

Tutorial Sheet 5

1. Is there a recursively enumerable language L which is not reducible to its complement? Justify your answer.
2. Show that for any recursively enumerable language L , there is a polynomial-time reduction from L to the Halting Problem.
3. Prove that every language in \mathbf{NP} can be recognized by a *deterministic* Turing machine in exponential time.
4. Show that if $\mathbf{NP} = \mathbf{P}$, then every language in \mathbf{P} except the empty language and the language of all strings is \mathbf{NP} -complete.
5. Show that the language of non-primes in binary representation is in \mathbf{NP} .