# Computer Graphics 7 - Texture mapping, bump mapping and antialiasing

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Slides courtesy of Taku Komura www.inf.ed.ac.uk/teaching/courses/cg

#### Overview

- Texture mapping and bump mapping
- Anti-aliasing

# Texture mapping

- Adding detail to polygon meshes to build high resolution models is computationally expensive
- In realtime applications these are not practical to use



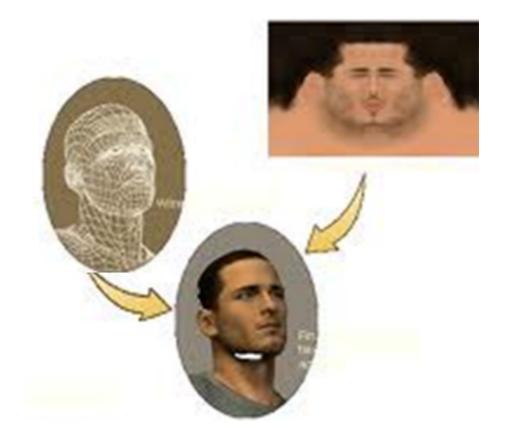


by Rami Ali Al-ashqar

# Texture mapping

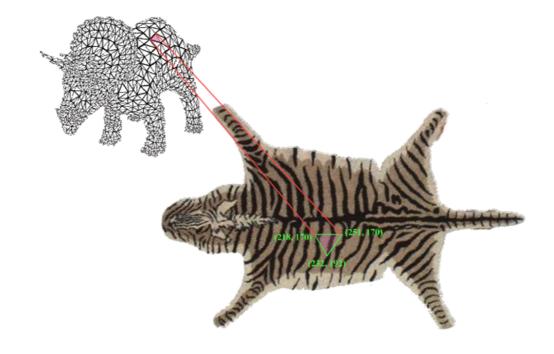
 We can improve the appearance of polygons by mapping images onto their surface

This is done during rasterisation



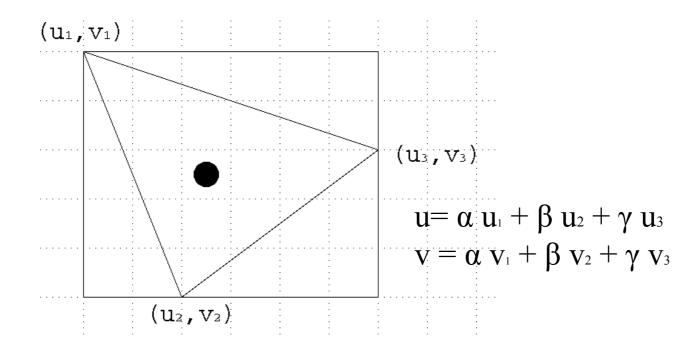
# Overview of texture mapping

- Assign each triangle in the mesh a region of the image
- During rasterisation, colour the surface of the triangle based on the pixels in the image
- Typically done by assigning triangle vertices coordinates (uv) within the image

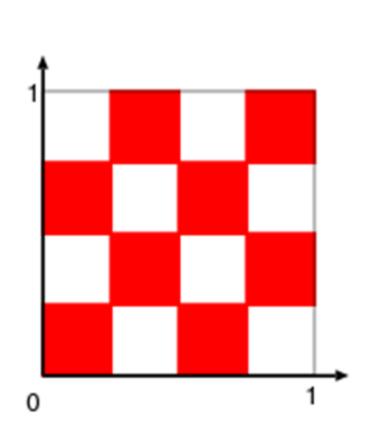


## Interpolation of uv coordinates

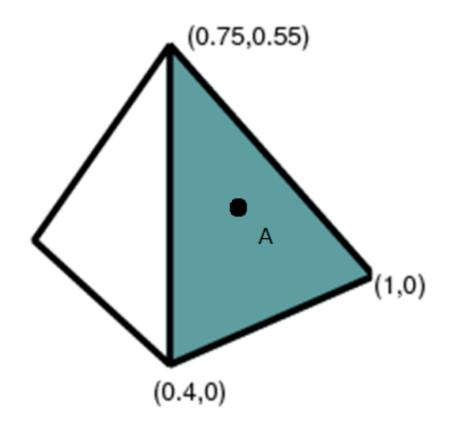
- To calculate which pixel in the image corresponds to a point inside the triangle, we interpolate uv coordinates between vertices
- This can be done using barycentric coordinates



# Example



#### uv coordinate of triangle



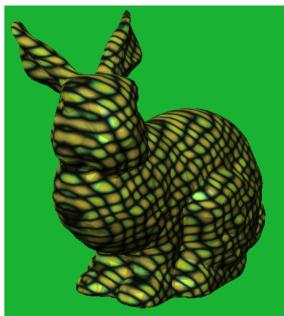
## Producing uv mappings

- Generated based on the mesh cylindrical, spherical, orthogonal
- Captured from real objects by scanning
- Manually specifying coordinates

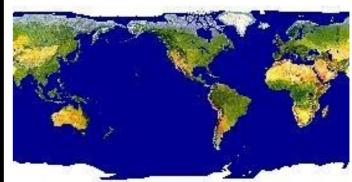
# Common uv mappings

- Orthogonal
- Cylindrical
- Spherical









# Capturing real data

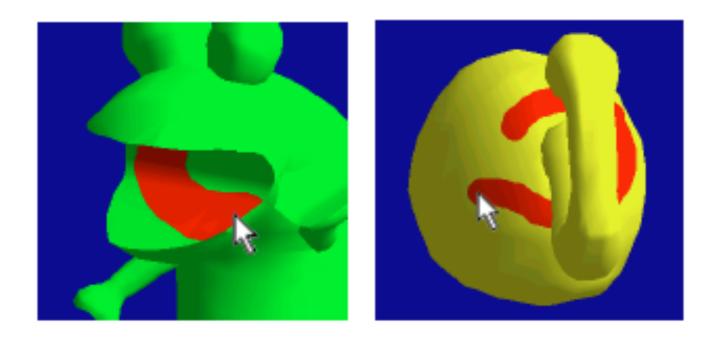
• Scanning depth and colour of objects



http://www.3dface.org/media/images.html

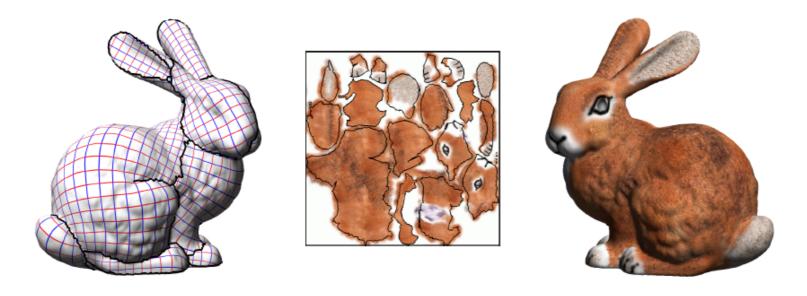
# Manual specification

- Painting on the geometry (Z-brush)
- Manually aligning an unfolded model on the image



# Geometry unfolding

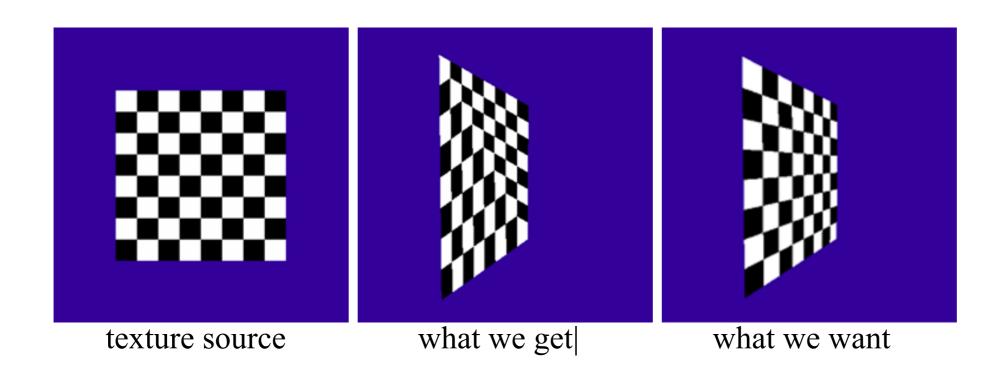
- Segment the mesh into regions that are arranged in a 2D plane
- Draw on these regions in 2D to texture the mesh



Levy et al. SIGGRAPH 2002

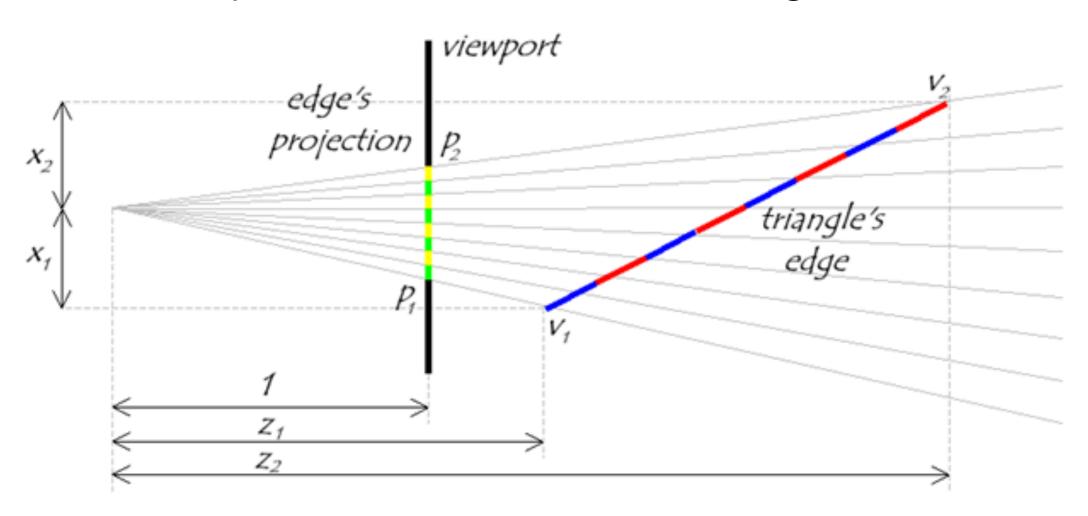
## Linear interpolation

Linearly interpolating uv coordinates does not produce the expected results



# Why does this happen?

• Uniform steps in 2D screen space do not correspond to uniform steps over the surface of the triangle



# Hyperbolic interpolation

- To interpolate between vertices P and Q, rather than interpolating between u(P) and u(Q), we interpolate u(P)/z, u(Q)/z and 1/z
- Considering a point M between P and Q and its projection M':

$$P' = -P/z_P, Q' = -Q/z_Q$$
$$M' = \alpha P' + (1 - \alpha)Q'$$

# Hyperbolic interpolation

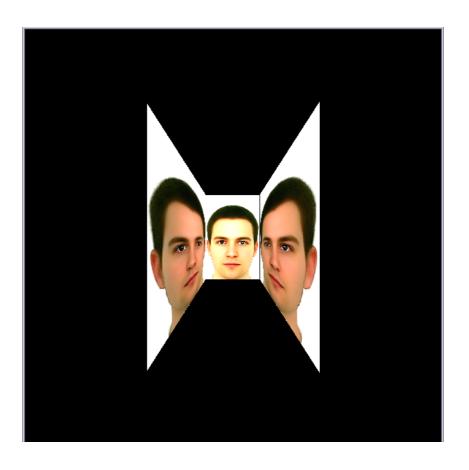
 For a point M the perspective correct interpolated u(M) is then:

$$\frac{u(M)}{-z_M} = \alpha \frac{u(P)}{-z_P} + (1 - \alpha) \frac{u(Q)}{-z_Q}$$
$$u(M) = \frac{\alpha \frac{u(P)}{-z_P} + (1 - \alpha) \frac{u(Q)}{-z_Q}}{\alpha \frac{1}{-z_P} + (1 - \alpha) \frac{1}{-z_Q}}$$

# Example

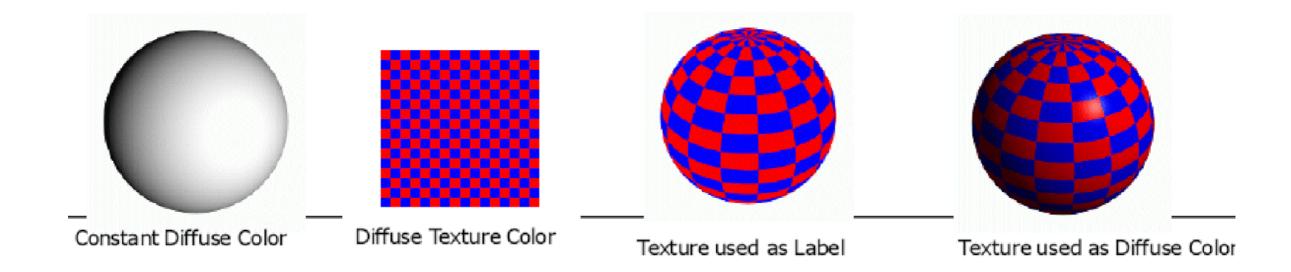
• Linear interpolation vs hyperbolic interpolation





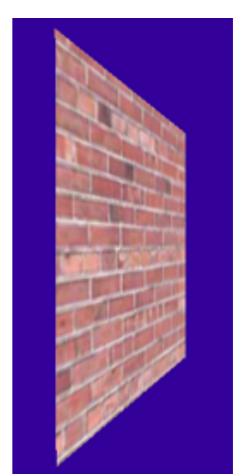
# Texture mapping and illumination

We can use texture information to alter illumination



# Bump mapping

- Texture mapping leaves the surface looking flat
- Adding extra mesh detail can be computationally too expensive

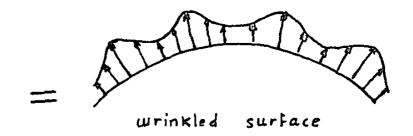


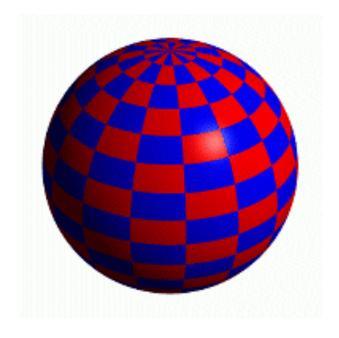


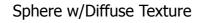
# Bump mapping

 Uses a texture to alter the surface normal to change the illumination smooth surface + wrinkle function

Applied during rasterisation









Swirly Bump Map

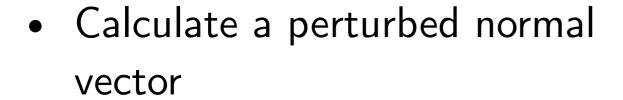


Sphere w/Diffuse Texture & Bump Map

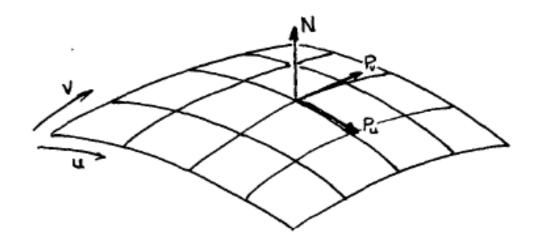
## Bump mapping

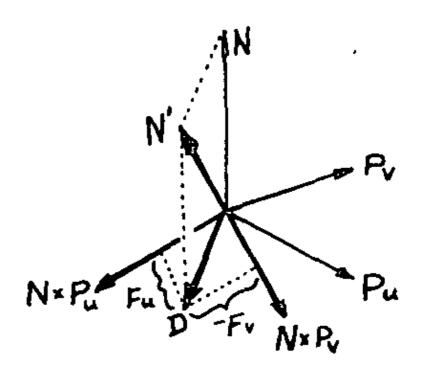
 Calculate finite differences from the bump map

$$F_u = \frac{dF}{du}, F_v = \frac{dF}{dv}$$



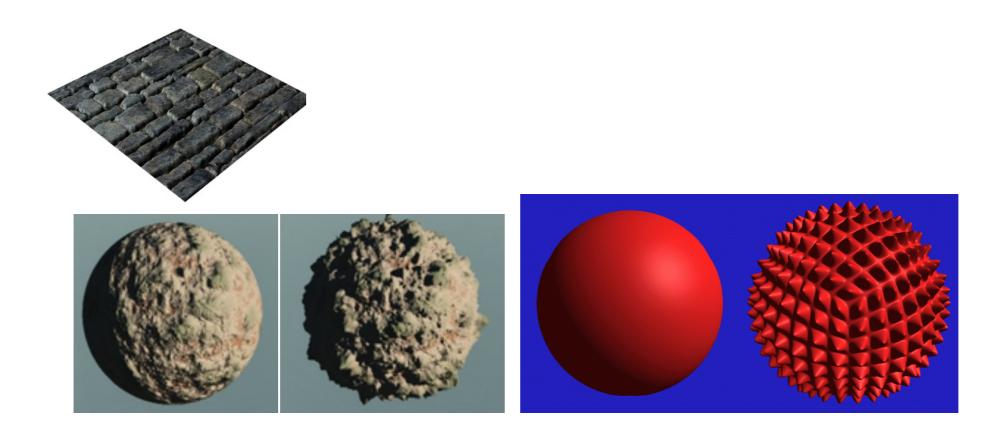
$$\mathbf{n}' = \mathbf{n} + \frac{F_u(\mathbf{n} \times \mathbf{P_v}) - F_v(\mathbf{n} \times \mathbf{P_u})}{||\mathbf{n}||}$$





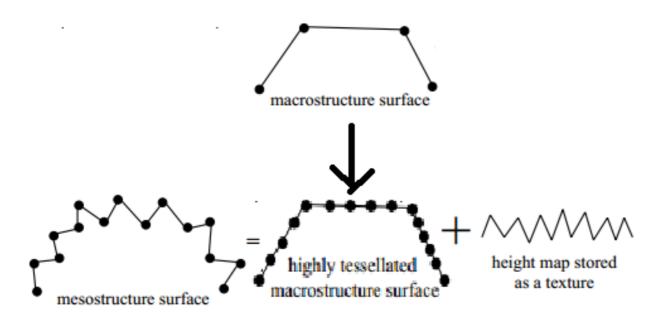
## Displacement mapping

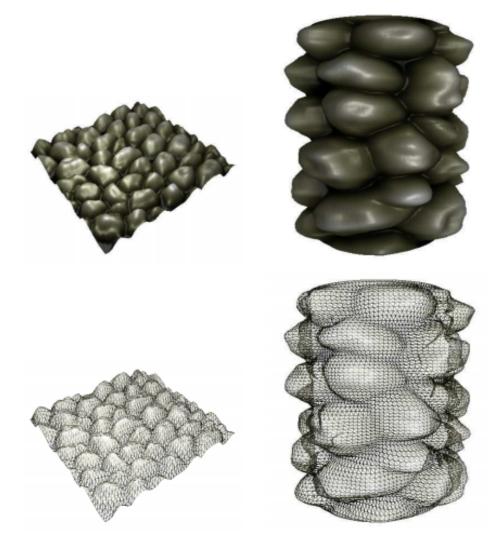
- Bump mapping only changes shading of the surface, not the actual geometry
- Displacement mapping alters the surface using the texture as a mesh defined in uv coordinates



# Displacement mapping

- Subdivide the surface to resolution of texture
- Displace vertices in normal direction of surface by height in displacement map



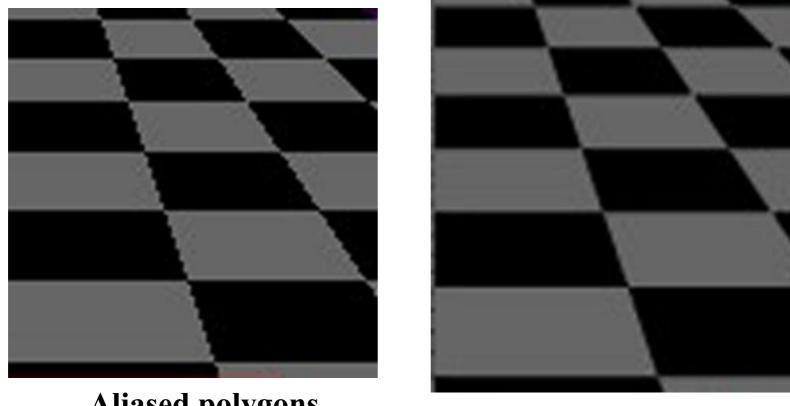


#### Overview

- Texture mapping
- Bump mapping
- Anti-aliasing

# Anti-aliasing

- Aliasing is the distortion produced by representing a high resolution signal at a lower resolution
- Anti-aliasing aims to remove this distortion

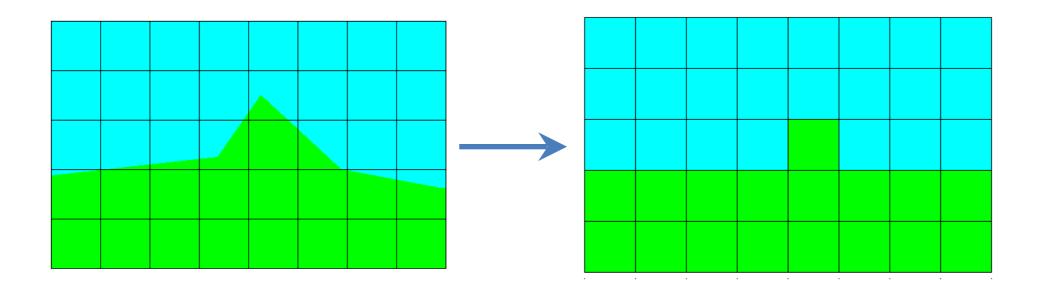


Aliased polygons (jagged edges)

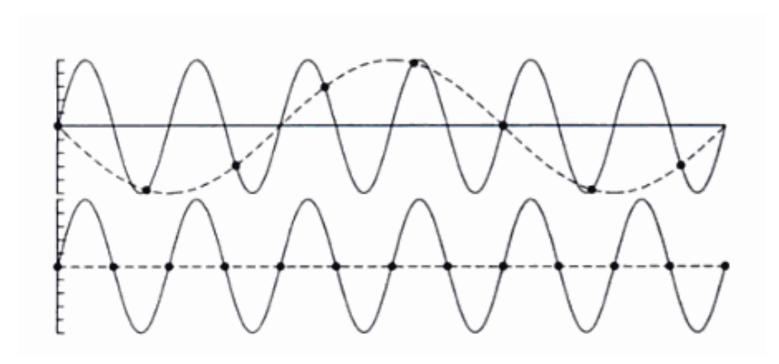
**Anti-aliased polygons** 

# Why does aliasing happen?

When the sampling frequency is too low to represent the signal



# Nyquist limit



$$f_{signal} = 0.8 f_{sample}$$

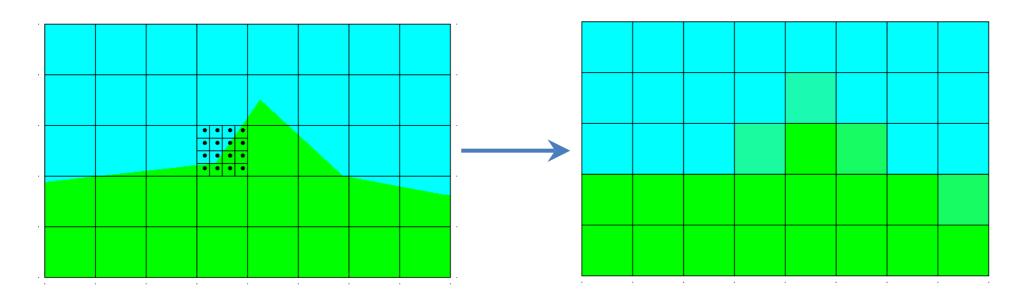
$$f_{signal} = 0.5 f_{sample}$$

 To reproduce a signal, the sampling frequency should be twice the signal frequency

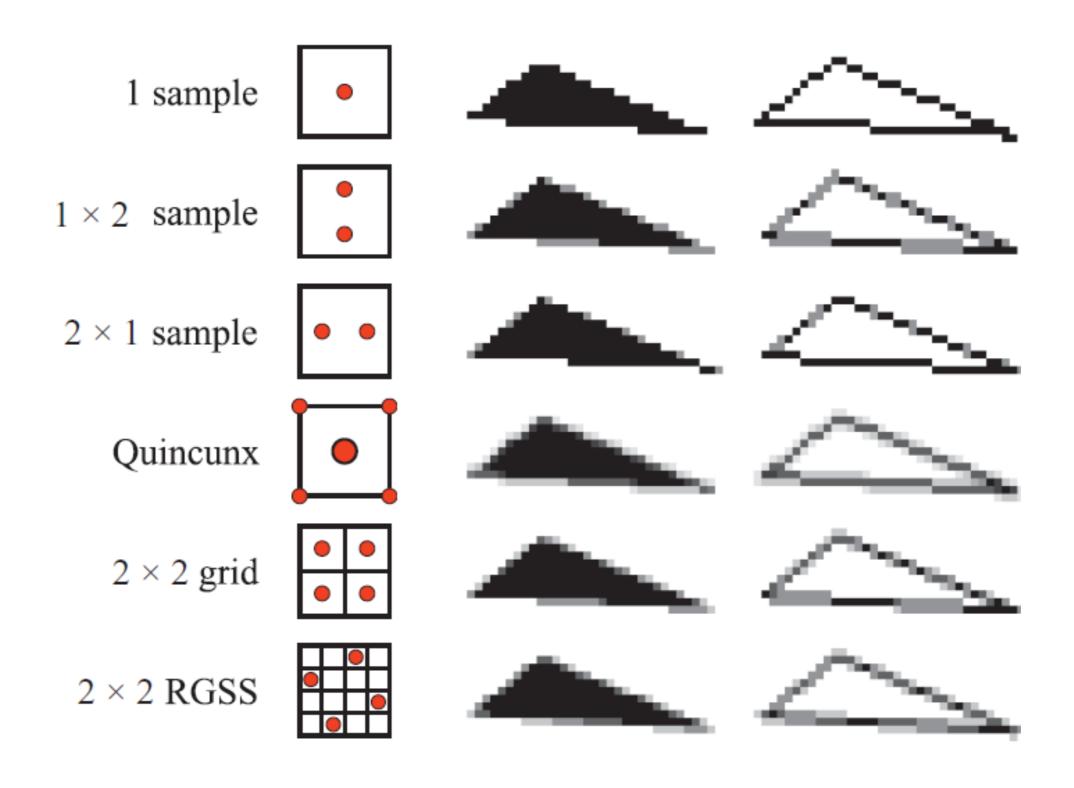
$$f_{signal} < 0.5 f_{sample}$$

# Anti-aliasing by subsampling

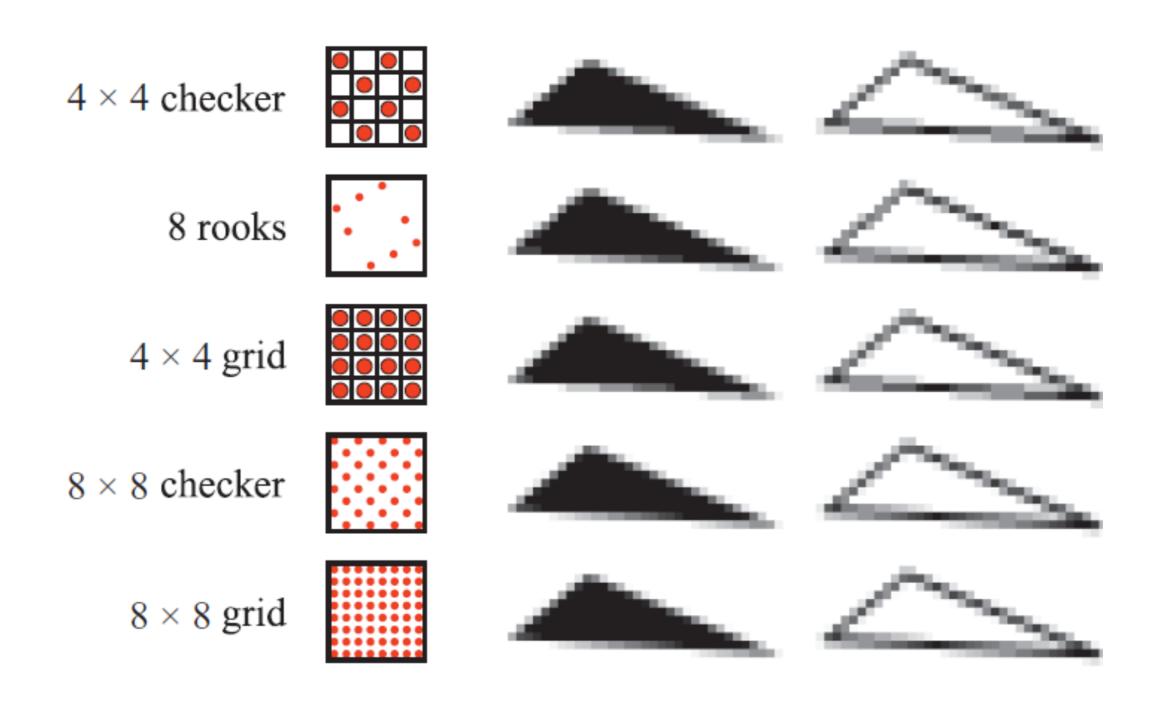
- Subdivide each pixel into n regions
- Colour each sub-pixel
- Calculate average colour



# Subsampling schemes

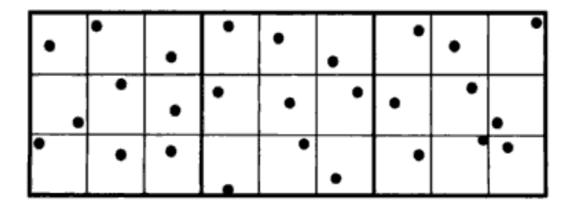


# Subsampling schemes



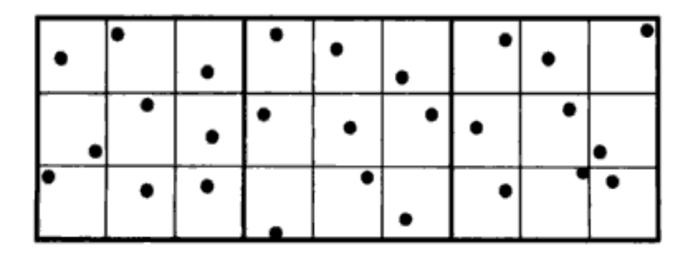
# Stochastic sampling

- Regular patterns still exhibit some aliasing for very small details
- Random sampling causes higher frequency signals to appear as noise rather than aliasing
- Our eyes are more sensitive to aliasing than noise



# Stochastic sampling

- Subdivide pixels into n regions and randomly sample within those regions
- Calculate colours for each subsample and average
- Either precompute a table of sample positions or calculate them in real time



# Comparison

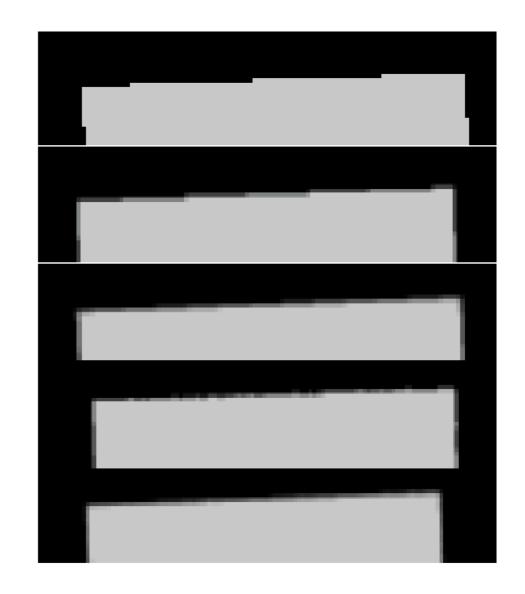
Regular, 1x1

Regular 3x3

Regular, 7x7

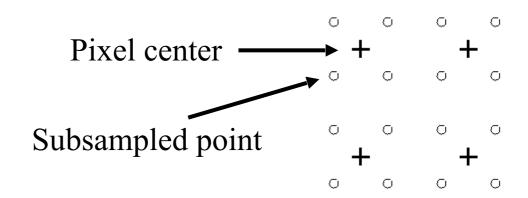
Jittered, 3x3

Jittered, 7x7



#### Accumulation buffers

 Use a buffer of the same size as the target image



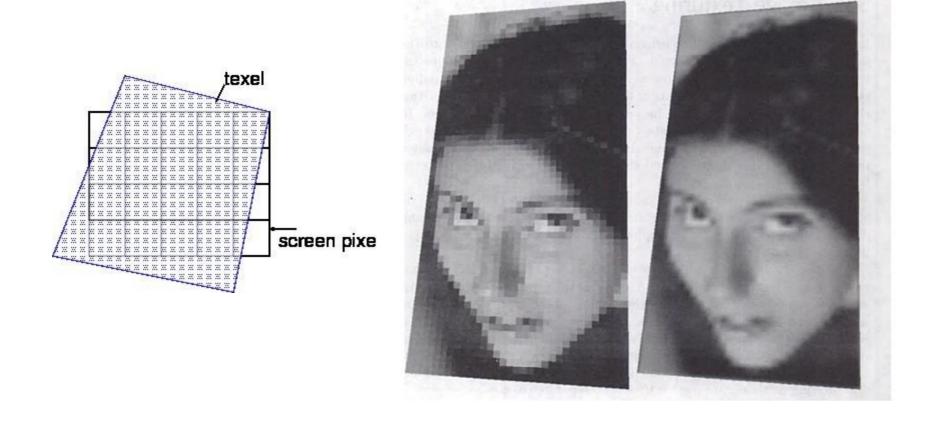
- Shift the frame buffer around each pixel center
- Accumulate and average

# Antialiasing textures

- When textures are zoomed in, individual texture pixels (texels) are clearly visible
- When zoomed out, several texels could be mapped to a single pixel

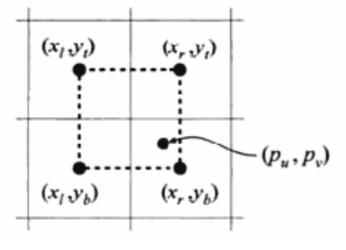


# Magnification



## Bilinear interpolation

 Averaging the neighbouring texels based on the uv coordinates for the current pixel

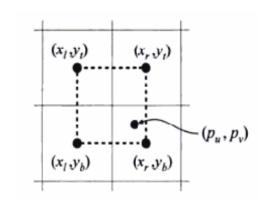






# Bilinear interpolation

 Colour is calculated from coordinates by interpolation, with u' and v' the distance from the rounded down coordinates



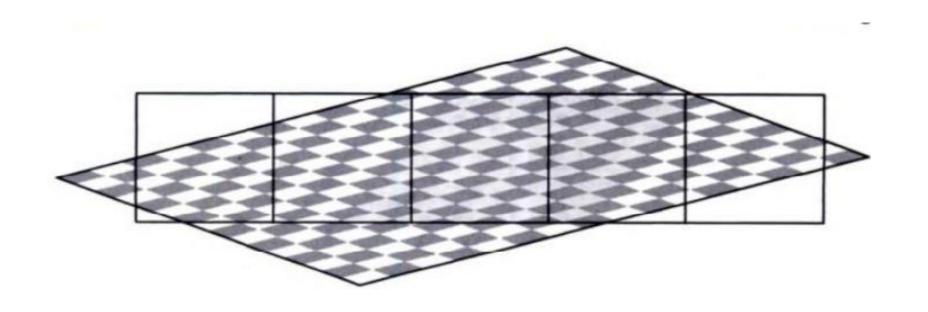
$$u' = p_u - (\text{int})p_u, v' = p_v - (\text{int})p_v$$

$$c(p_u, p_v) = (1 - u')(1 - v')t(x_l, y_b) + u'(1 - v')t(x_r, y_b)$$

$$+ (1 - u')v't(x_l, y_t) + u'v't(x_r, y_t)$$

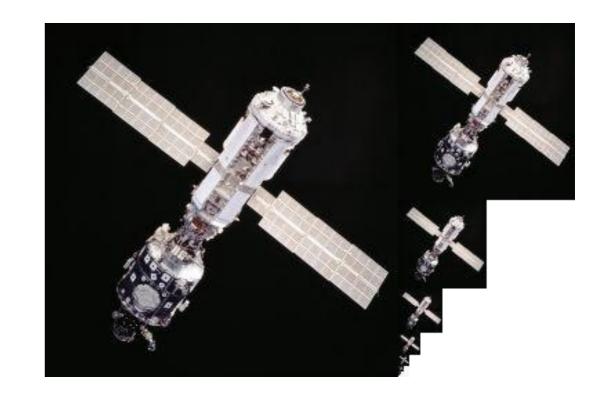
## Minification

 When textures are zoomed out, multiple texels fall inside a single pixel. Causes aliasing due to the Nyquist limit



## MIP mapping

- Textures are produced at multiple resolutions
- Resolutions are switched depending on number of texels in a pixel
- Select a resolution where ration of texels to pixel is 1:1



## MIP mapping

- Map pixel corners to texture space
- Find a resolution where texel size is close to the pixel size
- Alternatively, use trilinear interpolation between multiple resolutions

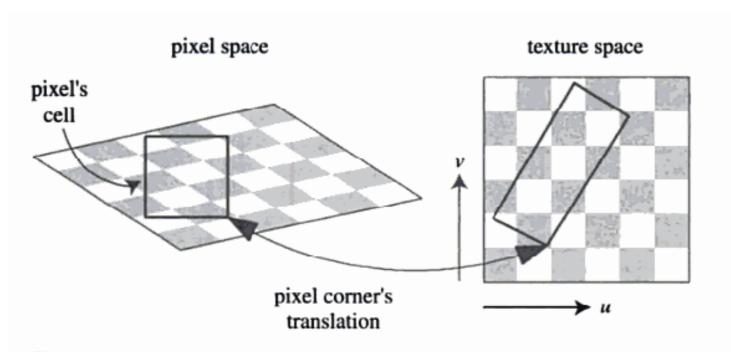
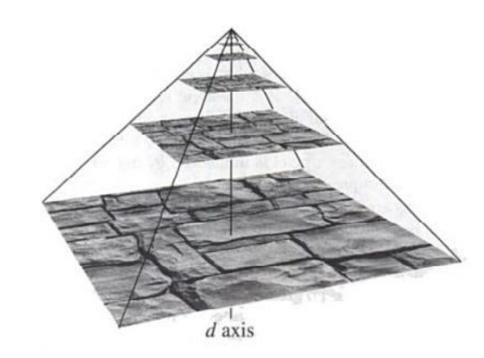
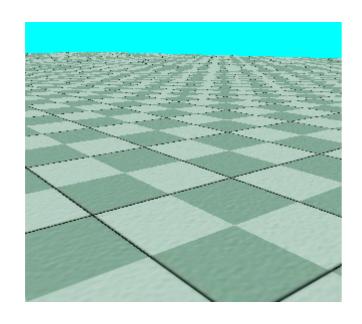


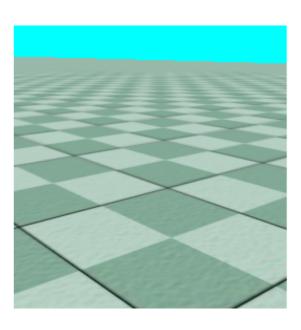
Figure 5.13. On the left is a square pixel cell and its view of a texture. On the right is the projection of the pixel cell onto the texture itself.



# Example



Standard



MIP mapping

#### References

- Texture mapping Shirley Chapter 11 (Texture mapping), <a href="https://www.comp.nus.edu.sg/~lowkl/publications/">https://www.comp.nus.edu.sg/~lowkl/publications/</a>

   lowk\_persp\_interp\_techrep.pdf
- Bump mapping Akenine-Möller Chapter 6.7 (6.7.1) Bump mapping. Blinn, J. F. (1978). Simulation of wrinkled surfaces. ACM SIGGRAPH Computer Graphics, 12(3).
- Anti-aliasing Shirley Chapter 8.2 (Simple anti-aliasing),
   Akenine-Möller Chapter 5.6.2 (Screen-based anti-aliasing),
   Chapter 6.2.1,6.2.2 (Magnification and Minification)