

# Computer Graphics 2 - Object representations

Tom Thorne

Some slides are courtesy of Taku Komura

[thomas.thorne@ed.ac.uk](mailto:thomas.thorne@ed.ac.uk)

[www.inf.ed.ac.uk/teaching/courses/cg/](http://www.inf.ed.ac.uk/teaching/courses/cg/)

## Last time

- ▶ History, applications
- ▶ Basic vector algebra
- ▶ Computer graphics pipeline

# Overview

## **Polygon meshes**

- ▶ Storage
- ▶ Representation
- ▶ Decomposition
- ▶ Quad meshes
- ▶ Generation
- ▶ Implicit surfaces

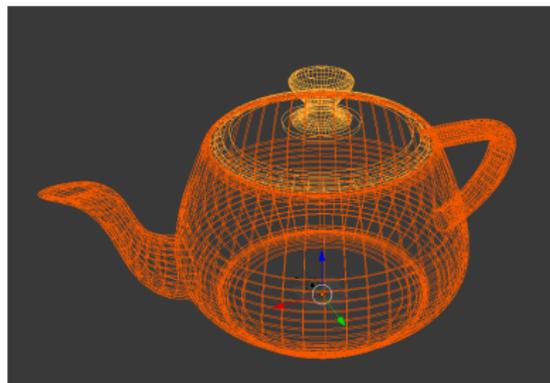
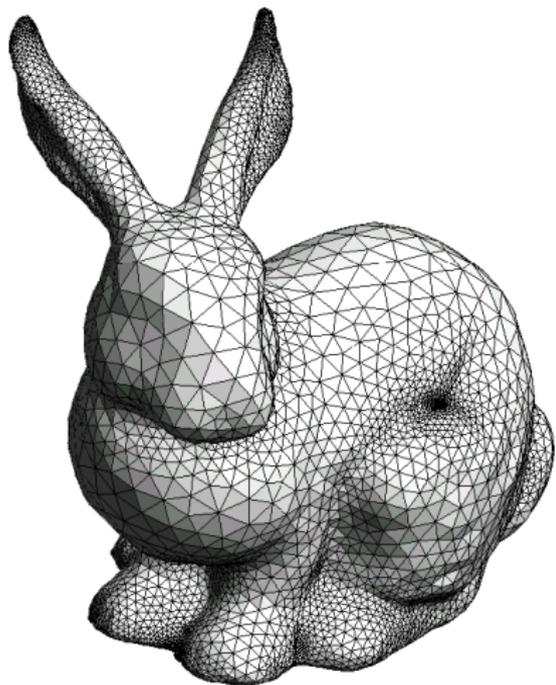
## Level of detail

- ▶ Scaling methods

## Image representations

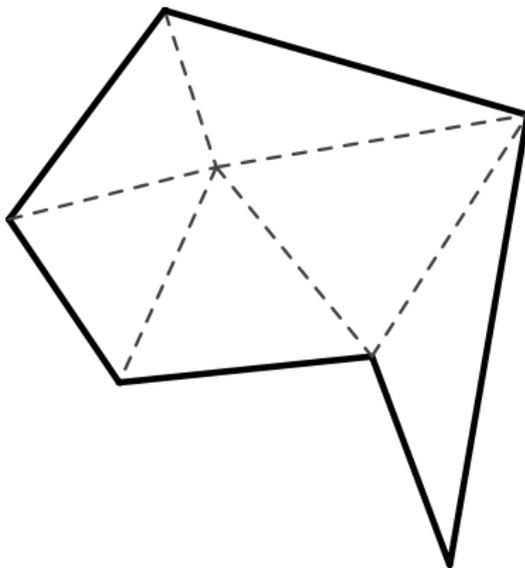
- ▶ Pixel Buffers
- ▶ Alpha channels
- ▶ Z buffers

# Mesh structures



Objects represented as a set of polygons

## Triangle representation

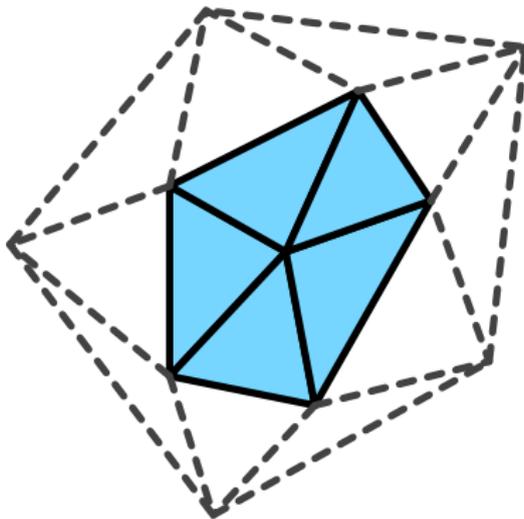


- ▶ Polygons can be broken down into triangles

# Mesh topology

Manifolds:

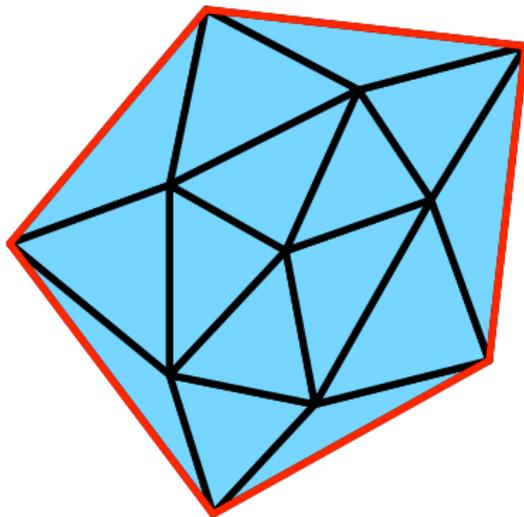
- ▶ All edges belong to two triangles
- ▶ All vertices have a single continuous set of triangles around them



## Mesh topology

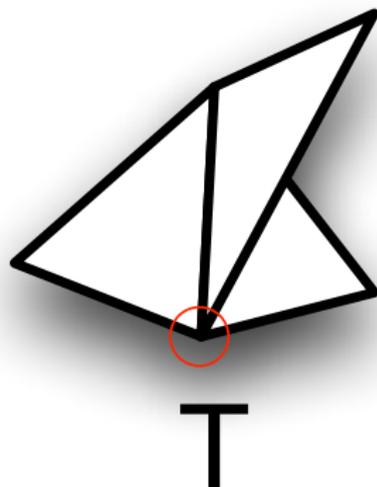
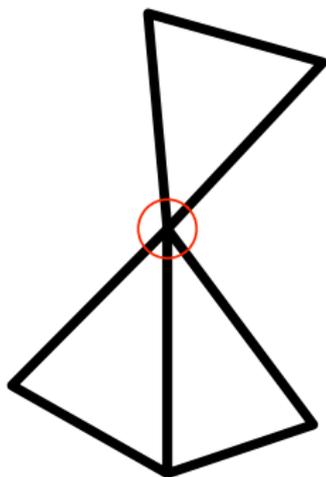
Manifolds with boundaries:

- ▶ All edges belong to one or two triangles
- ▶ All vertices have a single continuous set of triangles around them



## Mesh topology

Examples of non-manifold meshes:



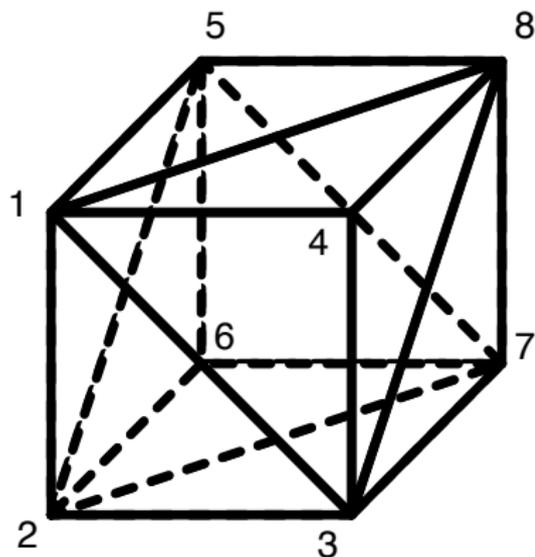
# Storage format

Vertices:

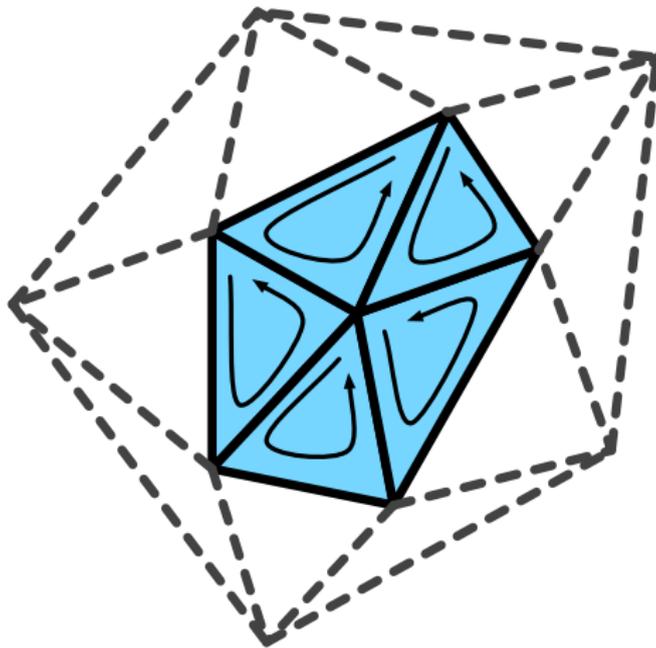
-1	1	1
-1	-1	1
1	-1	1
1	1	1
-1	1	-1
-1	-1	-1
1	-1	-1
1	1	-1

Polygons:

1	2	3
1	3	4
1	4	8
1	8	5
4	3	8
3	7	8
5	7	6
5	8	7
1	5	2
5	6	2
2	6	7
2	7	3

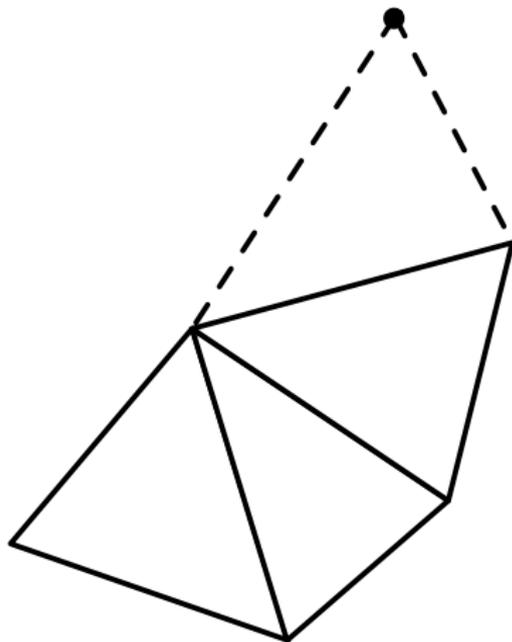
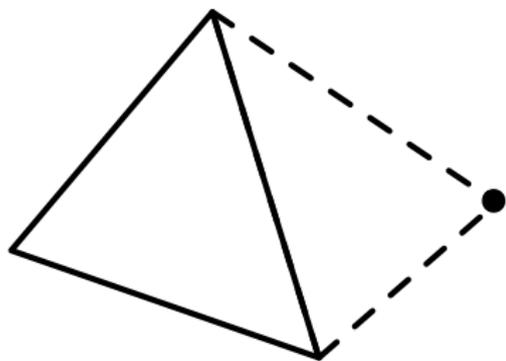


## Orientation



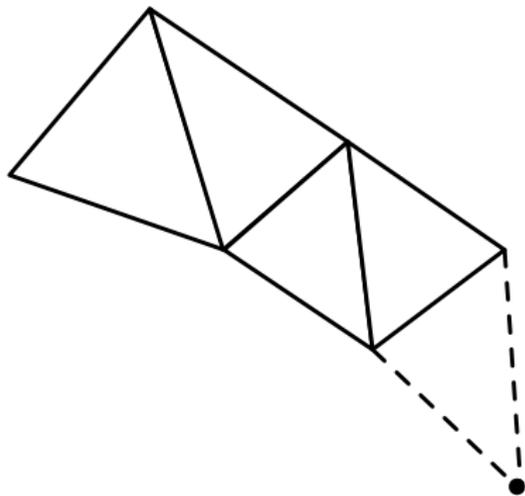
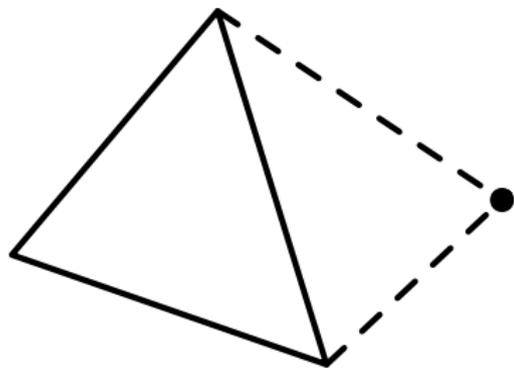
Vertexes in triangle list stored in counter clockwise order

## Triangle fans



Instead of storing  $3T$  edges, store  $T + 2$

## Triangle strips



Instead of storing  $3T$  edges, store  $T + 2$

# Decomposing surfaces

We can decompose meshes into triangle strips or fans to reduce storage requirements

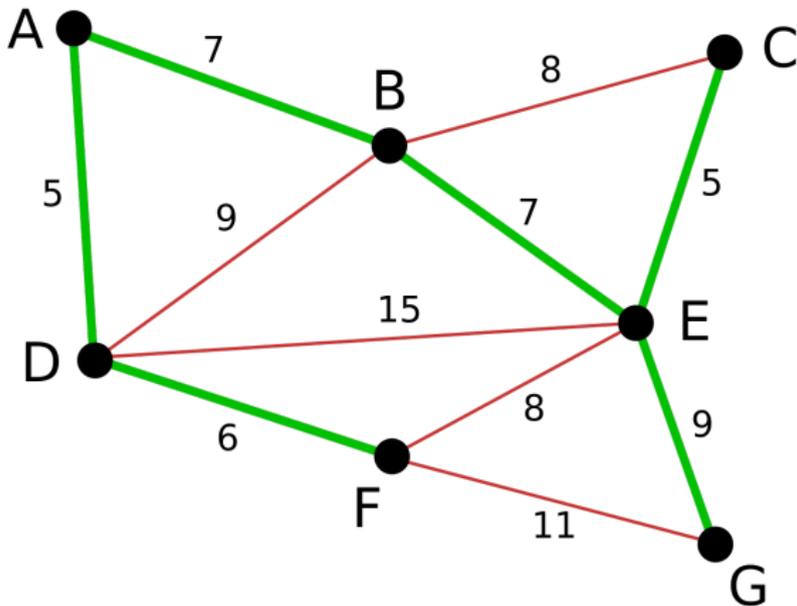
Some methods:

- ▶ Minimal spanning tree
- ▶ Spirals

## Minimal spanning tree decomposition

A minimal spanning tree produces a tree over a graph which visits every node whilst minimising costs

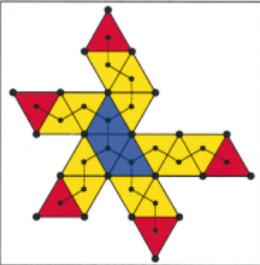
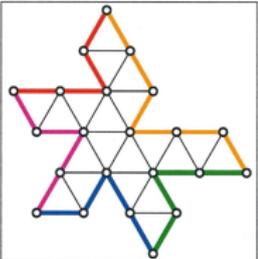
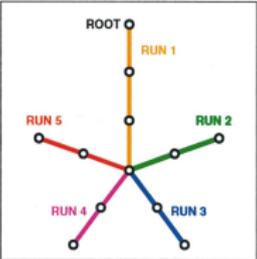
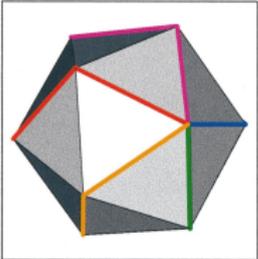
- ▶ edges are given costs
- ▶ a tree with minimal total cost is found



# Minimal spanning tree decomposition

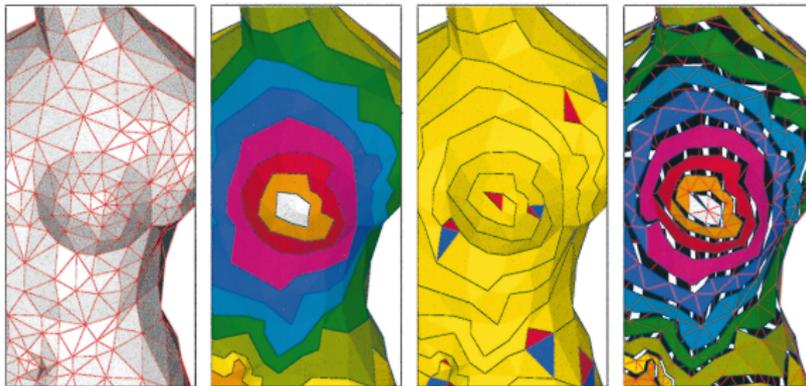
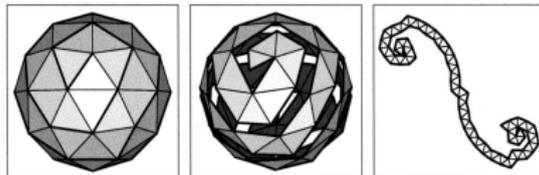
From a mesh, produce a graph where:

- ▶ nodes correspond to triangles of the mesh
- ▶ edges shared by a pair of triangles become edges in the graph
- ▶ cost is set to the Euclidean distance between the triangle and the root triangle



# Spiral decomposition

- ▶ Generate layers of triangles
- ▶ Connect layers into a single spiral of triangles



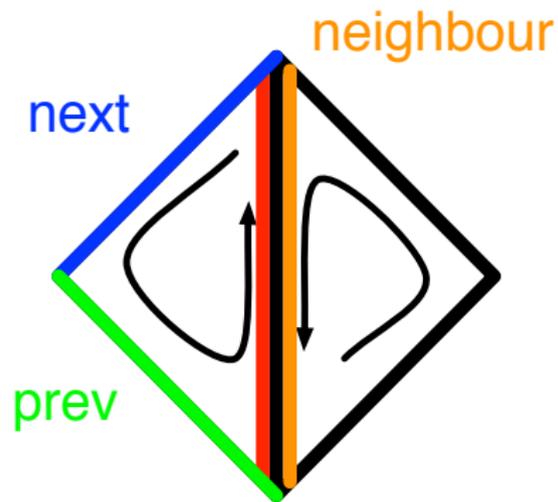
# Directed edge data structure

Vertices

$x_1$	$y_1$	$z_1$	$e_r$
$x_2$	$y_2$	$z_2$	$e_s$
$\vdots$	$\vdots$	$\vdots$	$\vdots$

Edges

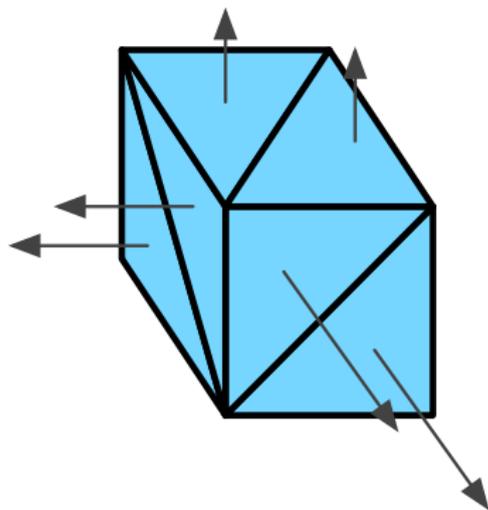
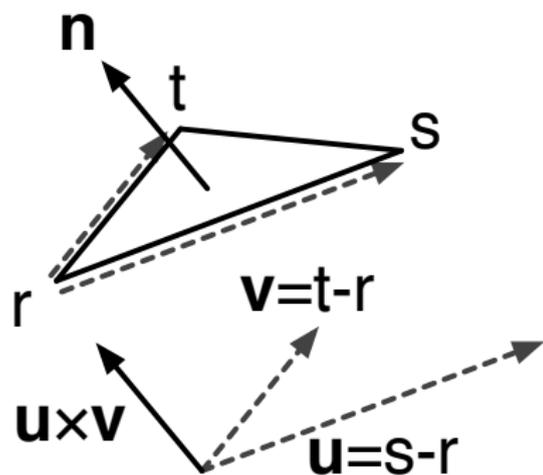
$v_a$	$v_b$	$e_{neighbour}$	$e_{next}$	$e_{prev}$
$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$



# Surface normals

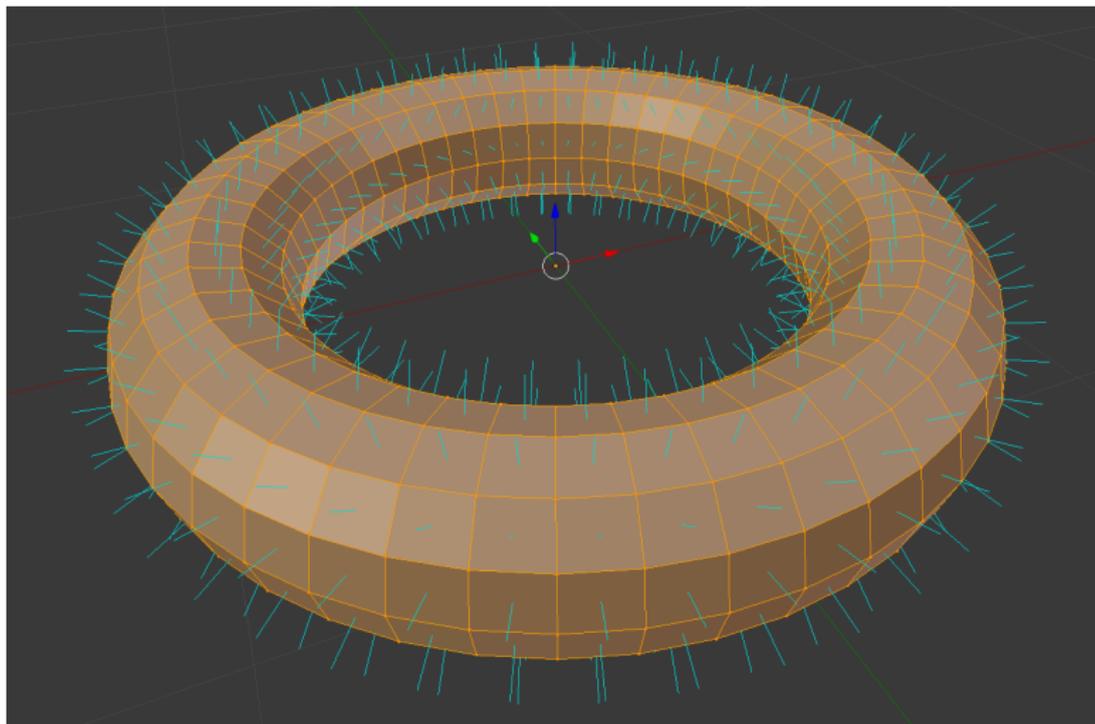
Calculation:

$$\mathbf{n} = (\mathbf{t} - \mathbf{r}) \times (\mathbf{s} - \mathbf{r})$$



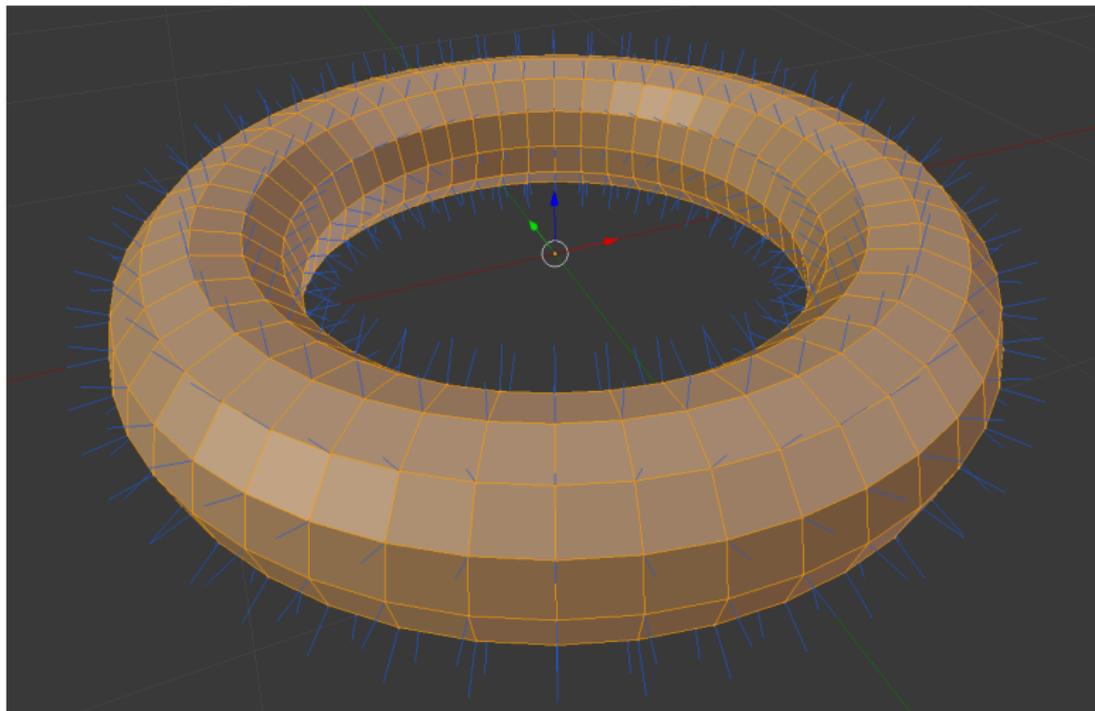
# Surface normals

Face normals



# Surface normals

Vertex normals



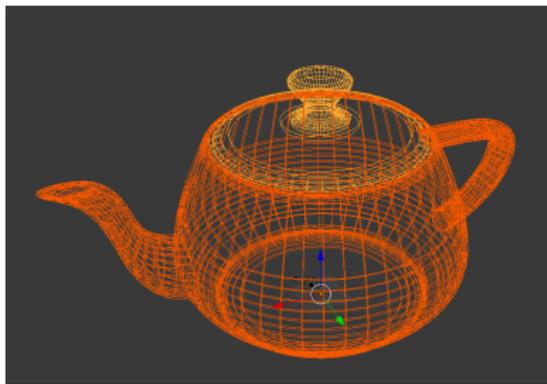
# Quadrilateral meshes

Relatively easy to extend to quadrilateral meshes (quadmeshes):

- ▶ Same storage format

Problems:

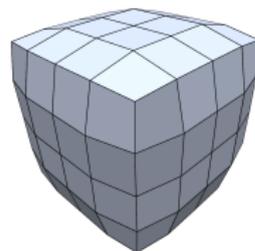
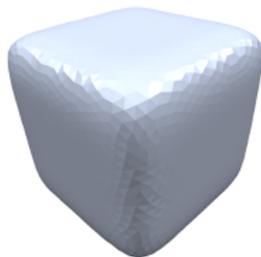
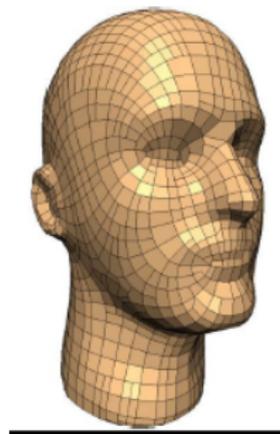
- ▶ 4 points don't always lie on a plane



# Quadrilateral meshes

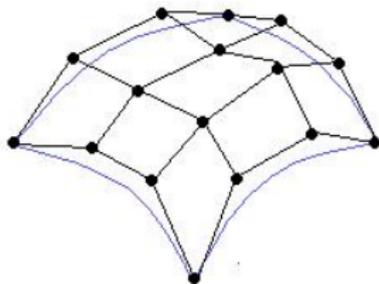
Benefits of quadmeshes:

- ▶ Easier to align edges to curvature or feature lines defining an object



## Quadrilateral meshes

- ▶ Easier to texture map
- ▶ Good for finite element simulation
- ▶ Easier to fit with parametric surfaces



## Generating polygon mesh data

- ▶ Where does the mesh come from?
- ▶ Modelling using software (e.g. Blender)
- ▶ Scanning
- ▶ Procedural methods

# Scanning meshes

## Laser range scanning

- ▶ Measuring time for a laser beam to bounce back from surface
- ▶ Produces accurate data

## Stereo vision

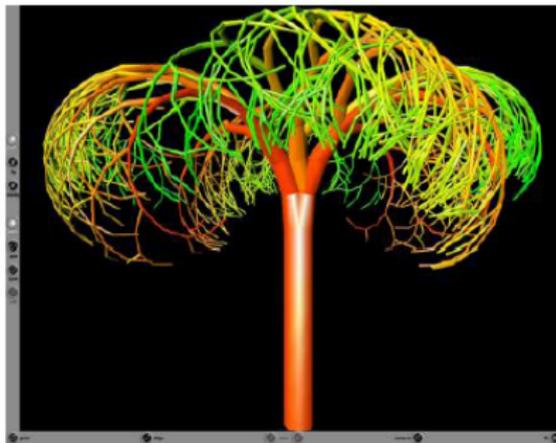
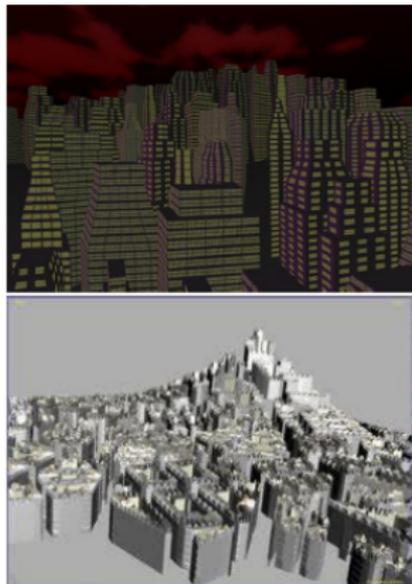
- ▶ Two cameras, estimate depth

## KINECT

- ▶ Estimating depth from infra-red light
- ▶ Limits on range (1.2-3.5m)

# Procedural models

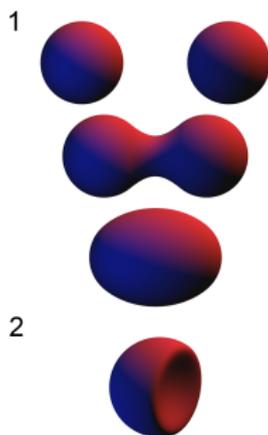
- ▶ Rule based approaches



## Implicit surfaces

Given some potential function  $f(x)$  we can evaluate at every point in space, define an isosurface of all points where  $f(x) = c$

- ▶ Metaballs (Blinn, Ohmura)
- ▶  $\sum_i \frac{a_i}{r}$





# Overview

## Polygon meshes

- ▶ Storage
- ▶ Representation
- ▶ Decomposition
- ▶ Quad meshes
- ▶ Generation
- ▶ Implicit surfaces

## **Level of detail**

- ▶ Scaling methods

## Image representations

- ▶ Pixel Buffers
- ▶ Alpha channels
- ▶ Z buffers

## Level of detail scaling

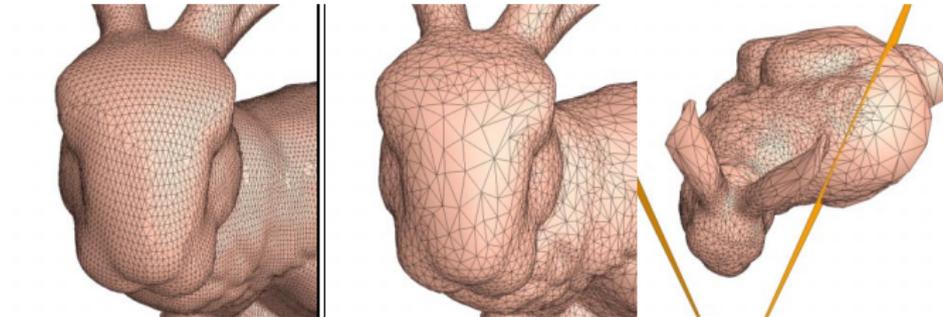
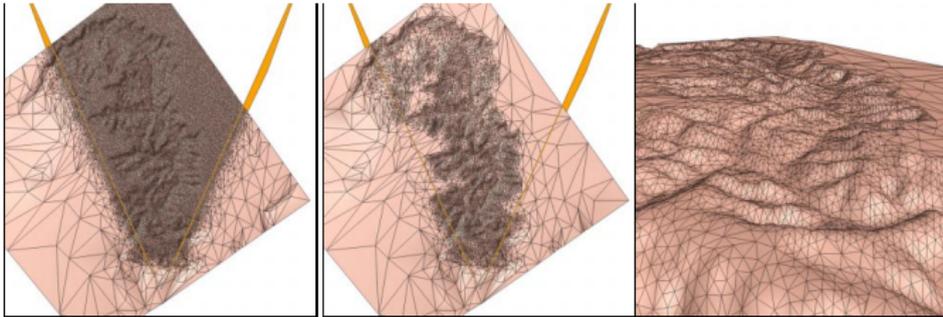
When an object is close to the camera we usually want a very detailed model. But not when:

- ▶ further away (taking up a small amount of space on screen)
- ▶ facing away from the camera
- ▶ outside the view volume

# Level of detail scaling

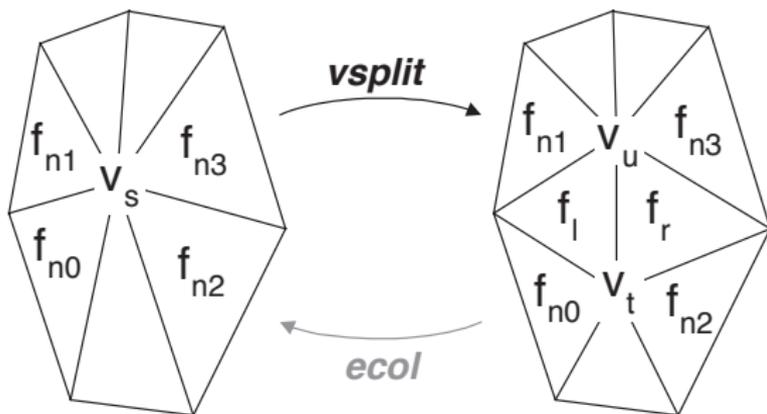
## Progressive meshes

- ▶ some polygons may be much closer to camera than others, within a single mesh



# Level of detail scaling

## Progressive meshes



# Overview

## Polygon meshes

- ▶ Storage
- ▶ Representation
- ▶ Decomposition
- ▶ Quad meshes
- ▶ Generation
- ▶ Implicit surfaces

## Level of detail

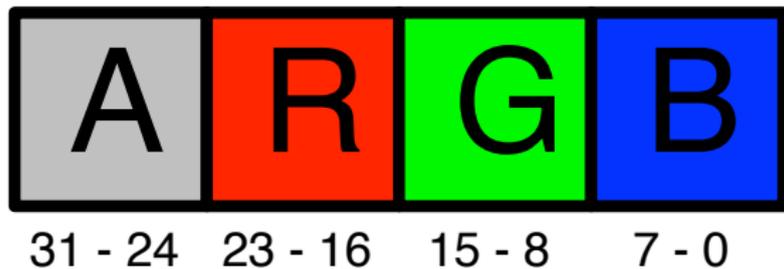
- ▶ Scaling methods

## **Image representations**

- ▶ Pixel Buffers
- ▶ Alpha channels
- ▶ Z buffers

## Image representations

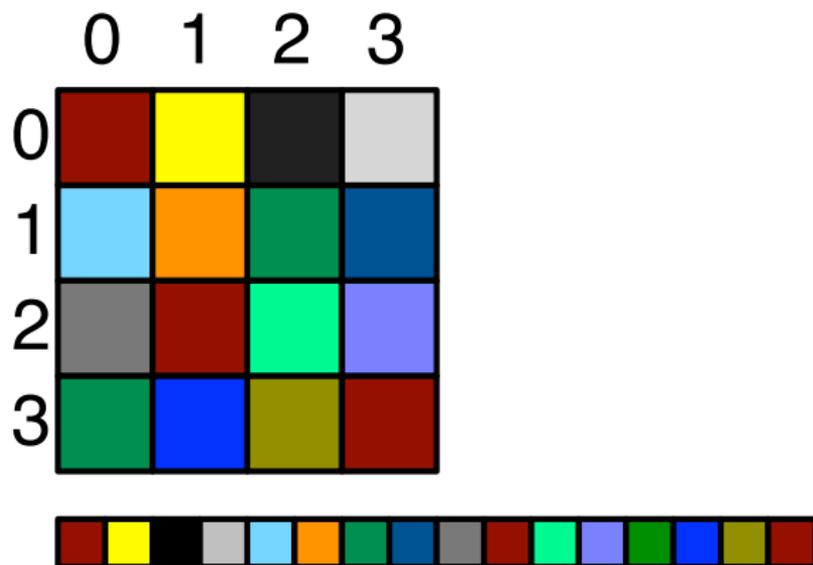
Standard 32 bit format for colours:



Other formats:

- ▶ 32bit Floats per channel (high dynamic range)
- ▶ 24bit RGB (usually padded)

## Pixel buffers



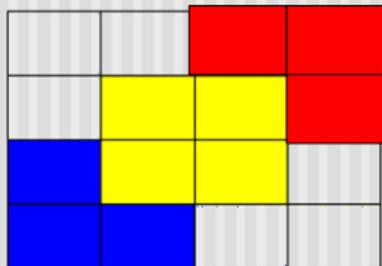
```
int array[4][4];  
int arrayFlat[16];  
array[y][x]=arrayFlat[y*width+x];
```

## Z buffers

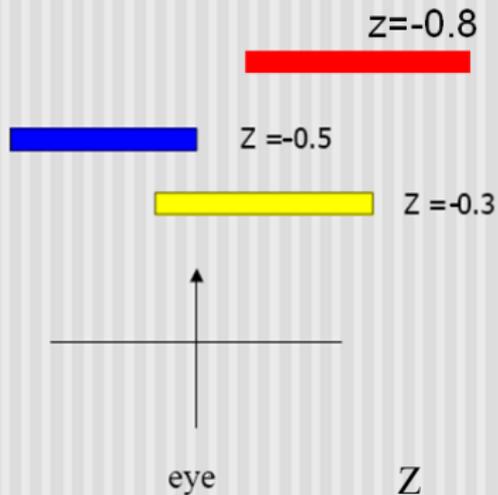
How do we make sure things closer to the camera are drawn on top of things behind?

- ▶ various methods covered later in the course
- ▶ current most popular method is the Z buffer
- ▶ implemented by GPU, very little work to use with OpenGL

## Z buffer example



Correct Final image



Top View

## Z buffer example

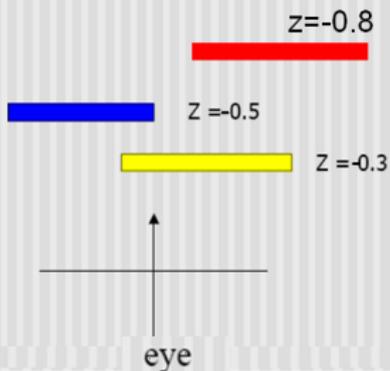
Step 1: Initialize the depth buffer

-1.0	-1.0	-1.0	-1.0
-1.0	-1.0	-1.0	-1.0
-1.0	-1.0	-1.0	-1.0
-1.0	-1.0	-1.0	-1.0

## Z buffer example

Step 2: Draw the blue polygon (assuming the program draws blue polygon first – the order does not affect the final result any way).

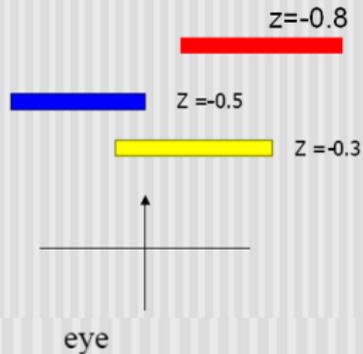
-1.0	-1.0	-1.0	-1.0
-1.0	-1.0	-1.0	-1.0
-0.5	-0.5	-1.0	-1.0
-0.5	-0.5	-1.0	-1.0



## Z buffer example

Step 3: Draw the yellow polygon

-1.0	-1.0	-1.0	-1.0
-1.0	-0.3	-0.3	-1.0
-0.5	-0.3	-0.3	-1.0
-0.5	-0.5	-1.0	-1.0

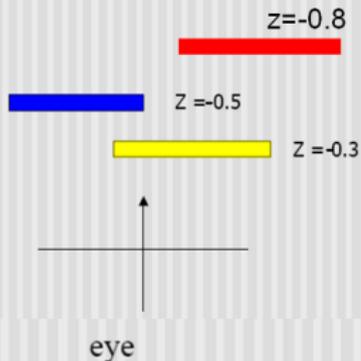


If the depth value is larger than that in the z-buffer, the pixel is coloured and value in the z-buffer is updated

## Z buffer example

Step 4: Draw the red polygon

-1.0	-1.0	-0.8	-0.8
-1.0	-0.3	-0.3	-0.8
-0.5	-0.3	-0.3	-1.0
-0.5	-0.5	-1.0	-1.0



If the depth value is larger than that in the z-buffer, the pixel is coloured and value in the z-buffer is updated

# Summary

## Polygon meshes

- ▶ How to store them
- ▶ Data structures for operations on meshes
- ▶ Creating mesh data

## Level of detail

- ▶ Why?
- ▶ Scaling

## Image data

- ▶ Standard storage format
- ▶ Alpha channels
- ▶ Z buffers

## References

### Shirley:

- ▶ Chapter 12.1 (Data Structures for Graphics – Triangle Meshes)
- ▶ Chapter 3 (Raster Images)

### Papers:

- ▶ Taubin, G., & Rossignac, J. (1998). Geometric compression through topological surgery. *ACM Transactions on Graphics*, 17(2), 84–115.
- ▶ D. Bommes, B. Lévy, N. Pietroni, E. Puppo, C. Silva, M. Tarini and D. Zorin, Eurographics STARS, 2012
- ▶ Hoppe, H. (1997). View-dependent refinement of progressive meshes (pp. 189–198). SIGGRAPH '97