dependence constrains application.

Used for increasing ILP and improving register use. Also for fork/join based parallelisation.

Loops can be partly fused after pre-distribution

## Iteration reordering: Loop interchange

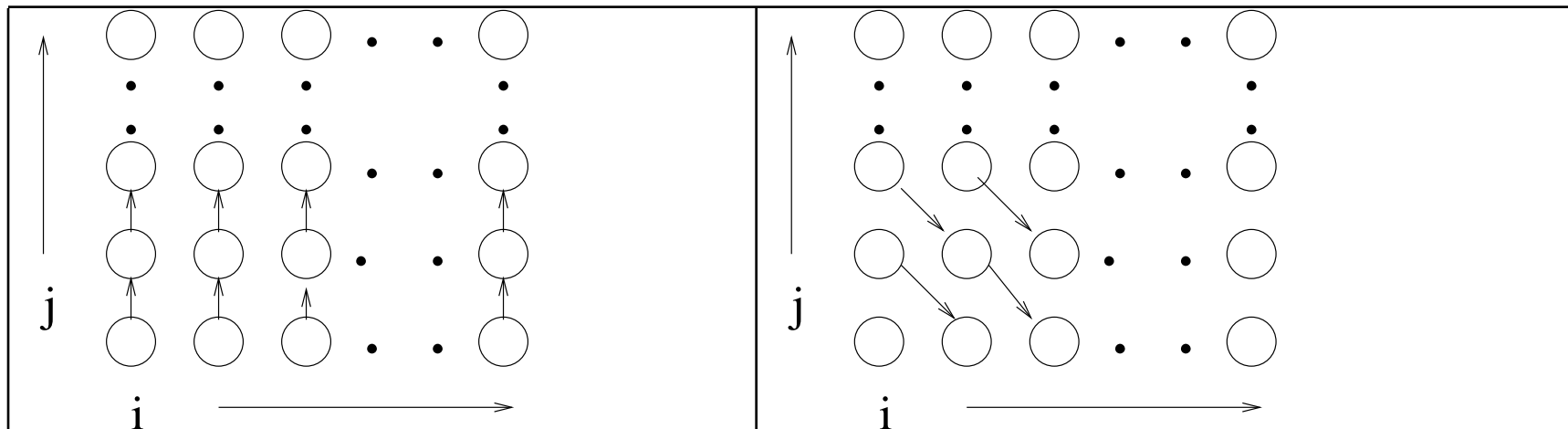
Important widely used transformation

<pre>Do i =1, N   Do j = 1,N     a(i,j) = a(i,j-1) +b(i)   Enddo Enddo</pre>	<pre>Do i =1, N   Do j = 1,N     a(i,j) = a(i-1,j+1) +b(i)   Enddo Enddo</pre>
<pre>Do j =1, N   Do i = 1,N     a(i,j) = a(i,j-1) +b(i)   Enddo Enddo</pre>	

$[i, j] \mapsto [j, i]$

Illegal to interchange  $[1,-1]$ ,  $[<, >]$  why?

## Iteration reordering: Loop interchange



Illegal to interchange  $[1,-1]$ : New vector  $[-1,1]$ :

Impossible dependence.

Linear models check  $TD > 0$

## Loop skewing

Always legal used in wavefront parallelisation

<pre>Do i =1, N   Do j = 1,N     a(i,j) = a(i,j-1)               +b(i)   Enddo Enddo</pre>	<pre>Do i =1, N   Do j = i+1,i+N     a(i,j-i) = a(i,j-i-1)                 +b(i)   Enddo Enddo</pre>
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- $[i, j] \mapsto [i, j + i]$
- Equivalent to a change of basis.
- Shifting by a constant referred to as loop bumping

## Loop reversal

```
Do i =1, N
  Do j = 1,N
    a(i,j) = a(i,j-1) +b(i)
  Enddo
Enddo
```

```
Do i =N, 1, -1
  Do j = 1,N
    a(i,j) = a(i,j-1) +b(i)
  Enddo
Enddo
```

- $[i, j] \mapsto [-i, j]$
- Rarely used in isolation. In unison with previous two.
- Can combine interchange, shewing and reversal as unimodular transformations/  
More on this later.

## Tiling = strip-mining plus interchange

<pre>Do i =1, N   Do j = 1,N     a(i,j) = a(i,j) +b(i)   Enddo Enddo</pre>	<pre>Do i =1, N,s   Do j = 1,N,s     Do ii = i, i+s-1       Do jj = j,j+s-1         a(ii,jj) = a(ii,jj) +b(ii)       Enddo     Enddo   Enddo Enddo</pre>
<pre>Do i =1, N   Do j = 1,N,s     Do jj = j,j+s-1       a(i,jj) = a(i,jj)+b(i)     Enddo   Enddo Enddo</pre>	<p>Strip-mine by factor s Non-convex space Interchange placing smaller strip-mine inside</p>



## Array layout transformations

- Less extensive literature though perhaps have a more significant impact
- Loop transformations affect all memory references within the loop but not elsewhere. Local in nature
- Array and more generally data transformations have global impact but do not affect other references to other arrays.
- Array layout transformations are used to improve memory access performance
- Also form the basis for data distribution based parallelisation schemes for distributed memory machines.

## Global index reordering

Dual of loop interchange. Always legal!  $[i_i, i_2] \mapsto [i_2, i_1]$

<pre>REAL A[10,20] Do i =1, 9   Do j = 2,20     a(i,j) = a(i+1,j-1) +b(i)   Enddo Enddo a(1,2) =0</pre>	<pre>REAL A[20,10] Do i =1, 9   Do j = 2,20     a(j,i) = a(j-1,i+1) +b(i)   Enddo Enddo a(2,1) =0</pre>
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- Array declaration and subscripts interchanged globally
- Difficulties occur if array reshaped on procedure boundaries

## Linearisation/delinearisation

### Dual of loop strip-mining/linearisation

<pre>REAL a[10,20] Do i =1, 9   Do j = 2,20     a(i,j) = a(i+1,j-1) +b(i)   Enddo Enddo a(1,2) =0</pre>	<pre>REAL a[200] Do i =1, 9   Do j = 2, 20     a(20*(i-1)+j) = a(20*(i)+j-1)                     +b(i)   Enddo Enddo a(2) =0</pre>
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## Padding

```
REAL A[10,20]
Do i =1, 9
  Do j = 2,20
    a(i,j) = a(i+1,j-1) +b(i)
  Enddo
Enddo
a(1,2) =0
```

```
REAL A[17,20]
Do i =1, 9
  Do j = 2,20
    a(i,j) = a(i+1,j-1) +b(i)
  Enddo
Enddo
a(1,2) =0
```

- Frequently used to overcome cache conflicts. Very simple
- Pad factor 7 in first index. Normally prime.

## Unification

- Presentation - simplistic conditions of application can be complex for arbitrary programs.
- Little overall structure.
- Unimodular transformation theory based on linear representation
- Extended to non-singular and the Unified Transformation Framework of Bill Pugh.
- Will return to look in more detail at this formulation in later lectures.

## Summary

- Large suite of transformations
- Loop restructuring and reordering
- Legality constraints restrict application
- Array based transformations. Always legal but global impact
- Unifying theories provide structured taxonomy.
- Next lecture: Vectorisation