

# LISSOM Orientation Maps

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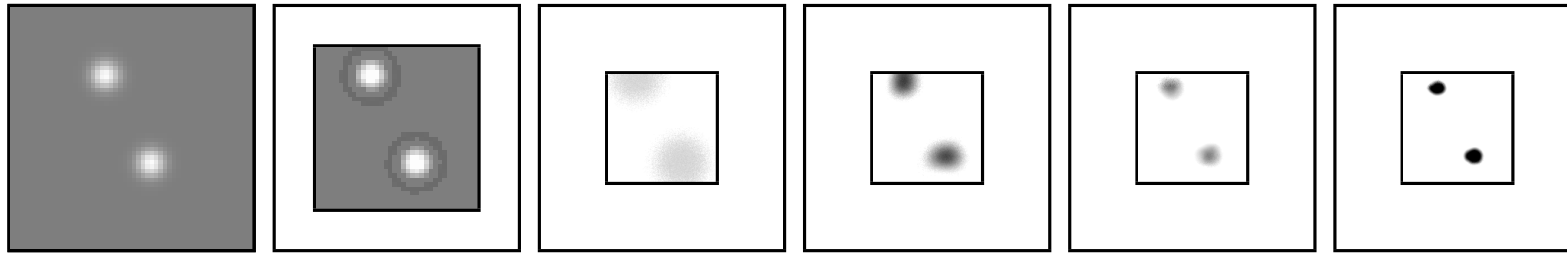
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<http://homepages.inf.ed.ac.uk/jbednar>

# Modeling Orientation

- Starting point: LISSOM retinotopy model
- Exactly the same architecture, different input pattern
- Three dimensions of variance: x, y, orientation
- How will that fit into a 2D map?

# Retinotopy input and response

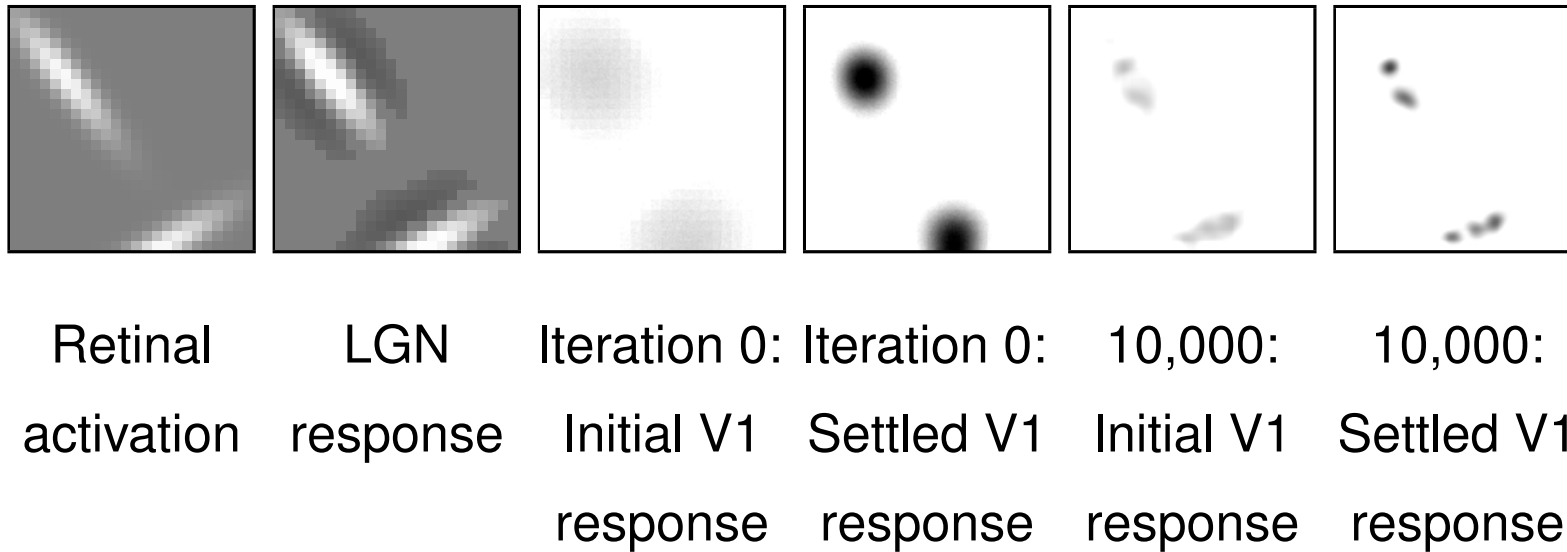


Retinal activation    LGN response    Iteration 0: Initial V1 response    Iteration 0: Settled V1 response    10,000: Initial V1 response    10,000: Settled V1 response

CMVC figure 4.4

(Reminder from previous slides)

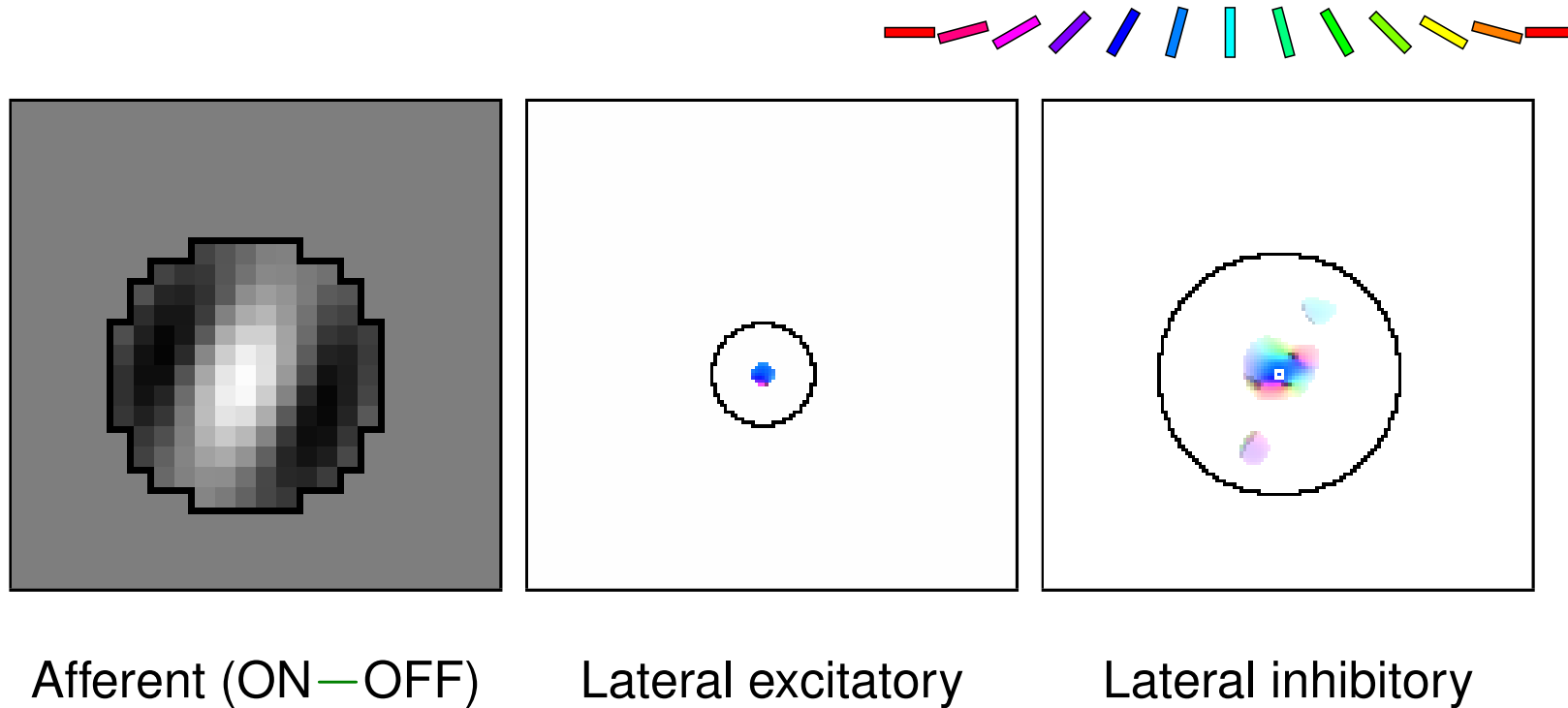
# Orientation input and response



CMVC figure 5.6

- Response before training similar to retinotopy case
- Response after training has multiple activity blobs per input pattern
- Final blobs are orientation-specific

# Self-organized V1 weights

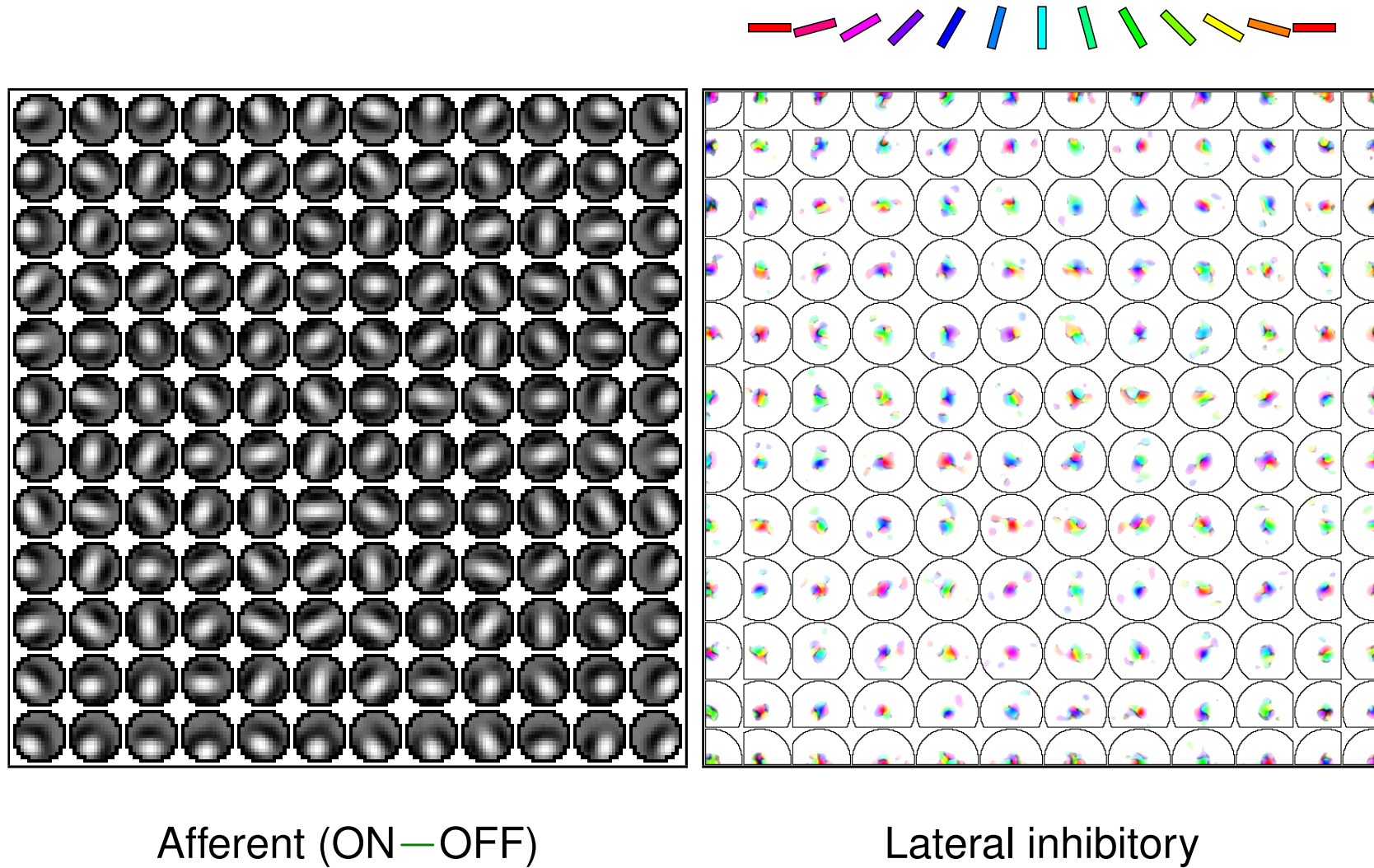


CMVC figure 5.7

Typical:

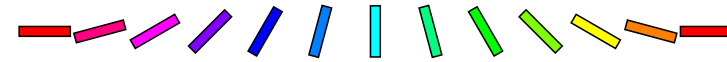
- Gabor-like afferent CF
- Nearly uniform short-range lateral excitatory
- Patchy, orientation-specific long-range lateral inhibitory

# Self-organized weights across V1

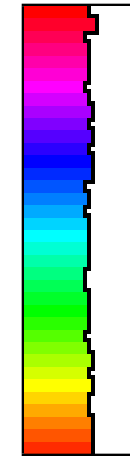
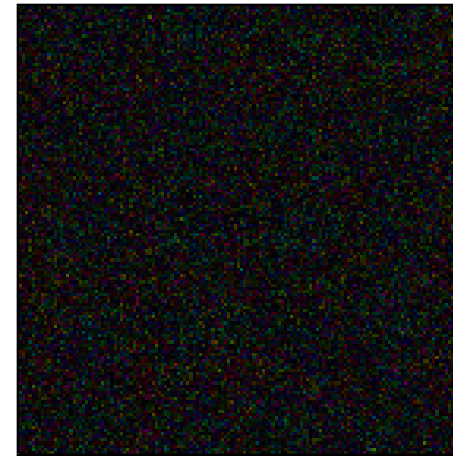
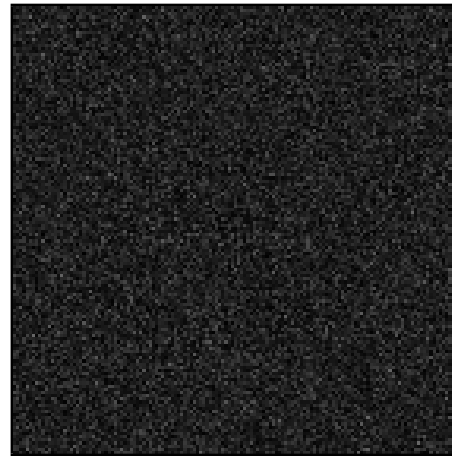
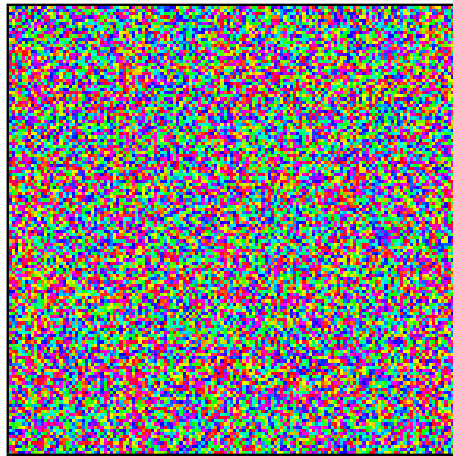


CMVC figure 5.8

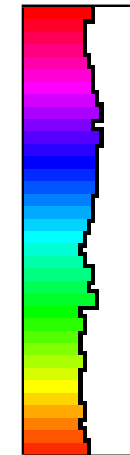
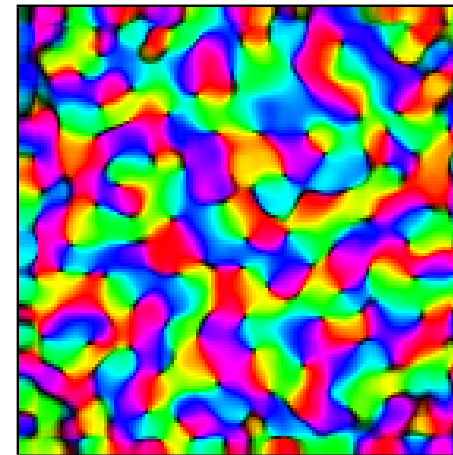
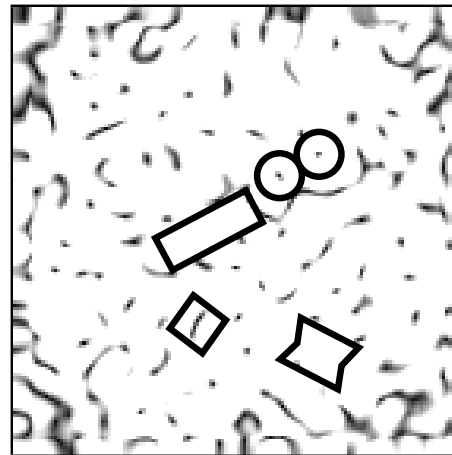
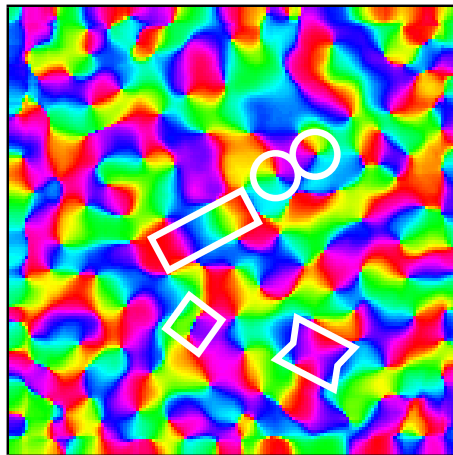
# OR map self-organization



Iteration 0



Iteration



OR preference

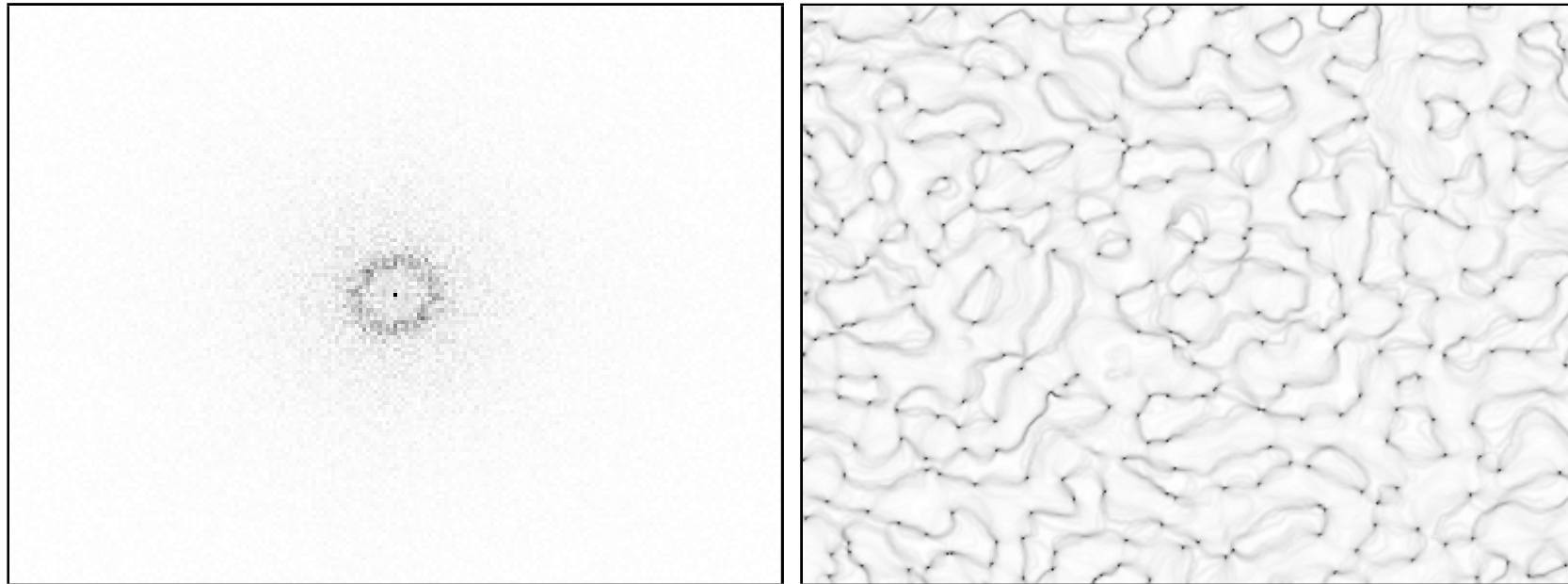
OR selectivity

OR preference &  
selectivity

OR H

CMVC figure 5.9

# Macaque ORmap: Fourier, gradient



CMVC figure 5.1

Fourier spectrum

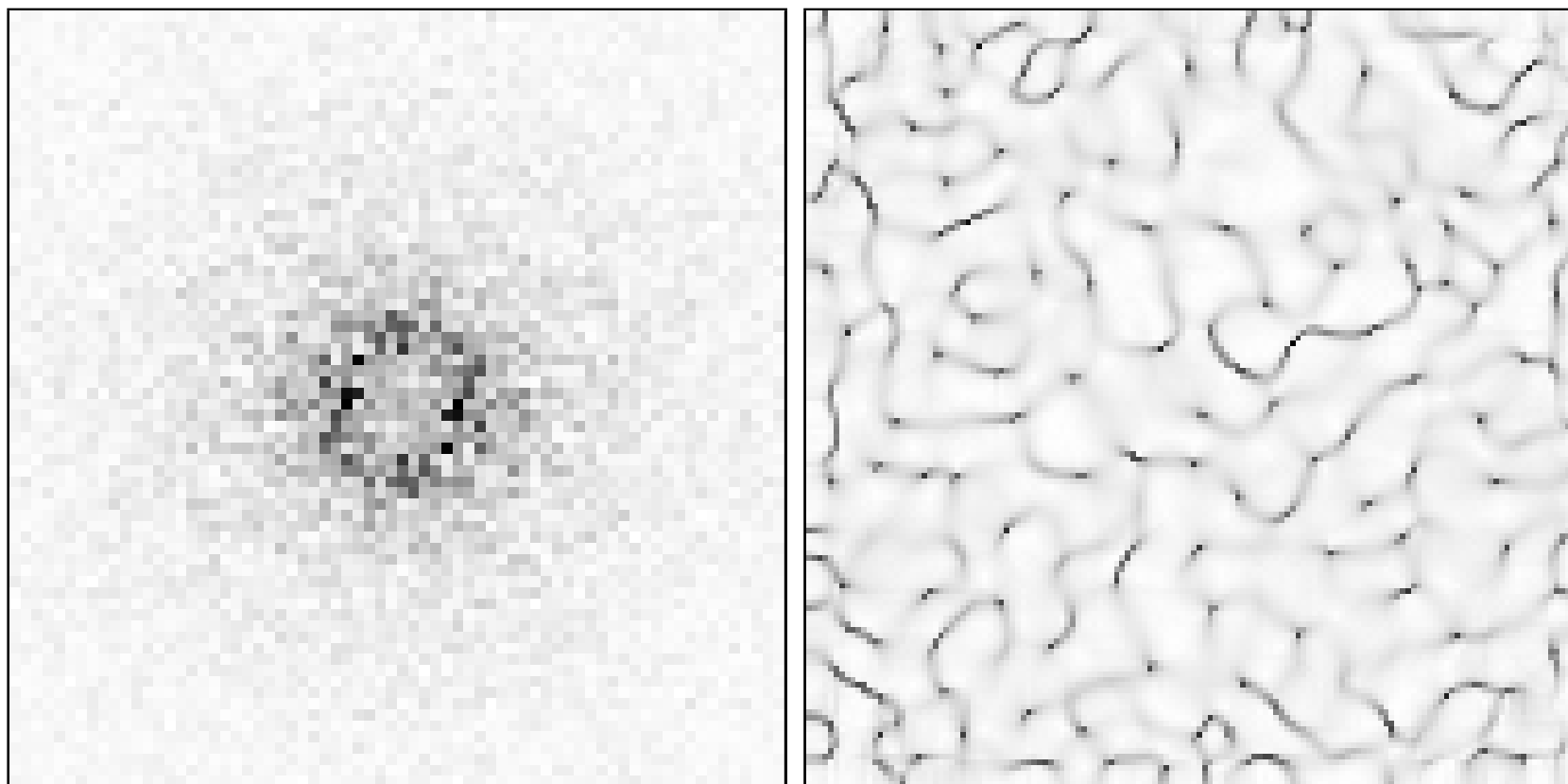
Gradient

In monkeys:

- Ring-shaped spectrum: repeats regularly in all directions
- High gradient at fractures, pinwheels.



# OR Map: Fourier, gradient



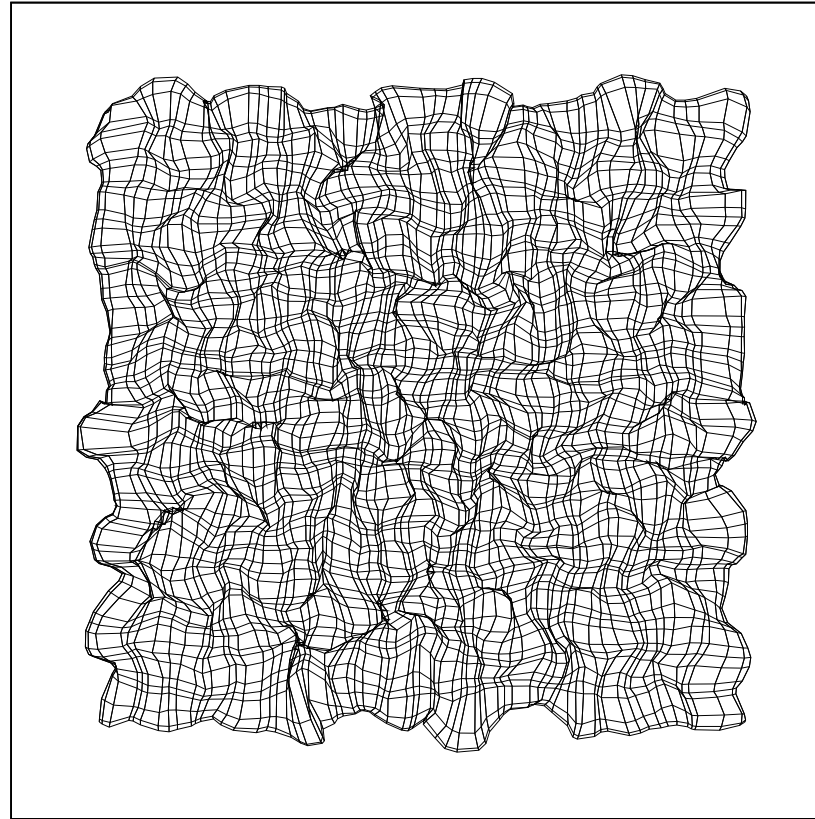
Fourier spectrum

Gradient

LISSOM model has similar spectrum, gradient

CMVC figure 5.10

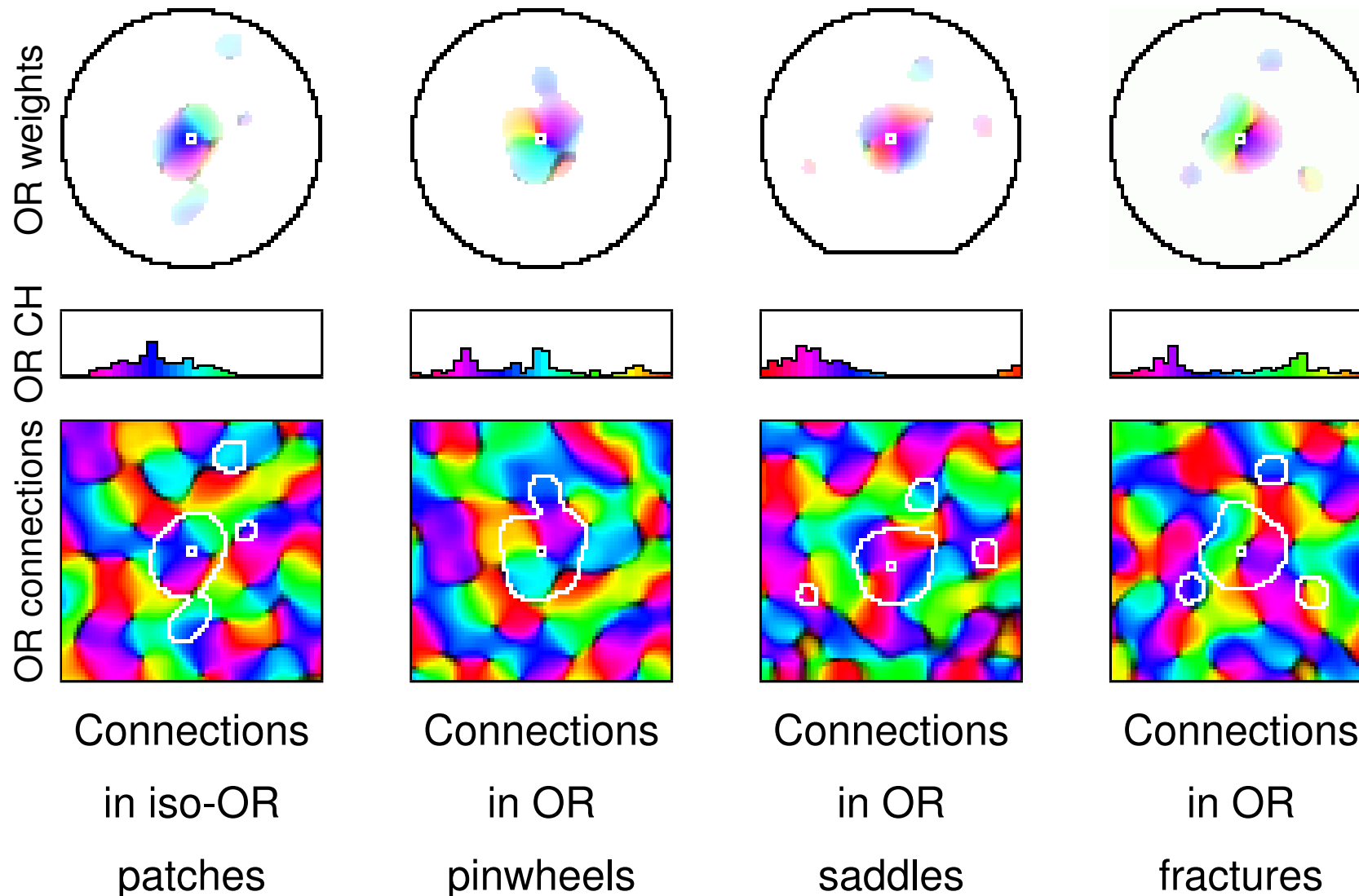
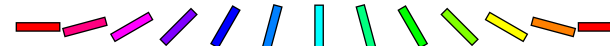
# OR Map: Retinotopic organization



CMVC figure 5.11

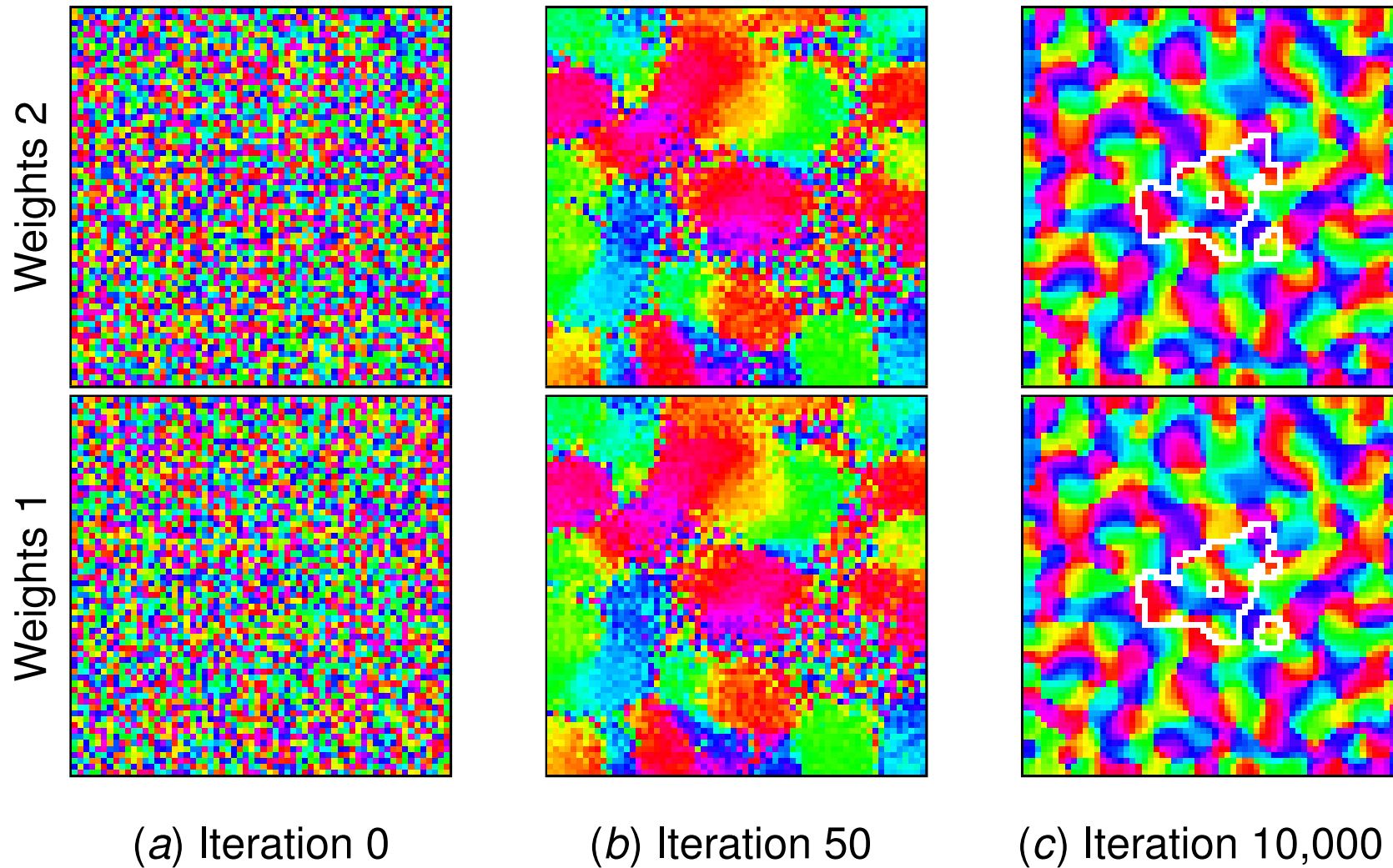
- Retinotopy is distorted locally by orientation prefs
- Matches distortions found in animal maps?

# OR Map: Lateral connections



CMVC figure 5.12

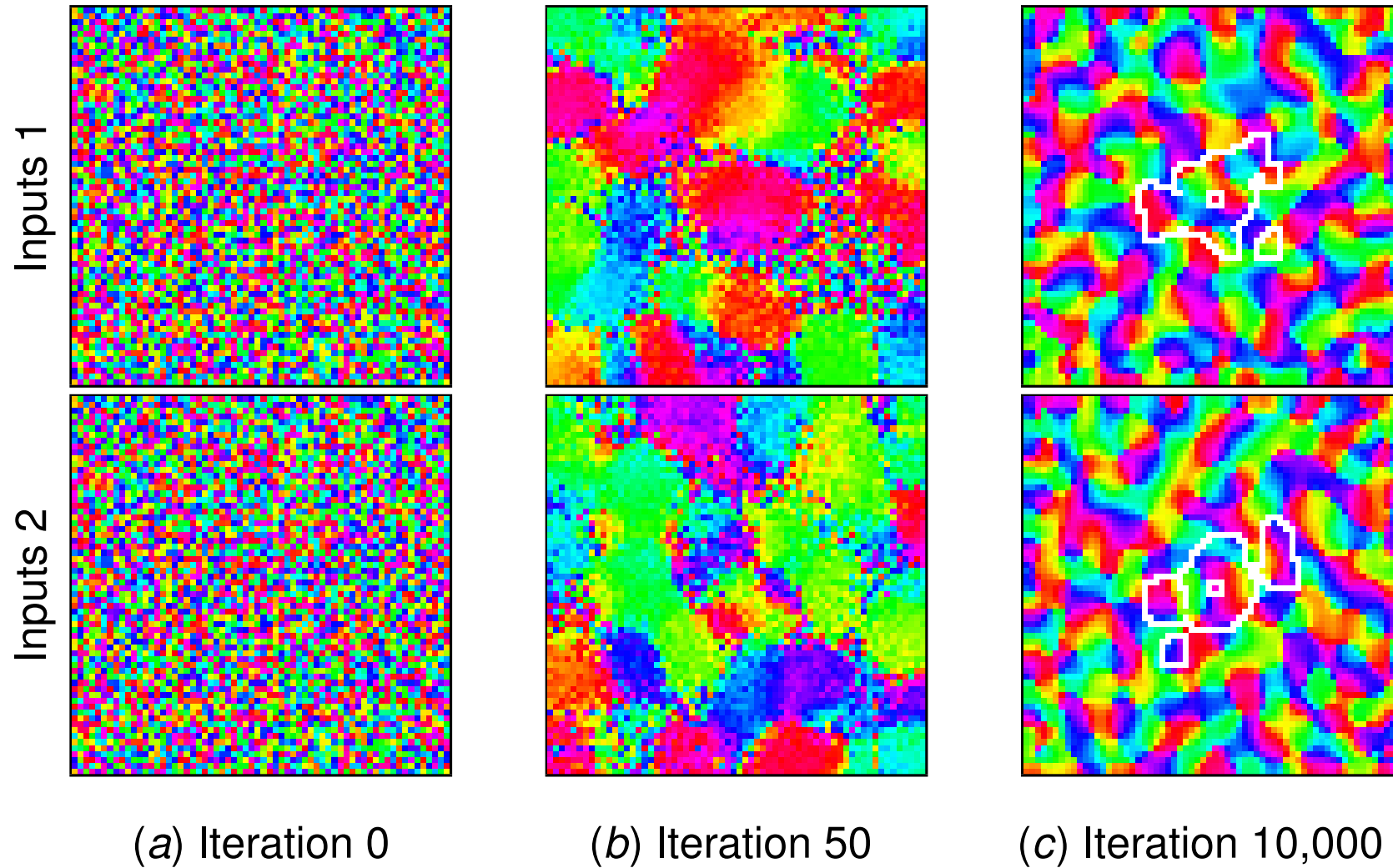
# Effect of initial weights



CMVC figure 8.5

Changing weights doesn't change map folding pattern.

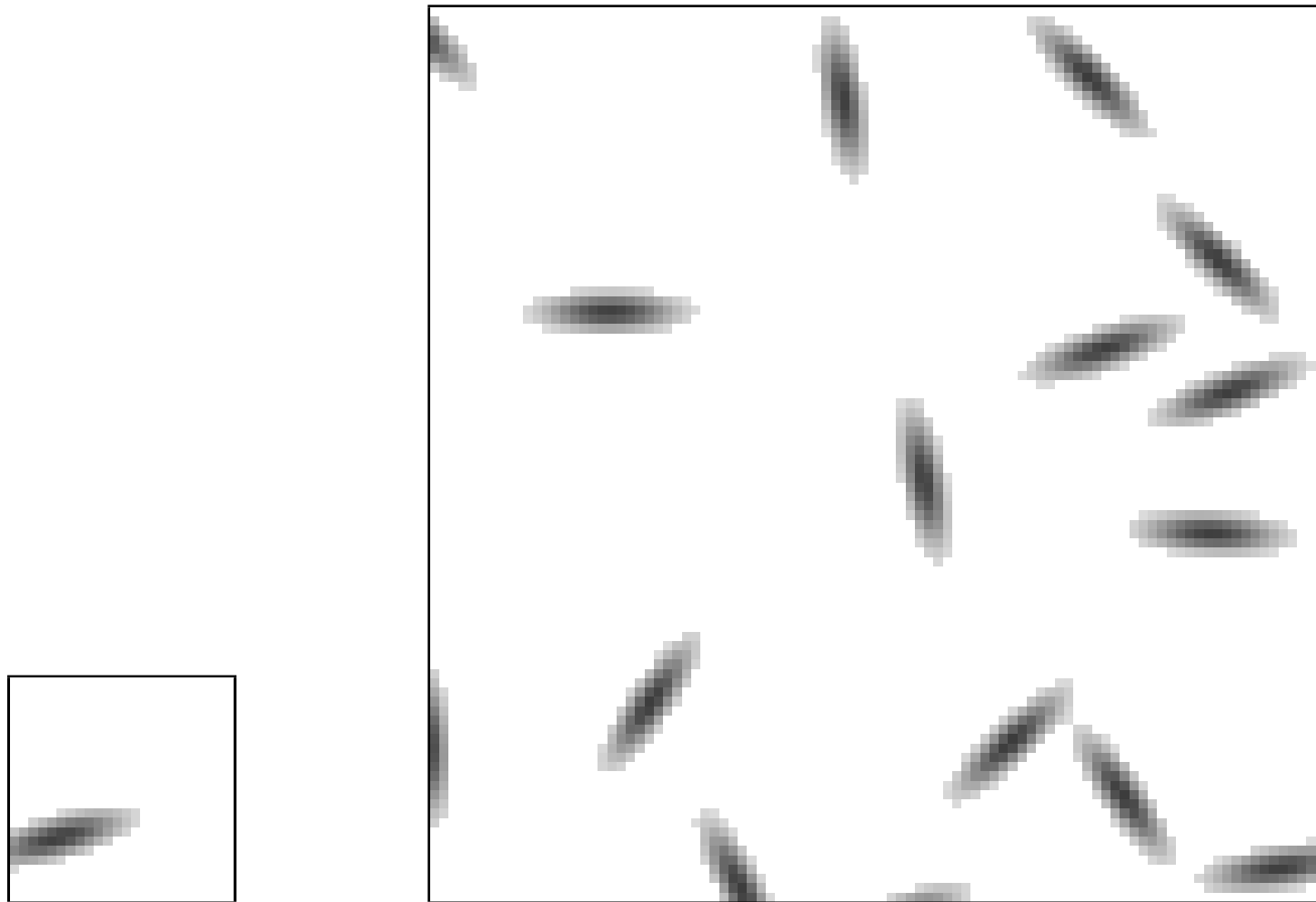
# Effect of input streams



CMVC figure 8.5

Changing inputs changes entire pattern.

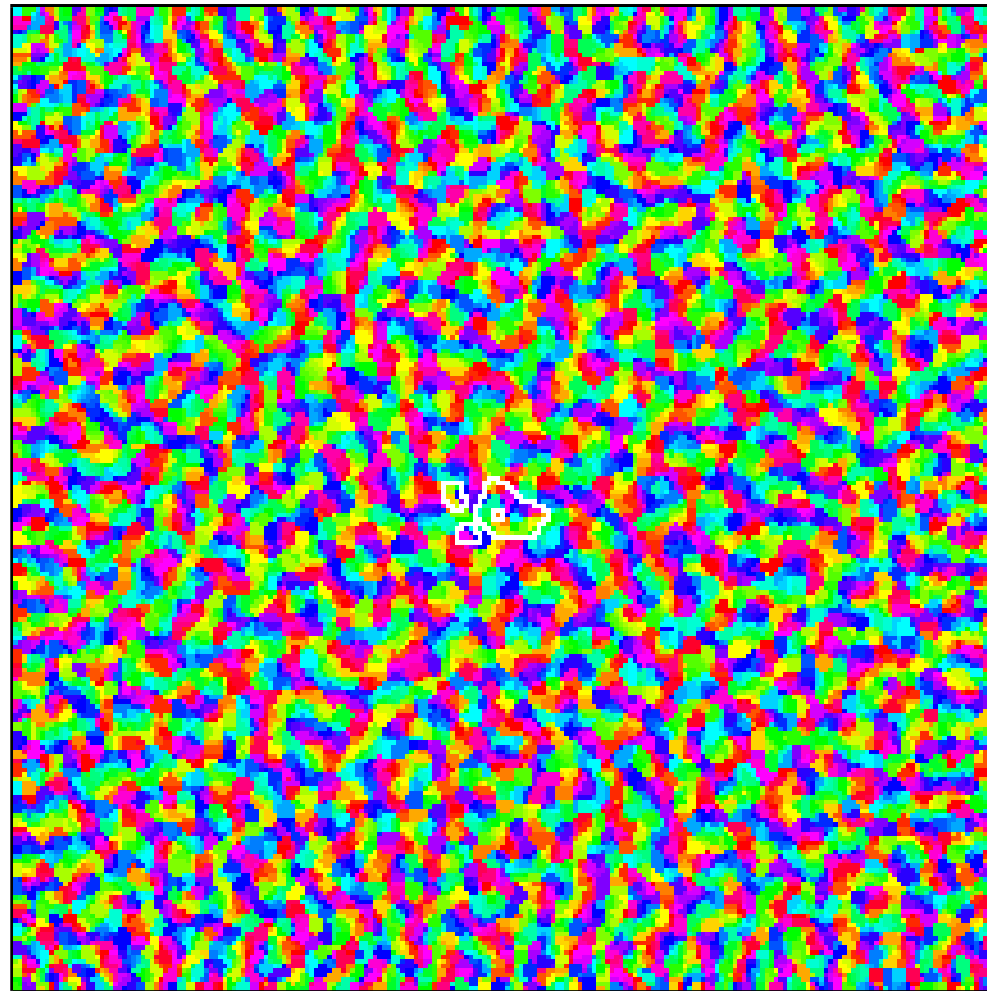
# Scaling retinal and cortical area



CMVC figure 15.1a,b

(a) Original retina:  $R = 24$     (b) Retinal area scaled by 4.0:  
 $R = 96$

# Scaling retinal and cortical area



(c) Original V1:

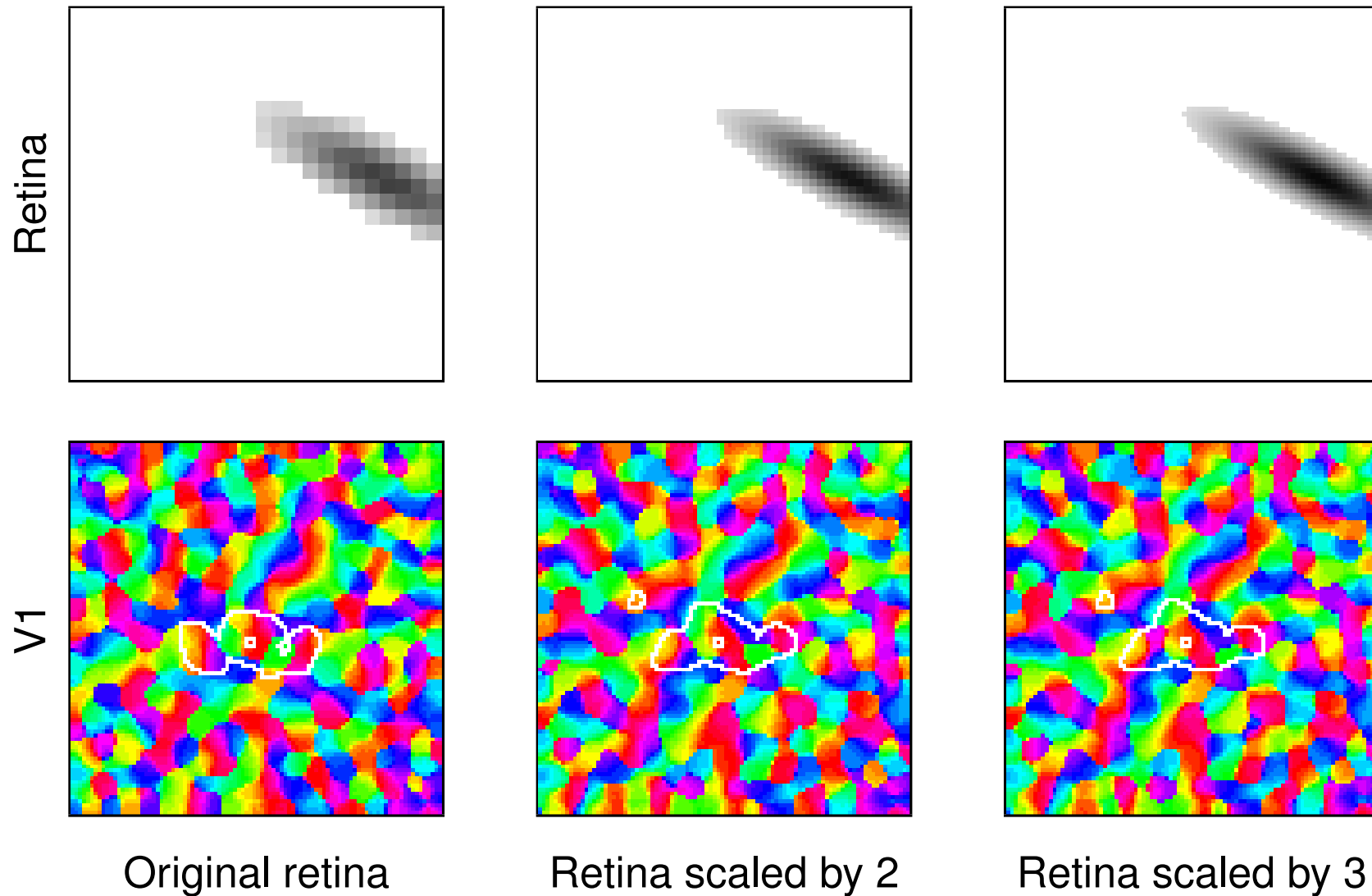
$N = 54$ , 0.4 hours, 8 MB

(d) V1 area scaled by 4.0:

$N = 216$ , 9 hours, 148 MB

CMVC figure 15.1c,d

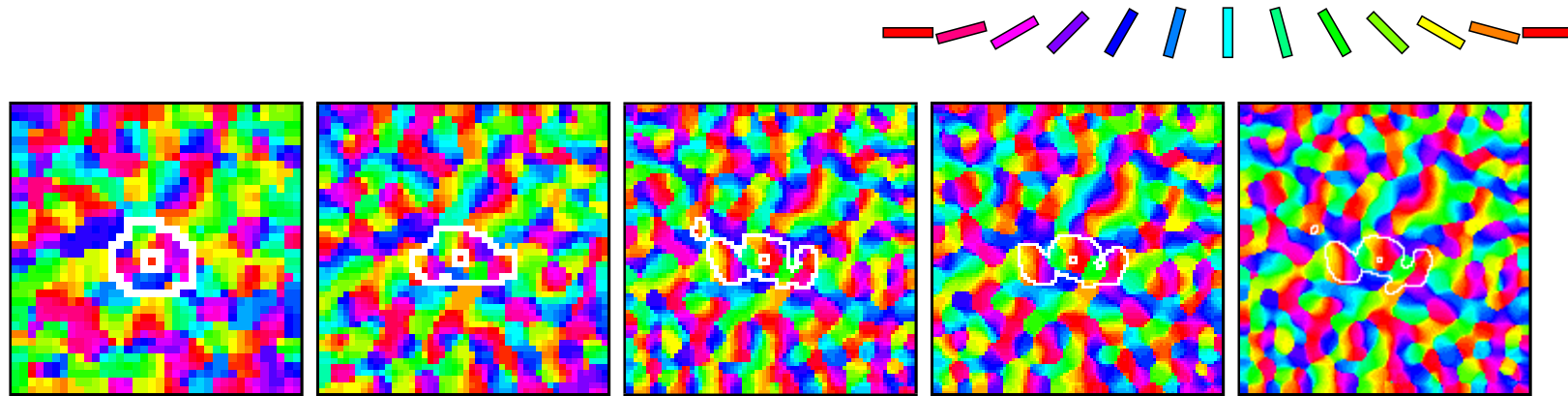
# Scaling retinal density



CMVC figure 15.2



# Scaling cortical density

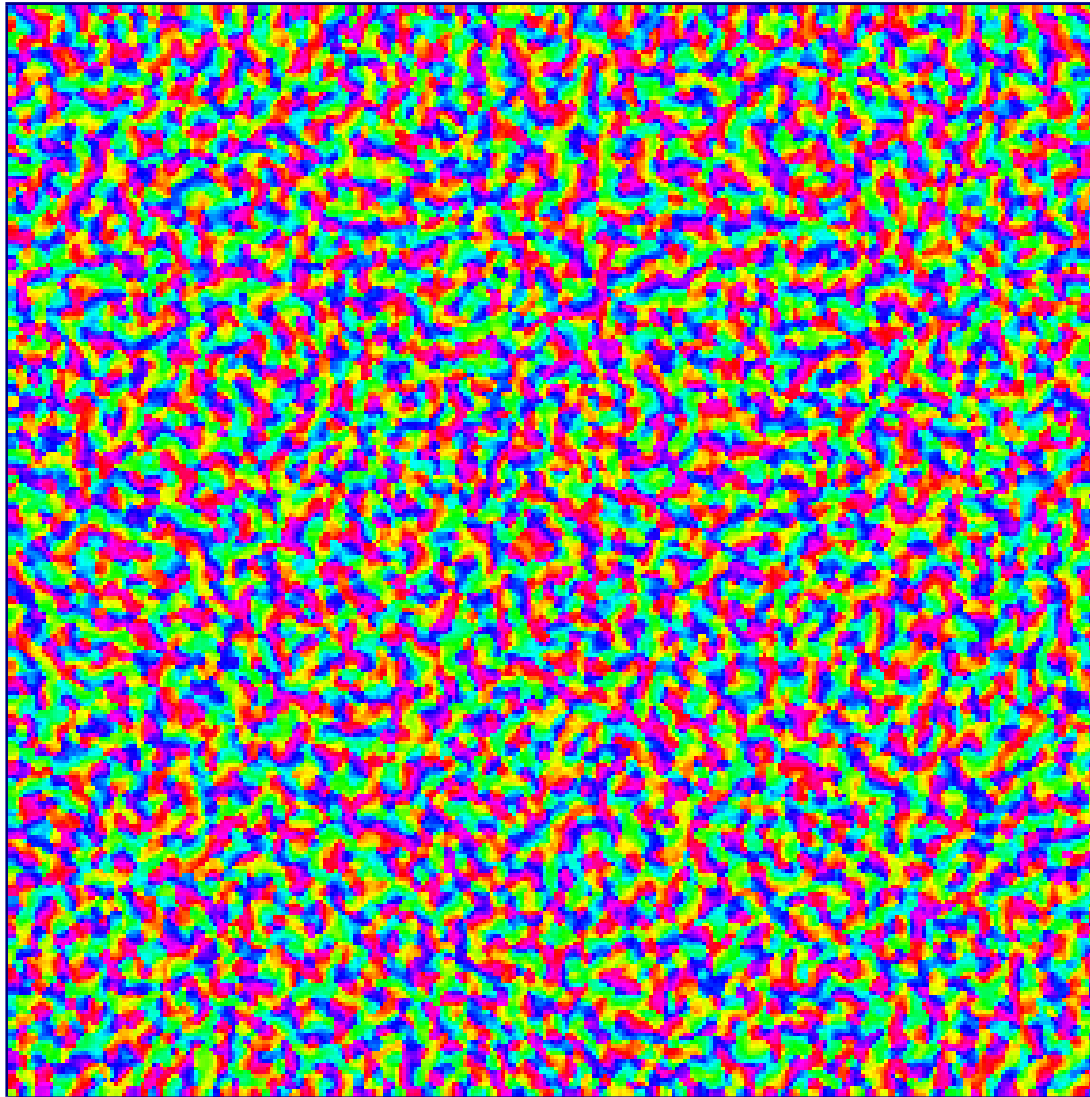


(a)  $36 \times 36$ : 0.17 hours, 2.0 MB  
(b)  $48 \times 48$ : 0.32 hours, 5.2 MB  
(c)  $72 \times 72$ : 0.77 hours, 22 MB  
(d)  $96 \times 96$ : 1.73 hours, 65 MB  
(e)  $144 \times 144$ : 5.13 hours, 317 MB

CMVC figure 15.3

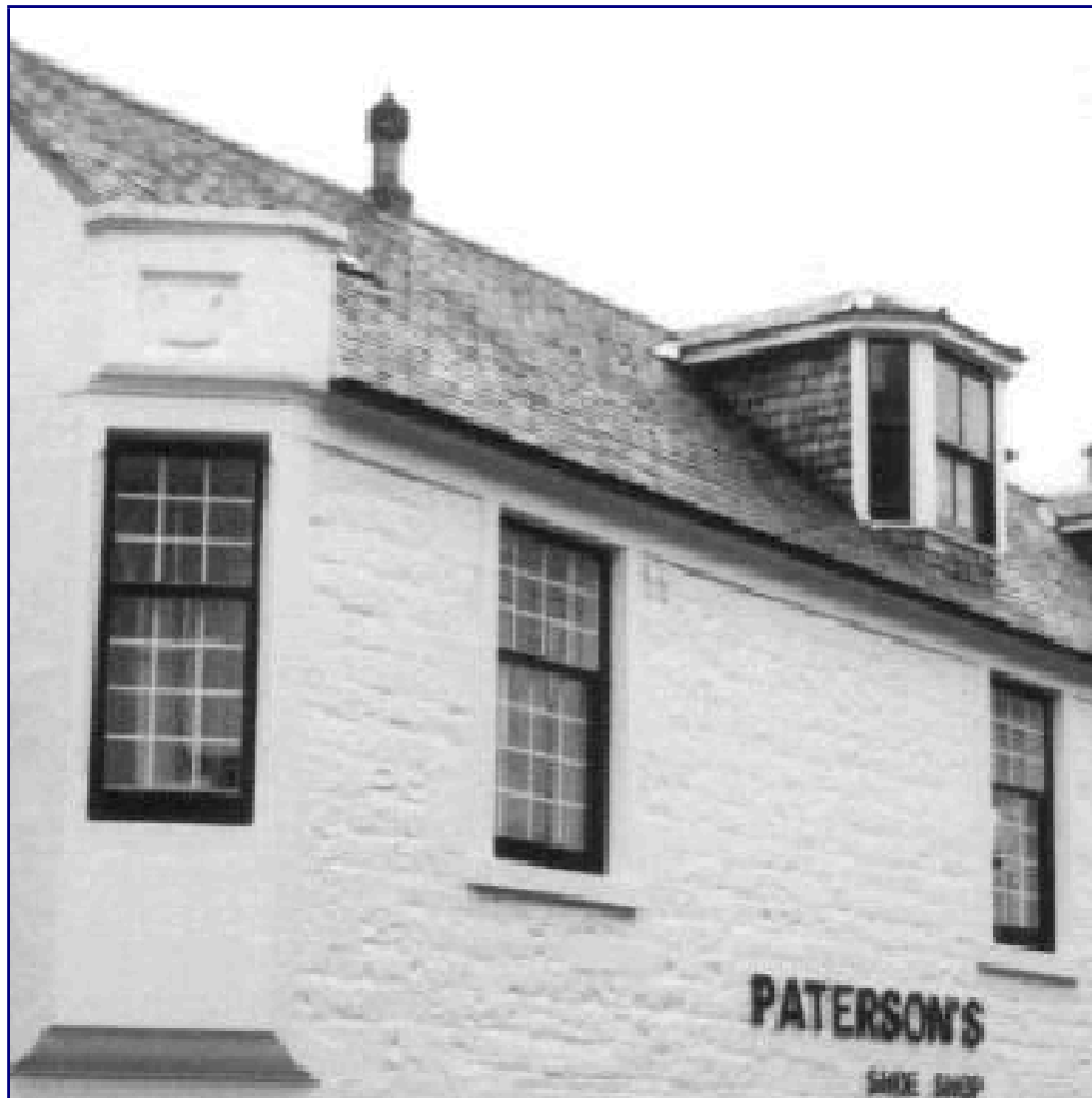
Above minimum density (due to lateral radii),  
density not crucial for organization

# Full-size V1 Map



- Map scaled to cover most of visual field
- Allows testing with full-size images
- 30 million connections

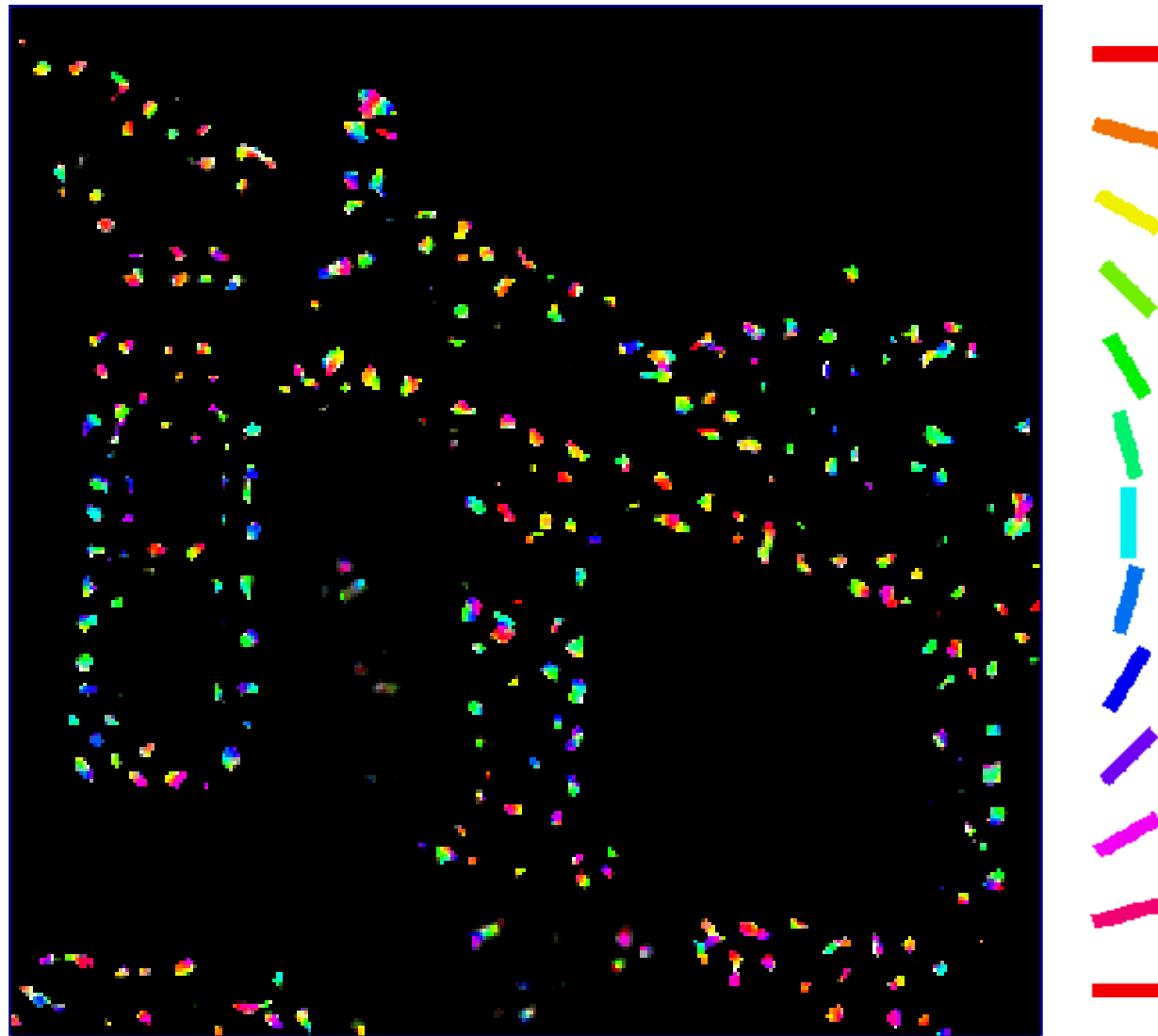
# Sample Image



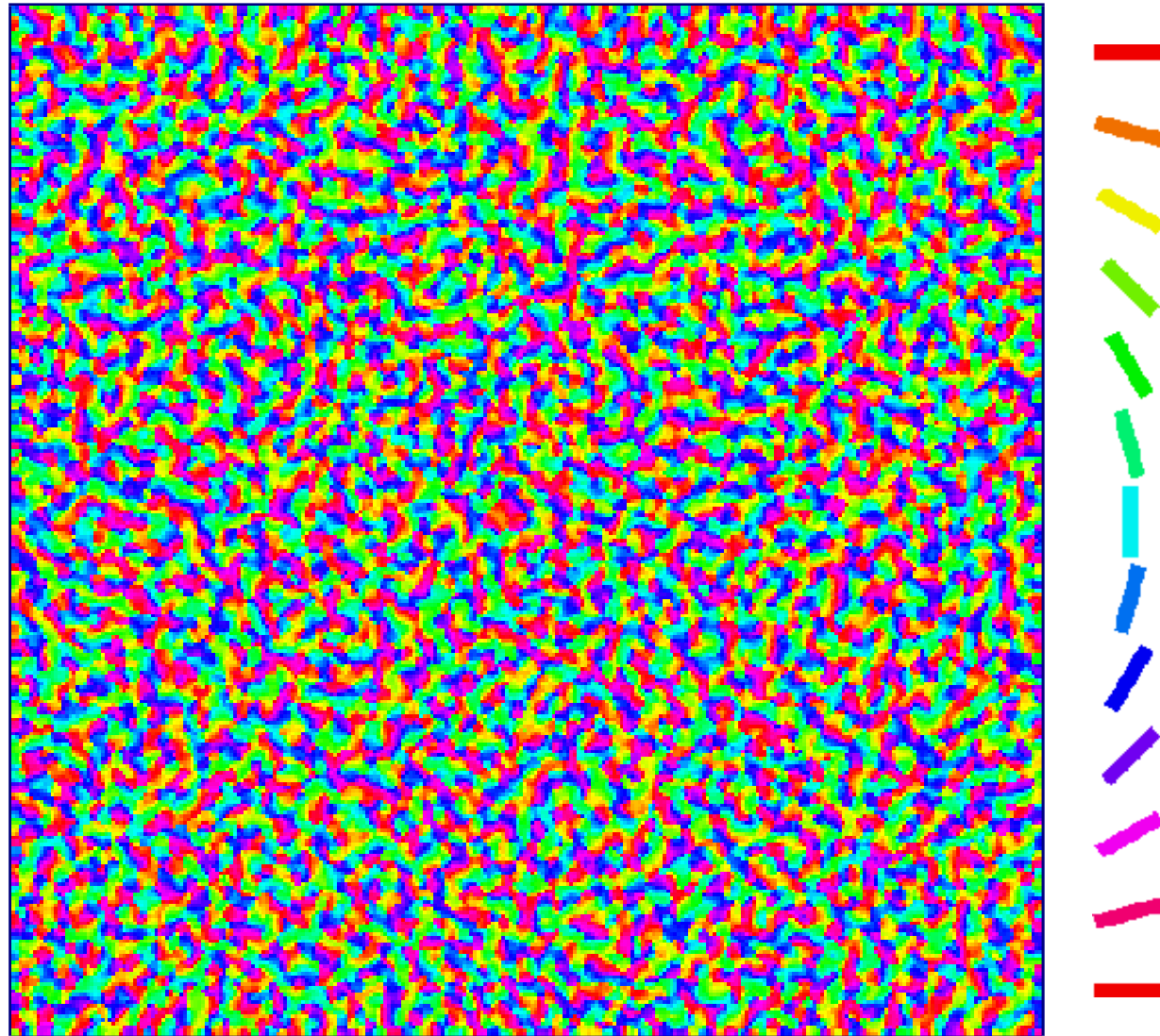
# RGC/LGN Response



# V1 Response with $\gamma_n$



# V1 Orientation Map



# Afferent normalization

LISSOM mechanism for contrast invariant tuning:

$$s_{ij} = \frac{\gamma_A \left( \sum_{\rho ab} \xi_{\rho ab} A_{\rho ab, ij} \right)}{1 + \gamma_n \left( \sum_{\rho ab} \xi_{\rho ab} \right)}, \quad (1)$$

$\xi_{\rho ab}$ : activation of unit  $(a, b)$  in afferent CF  $\rho$  of neuron  $(i, j)$

$A_{ab, ij}$  is the corresponding afferent weight

$\gamma_A, \gamma_n$  are constant scaling factors

GCAL achieves similar results with lateral inhibition in RGC/LGN

# RGC/LGN response to large image



Retinal activation



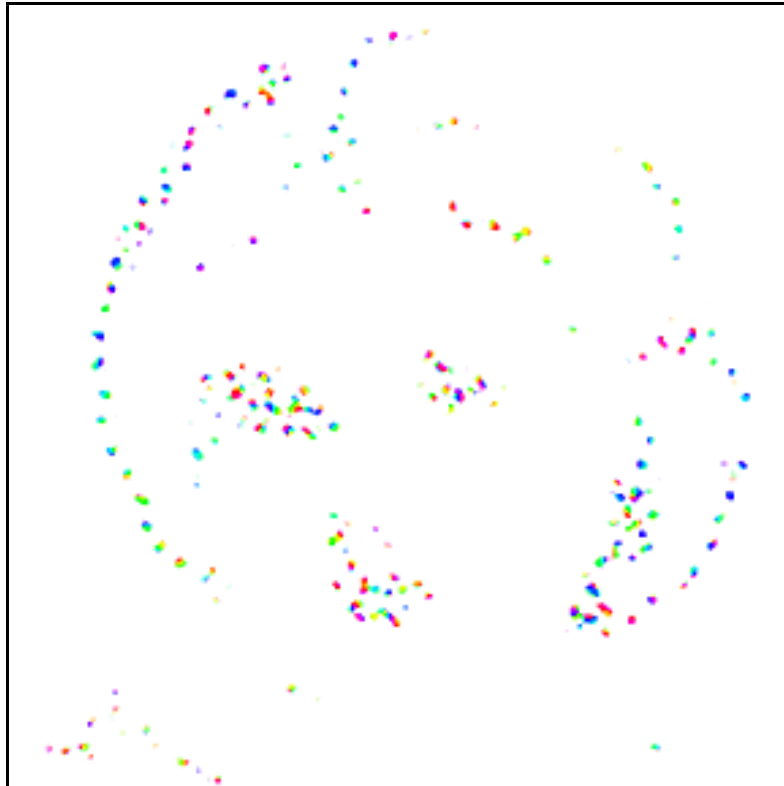
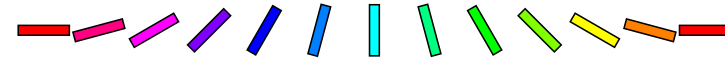
LGN response

RGC/LGN responds to most of the visible contours

CMVC figure 8.2a,b

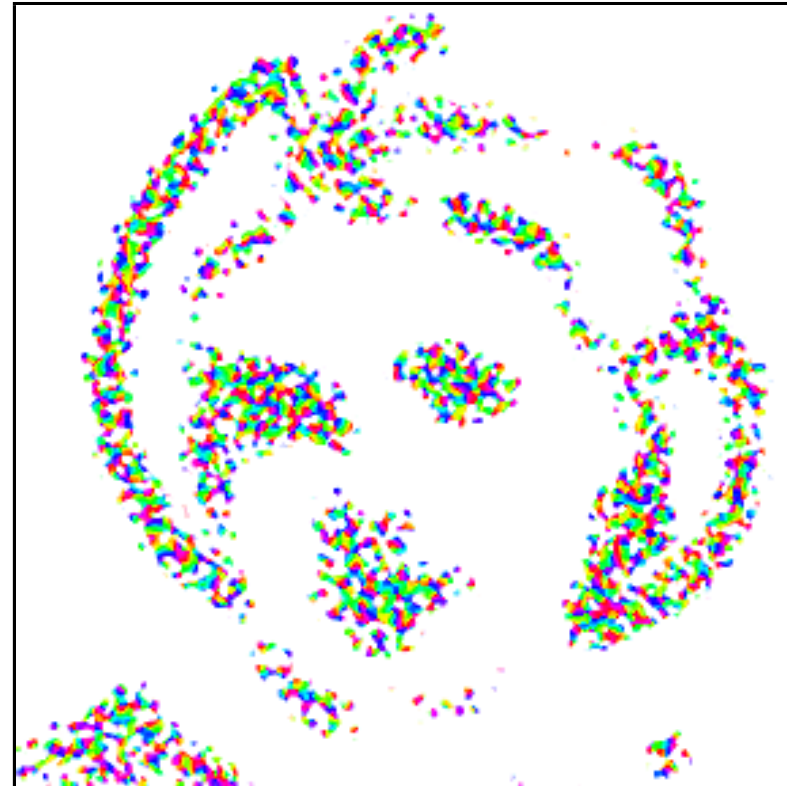


# V1 without afferent normalization



V1 response:

$$\gamma_n = 0, \gamma_A = 3.25$$



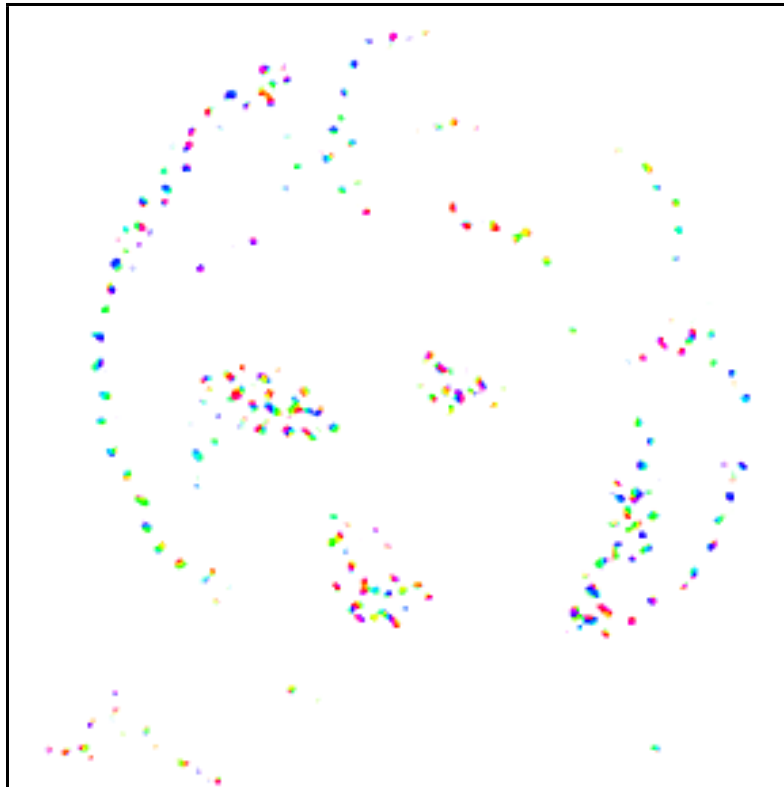
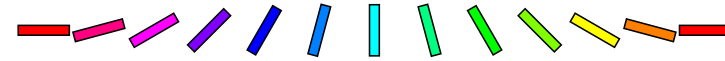
V1 response:

$$\gamma_n = 0, \gamma_A = 7.5$$

Cannot get selective response to all contours

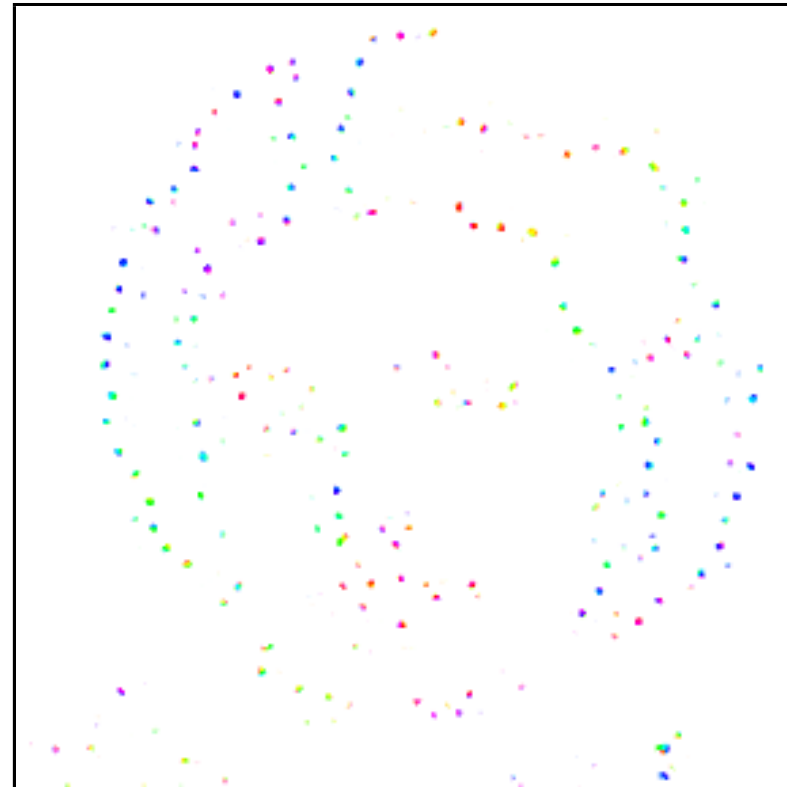
CMVC figure 8.2c-e

# V1 with afferent normalization



V1 response:

$$\gamma_n = 0, \gamma_A = 3.25$$



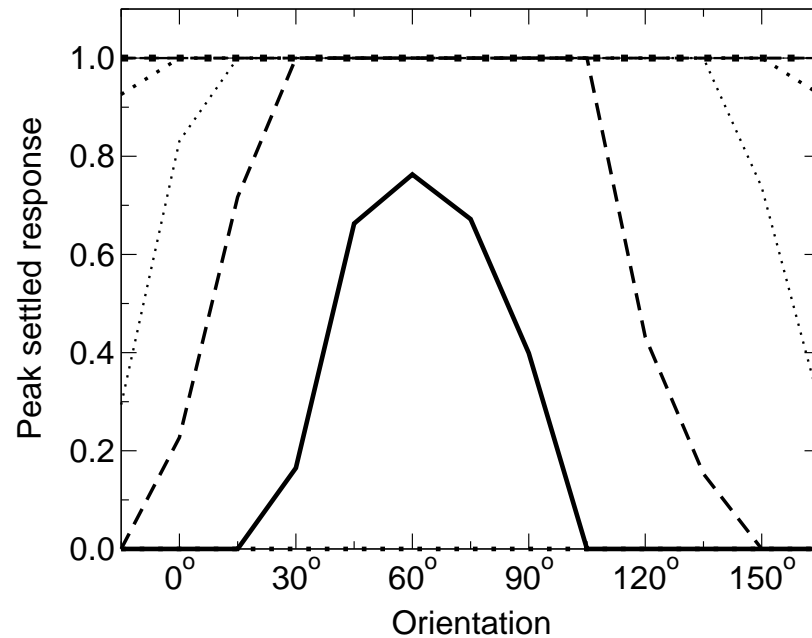
V1 response:

$$\gamma_n = 80, \gamma_A = 30$$

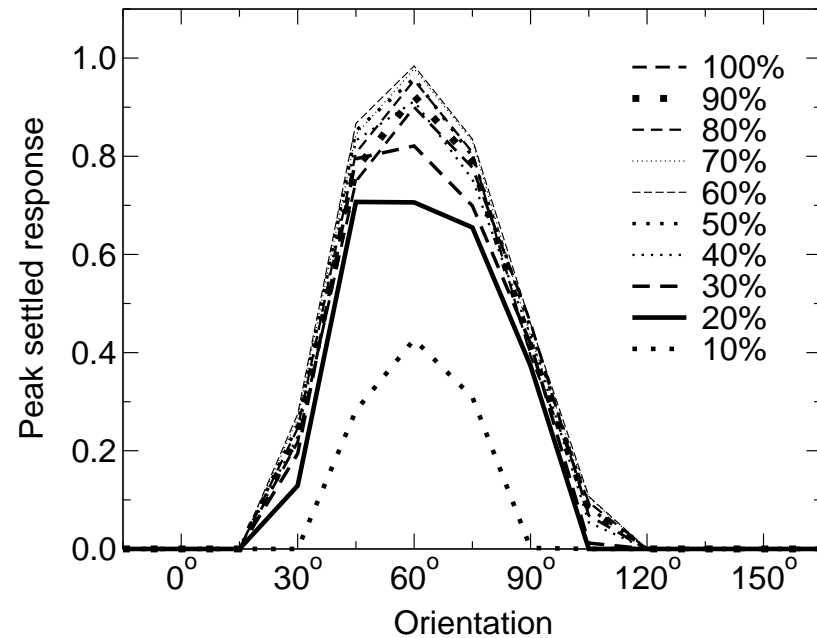
Responds based on contour, not contrast

CMVC figure 8.2c-e

# Tuning with afferent normalization



$$\gamma_n = 0, \gamma_A = 3.25$$



$$\gamma_n = 80, \gamma_A = 30$$

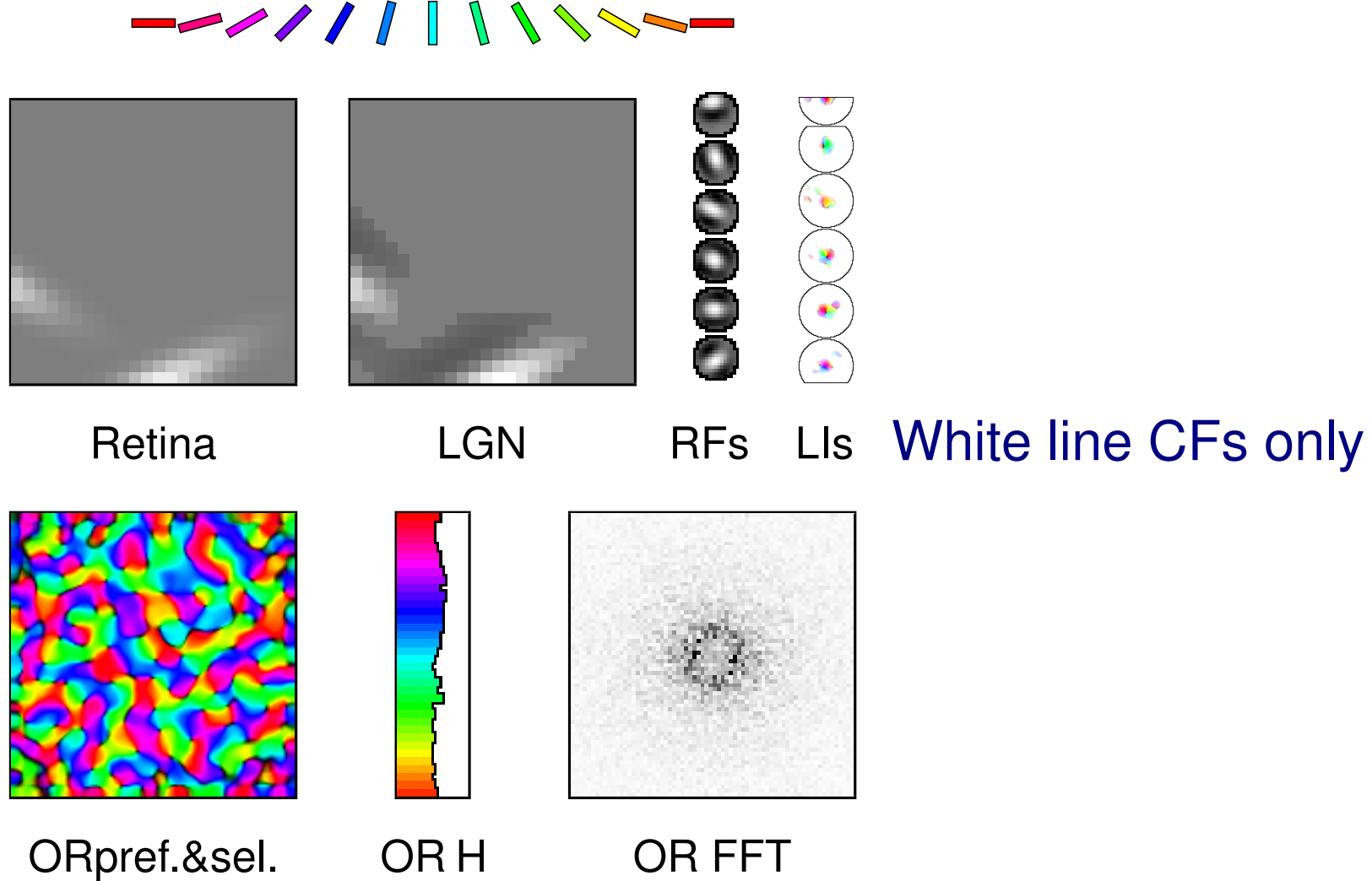
CMVC figure 8.3

Sine grating tuning curve:

- Without  $\gamma_n$ : selectivity lost as contrast increases
- With  $\gamma_n$ : always orientation-specific

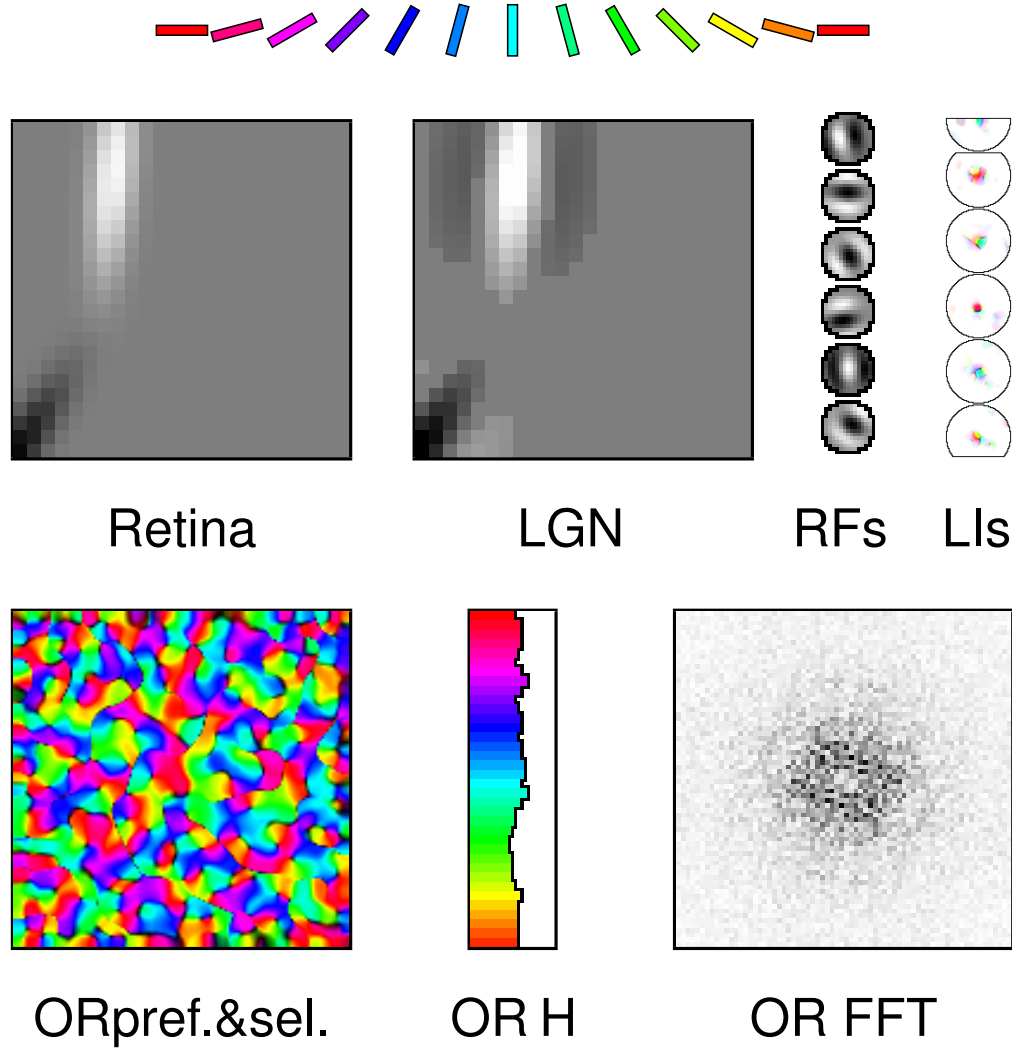
# OR Map: Gaussian

CMVC figure 5.13



# OR Map: +/- Gaussian

CMVC figure 5.13

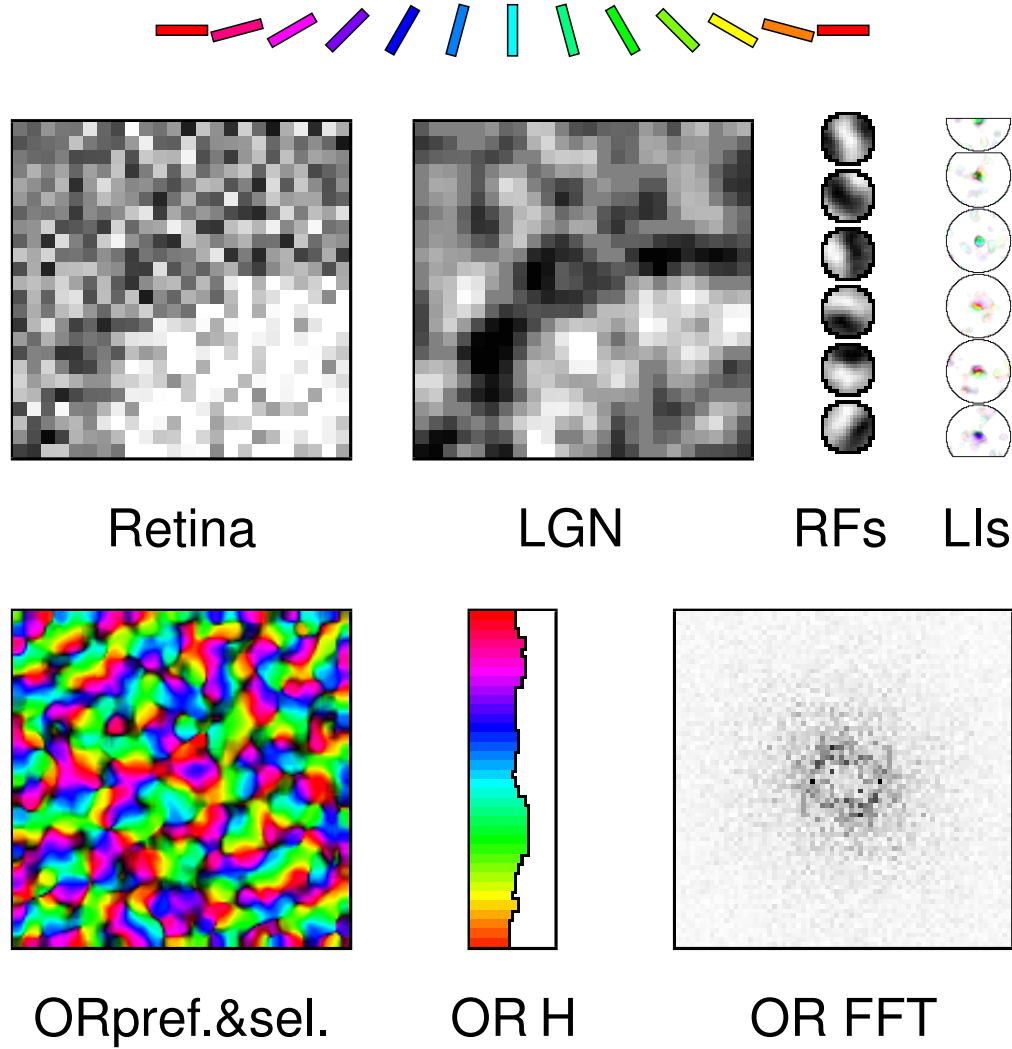


White or black  
line CFs

OR map disrupted  
due to phase  
columns

# OR Map: Retinal wave model

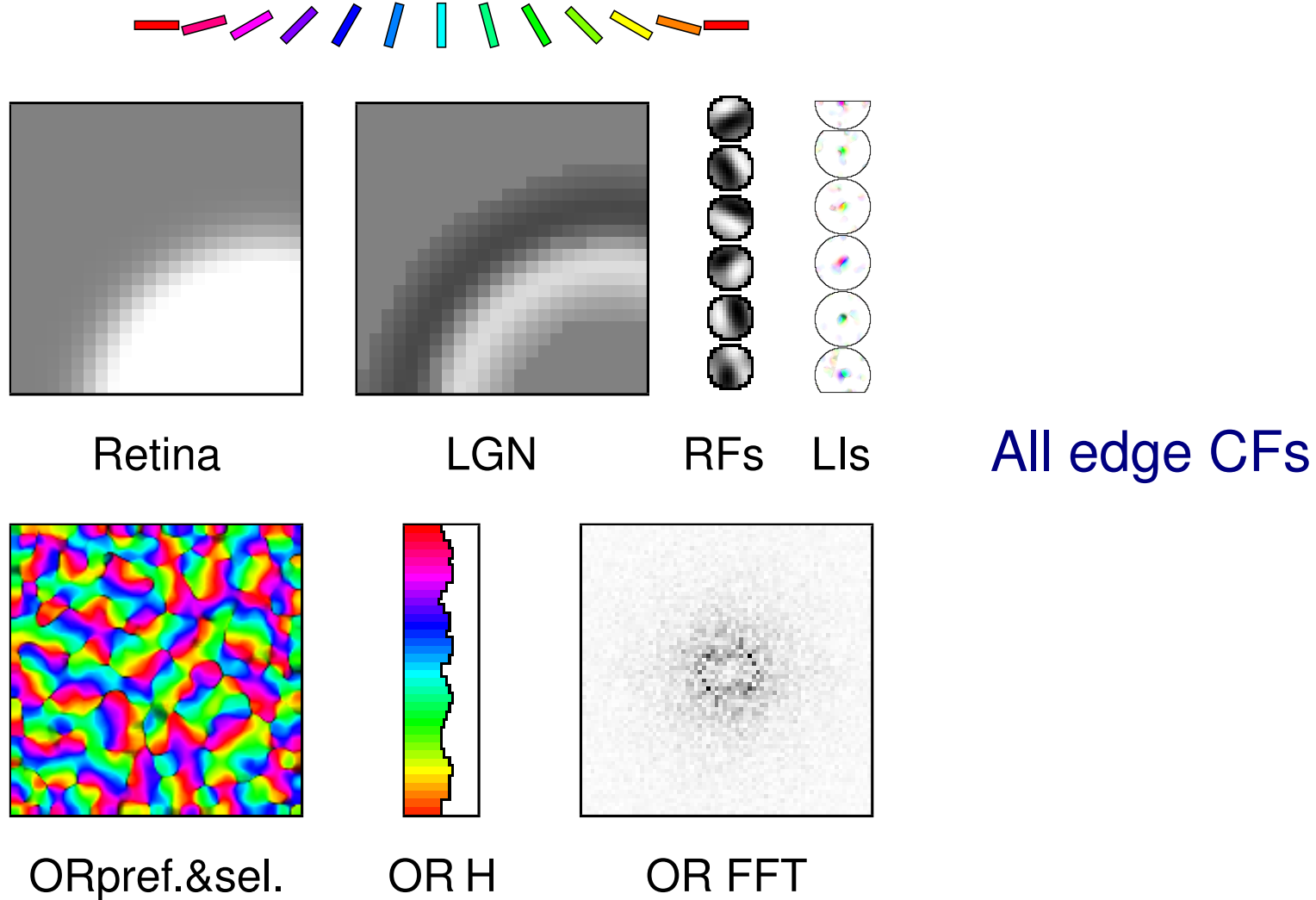
CMVC figure 5.13



Some line, mostly edge CFs

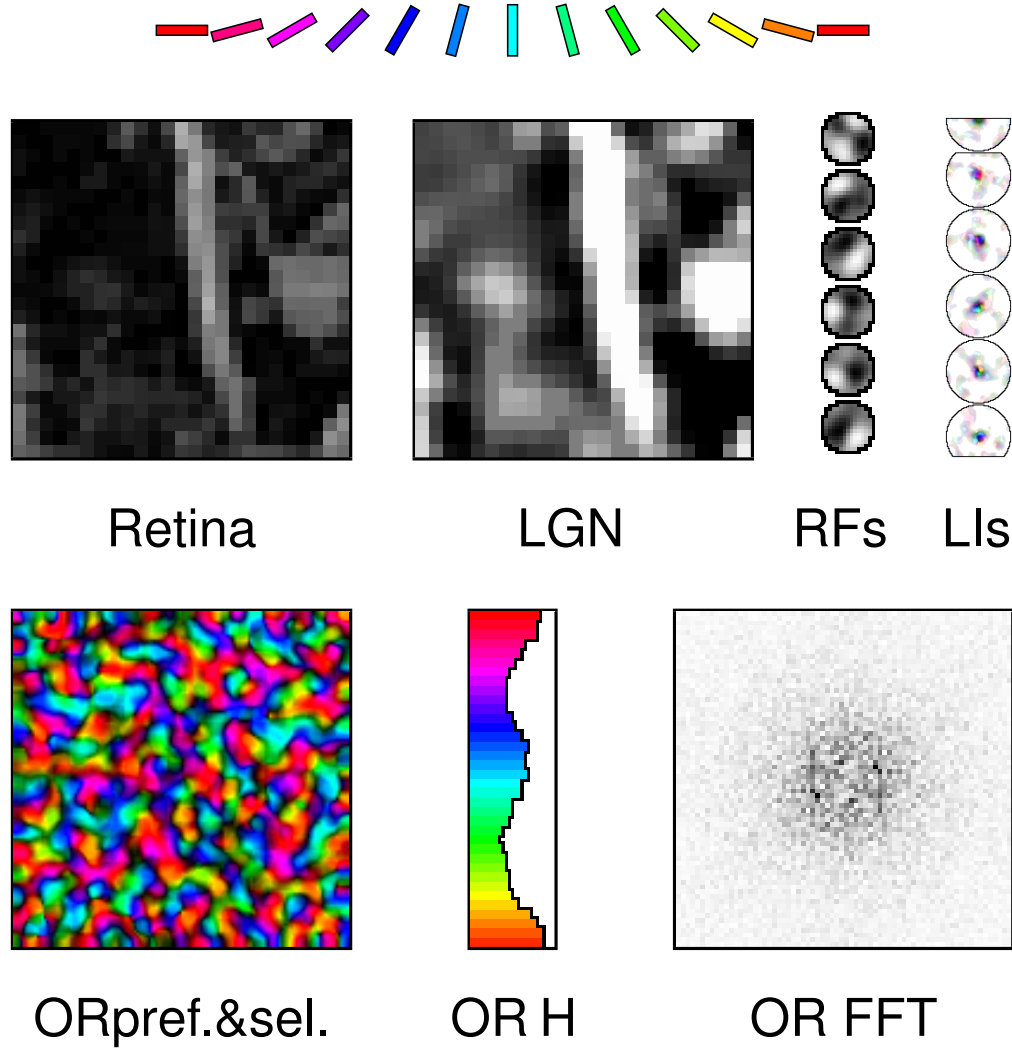
# OR Map: Smooth disks

CMVC figure 5.13



# OR Map: Natural images

CMVC figure 5.13



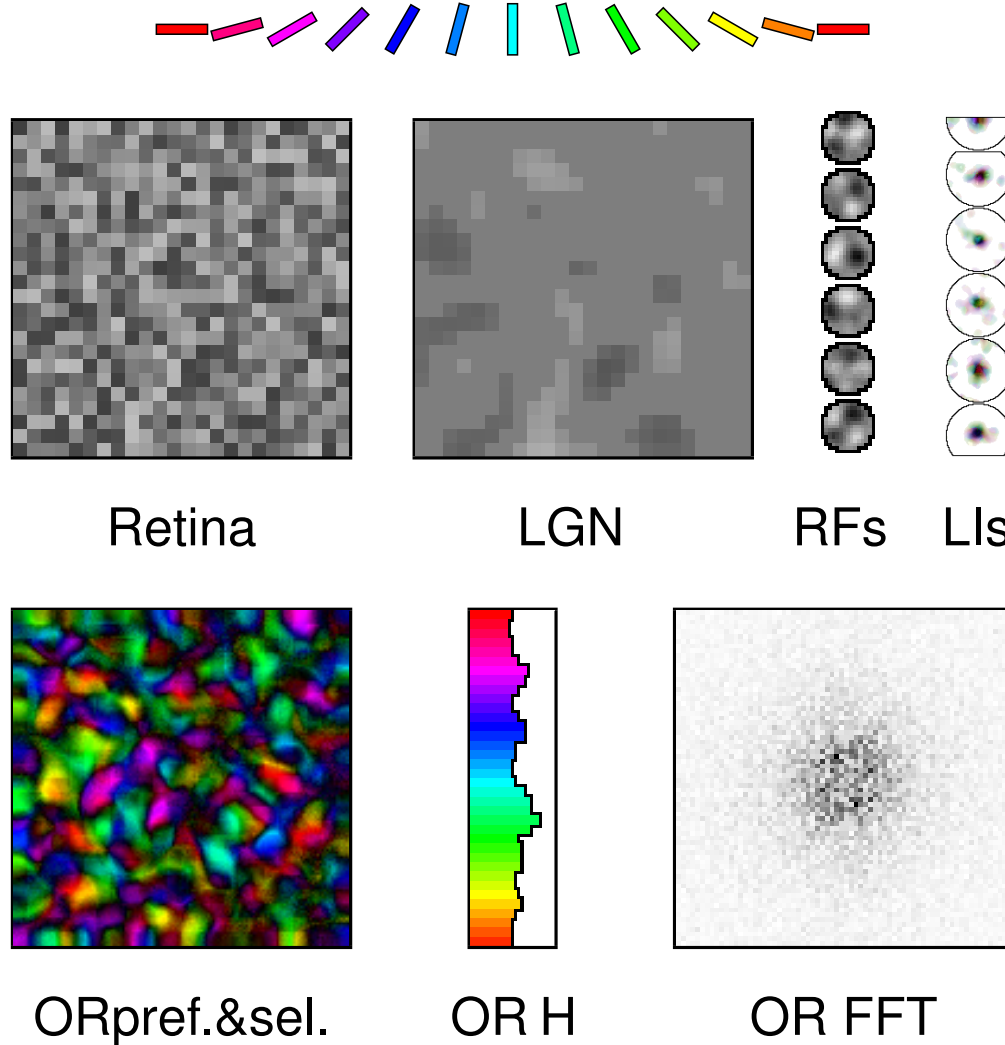
All types of CFs  
Longer range lateral weights

Histogram:  
horizontal, vertical bias



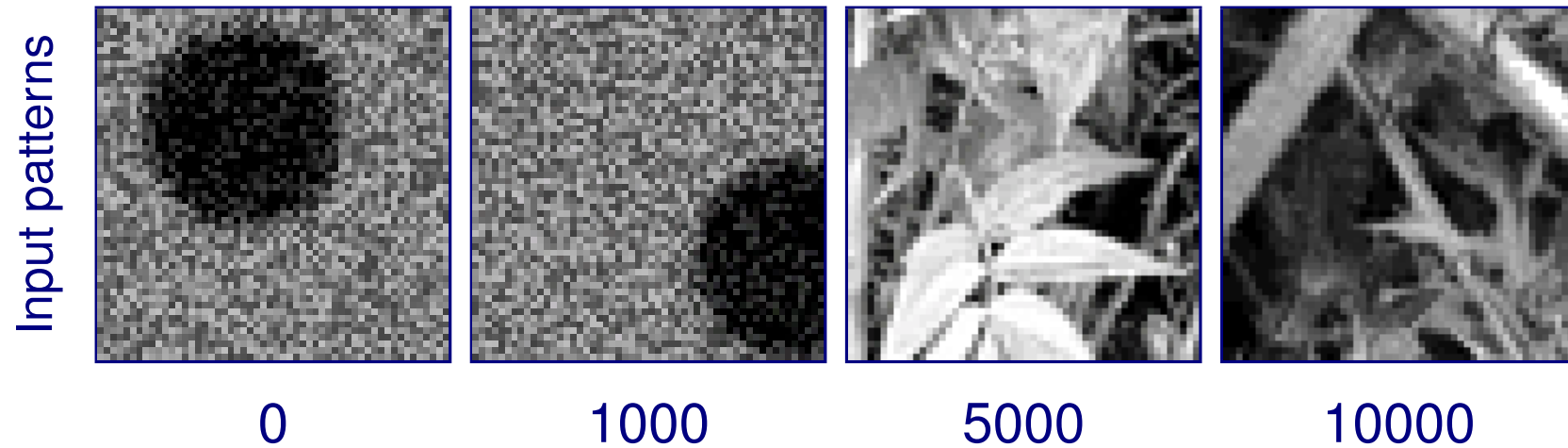
# OR Map: Uniform noise

CMVC figure 5.13



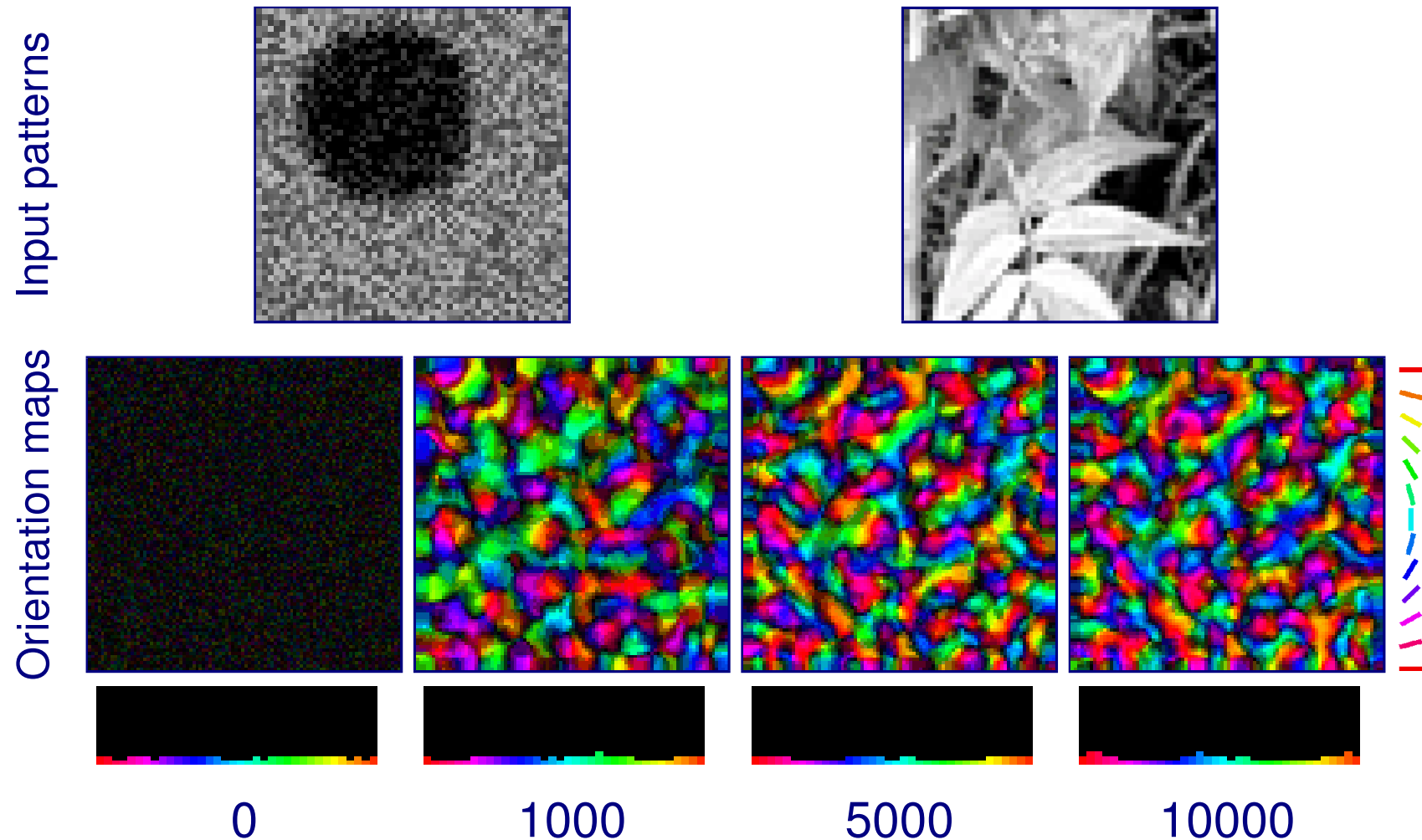
Relatively  
unselective CFs

# Modeling pre/post-natal phases



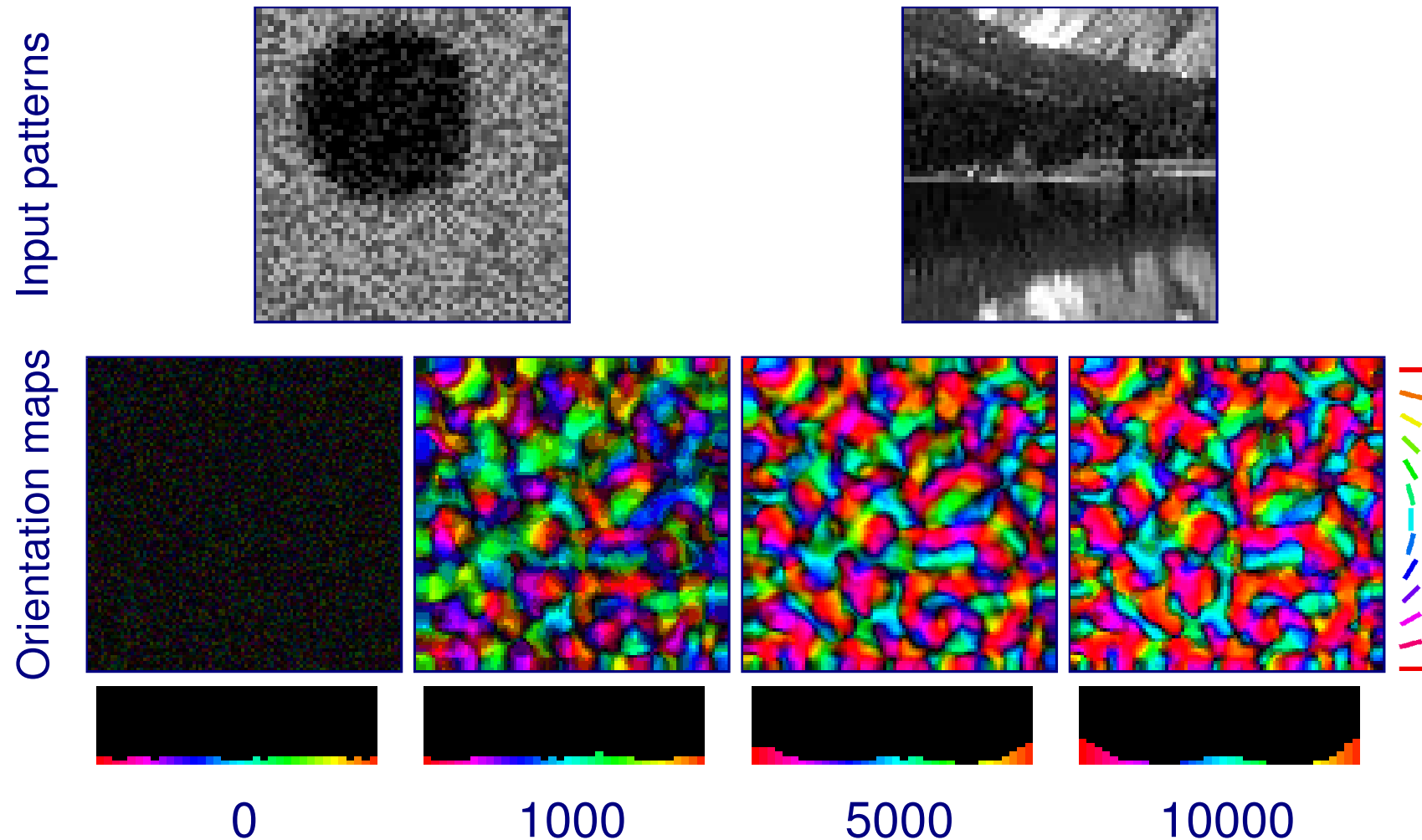
- **Prenatal:** internal activity
- **Postnatal:** natural images (Shouval et al. 1996)

# Pre/post-natal V1 development



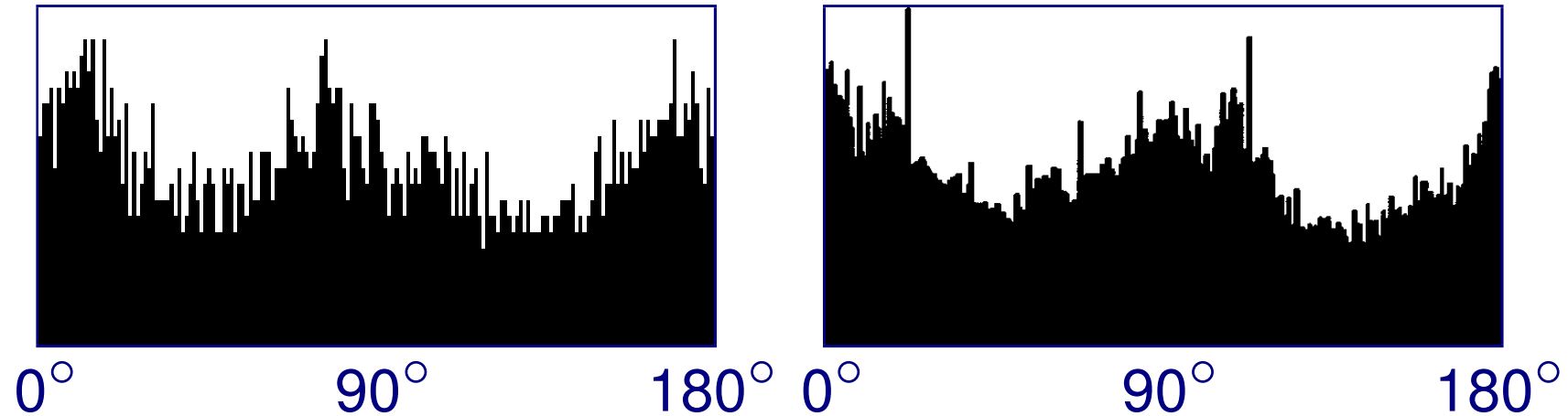
- Neonatal map smoothly becomes more selective

# Statistics drive development



- Biased image dataset: mostly landscapes
- Smoothly changes into horizontal-dominated map

# OR Histograms

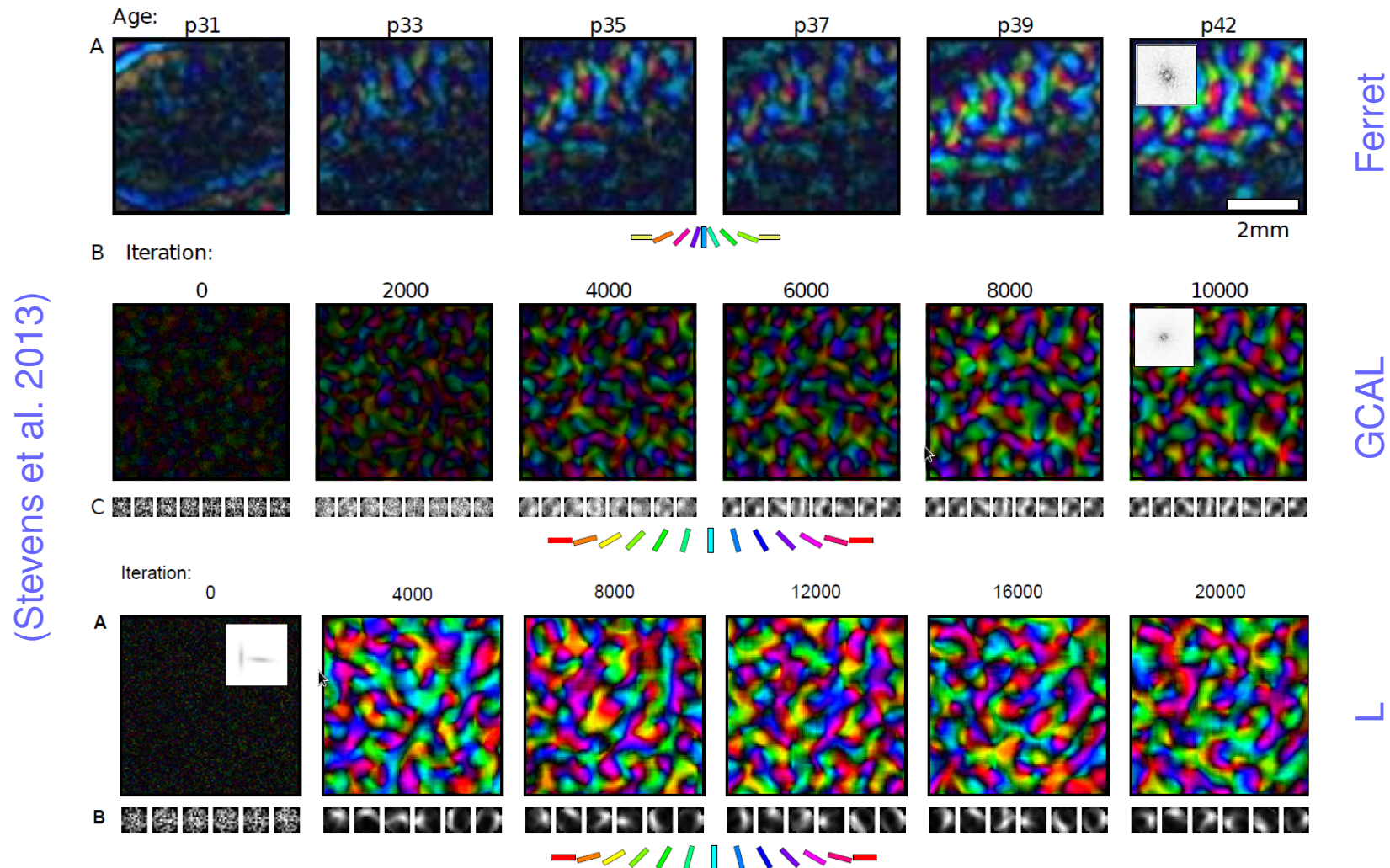


HLISSOM model

Adult ferret V1  
(Coppola et al. 1998)

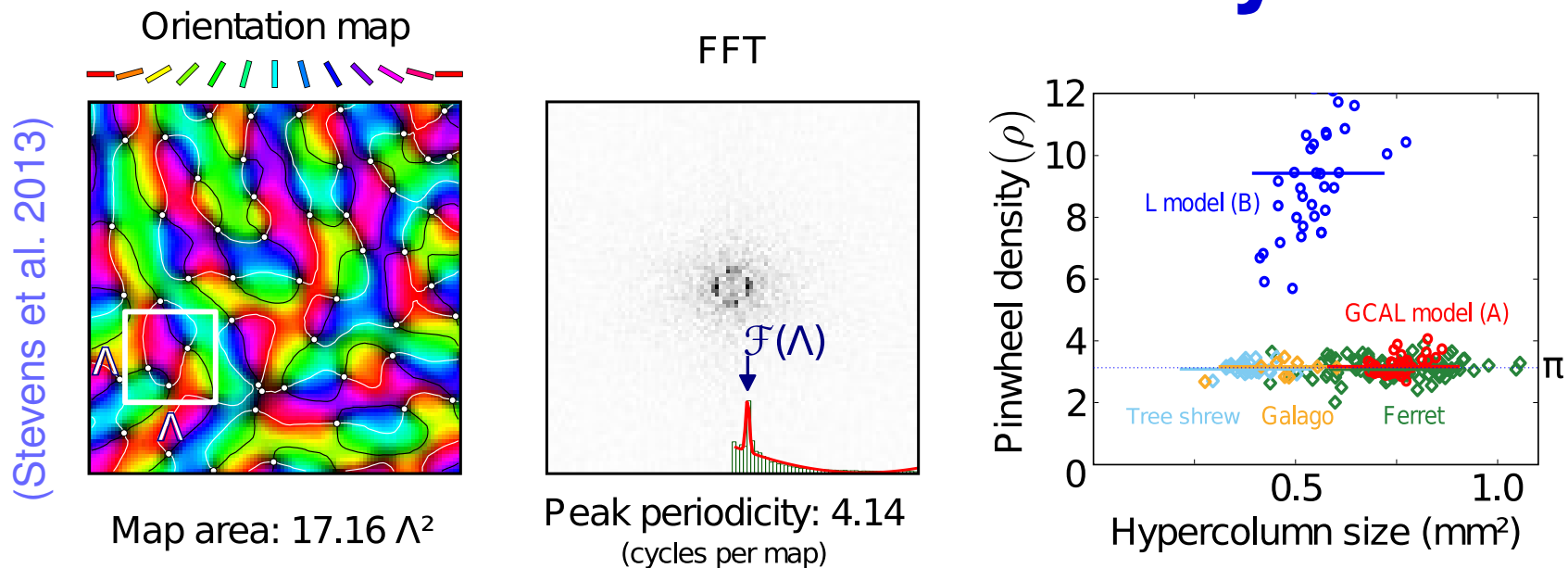
- After postnatal training on Shouval natural images, orientation histogram matches results from ferrets
- Model adapts to statistical structure of images

# Stable development



GCAL map development is stable like ferret V1; LISSOM is unstable even w/o threshold changes, radius shrinking (L)

# Pinwheel density



- Animal orientation maps have an average of  $\pi$  pinwheels per hypercolumn (Kaschube et al. 2010)
- GCAL is so far the only mechanistic model shown to have this property
- LISSOM probably would as well, but requires unrealistic mechanisms to do so, since L does not

# Summary

- Development depends on features of input pattern
- Orientation maps develop with many different patterns
- Develops Gabor-type CFs with most inputs
- Breaks up image into oriented patches
- Scale response by local contrast to work for large images
- Matching biology requires prenatal, postnatal phases
- Can get more elaborate: complex cells, multiple laminae/cell types, short-range inhibition, feedback, ...



# References

- Coppola, D. M., White, L. E., Fitzpatrick, D., & Purves, D. (1998). Unequal representation of cardinal and oblique contours in ferret visual cortex. *Proceedings of the National Academy of Sciences, USA*, 95 (5), 2621–2623.
- Kaschube, M., Schnabel, M., Löwel, S., Coppola, D. M., White, L. E., & Wolf, F. (2010). Universality in the evolution of orientation columns in the visual cortex. *Science*, 330 (6007), 1113–1116.
- Miikkulainen, R., Bednar, J. A., Choe, Y., & Sirosh, J. (2005). *Computational Maps in the Visual Cortex*. Berlin: Springer.
- Shouval, H. Z., Intrator, N., Law, C. C., & Cooper, L. N. (1996). Effect of binocular cortical misalignment on ocular dominance and orientation selectivity. *Neural Computation*, 8 (5), 1021–1040.

Stevens, J.-L. R., Law, J. S., Antolik, J., & Bednar, J. A. (2013). Mechanisms for stable, robust, and adaptive development of orientation maps in the primary visual cortex. *Journal of Neuroscience*, *33*, 15747–15766.