



# Virtual Memory

---

## Motivation:

- Each process would like to see its own, full, address space
- Clearly impossible to provide full physical memory for all processes
- Processes may define a large address space but use only a small part of it at any one time
- Processes would like their memory to be protected from access and modification by other processes
- The operating system needs to be protected from applications

# Virtual Memory

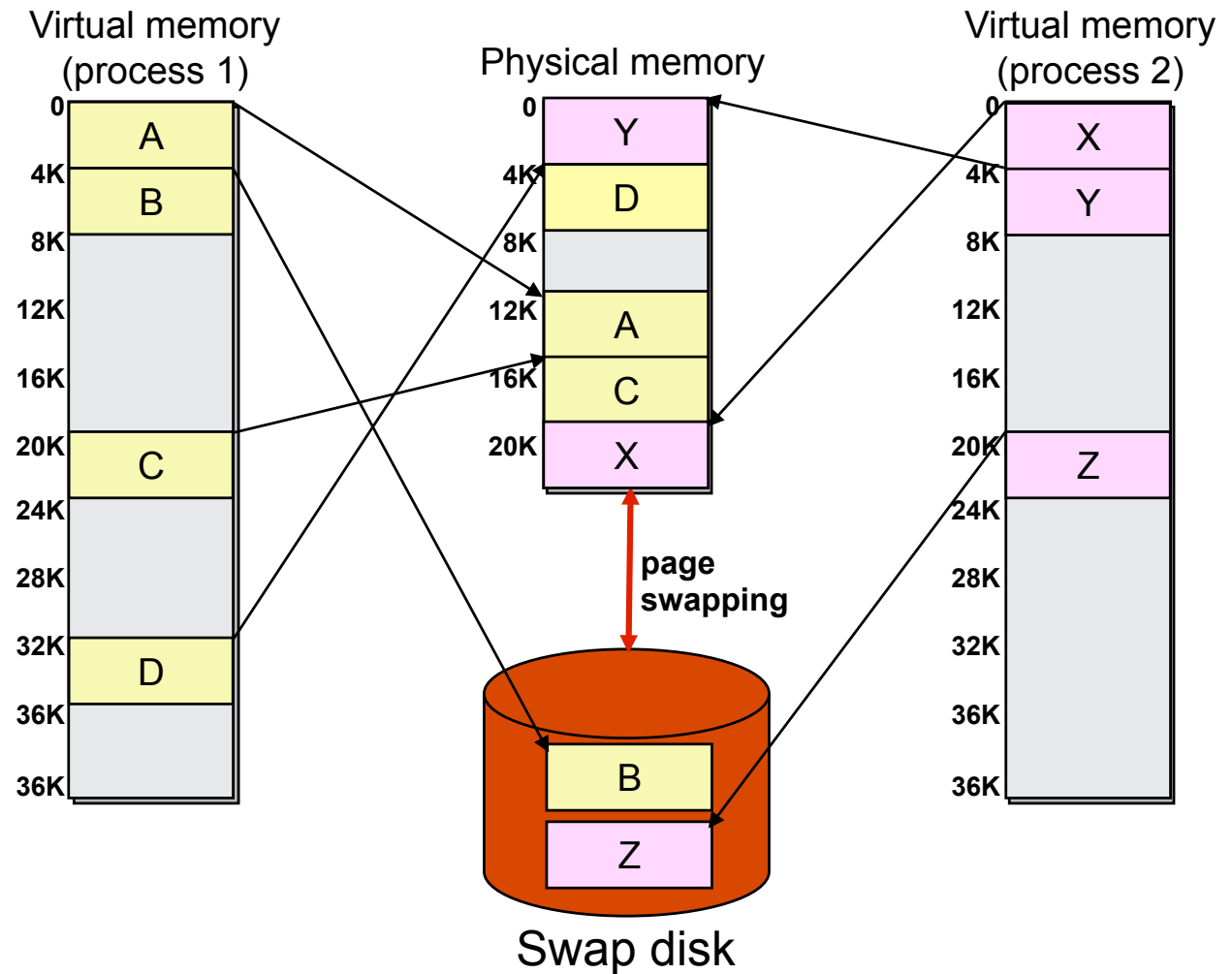
---

## Basic idea:

- Each process has its own Virtual Address Space, divided into fixed-sized pages
- Virtual pages that are in use get mapped to pages of physical memory (called **page frames**).
  - Virtual memory: pages
  - Physical memory: frames
- Virtual pages not recently used may be stored on disk
- Extends the memory hierarchy out to the swap partition of a disk

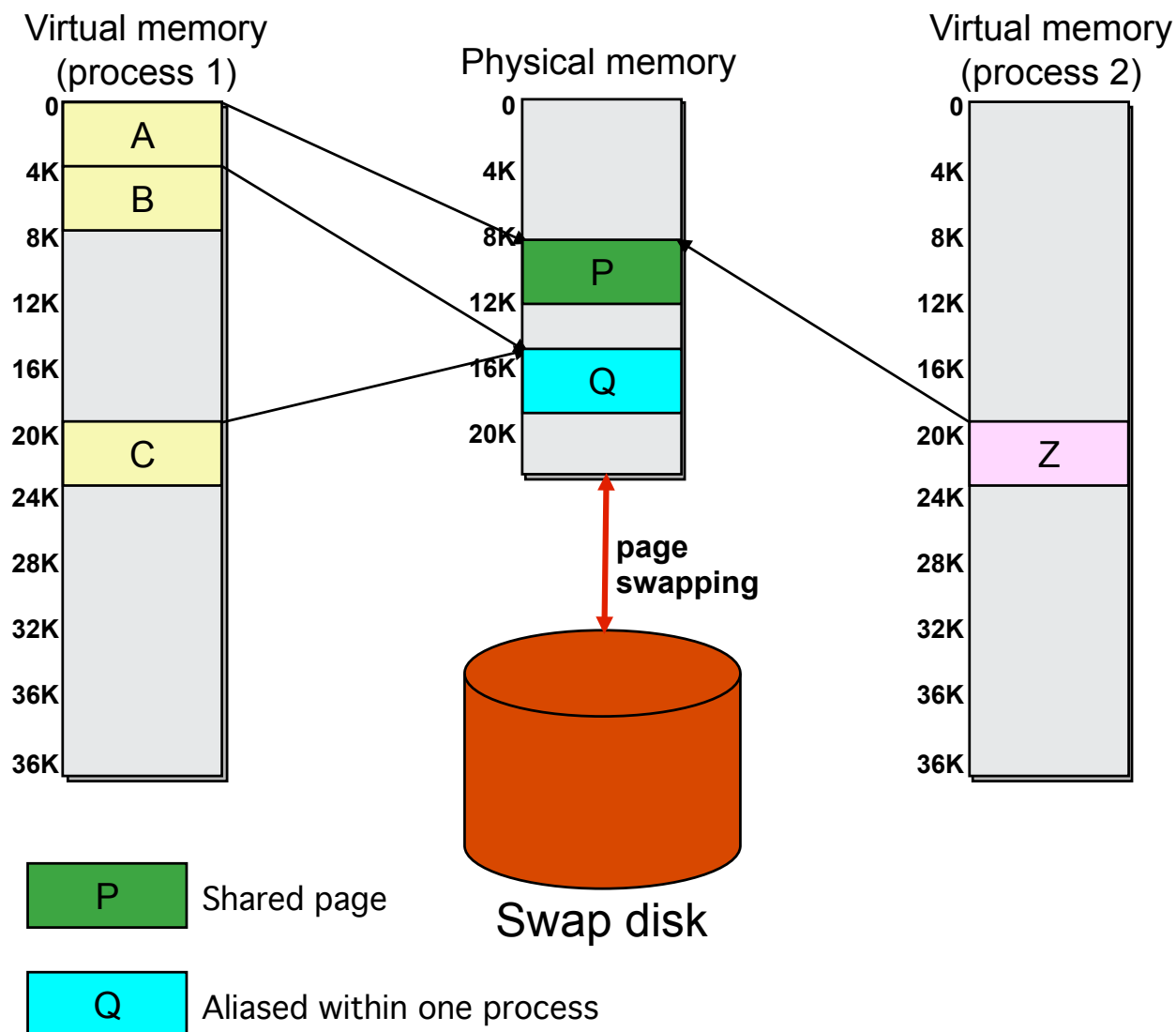
# Virtual and Physical Memory

- Example 4K page size
- Process 1 has pages A, B, C and D
- Page B is held on disk
- Process 2 has pages X, Y, Z
- Page Z is held on disk
- Process 1 cannot access pages X, Y, Z
- Process 2 cannot access page A, B, C, D
- O/S can access any page (full privileges)



# Sharing memory using Virtual Aliases (Synonym)

- Process 1 and Process 2 want to share a page of memory
- Process 1 maps virtual page A to physical page P
- Process 2 maps virtual page Z to physical page P
- Permissions can vary between the sharing processors.
- Note: Process 1 can also map the same physical page at multiple virtual addresses !!



# Typical Virtual Memory<sup>1</sup> Parameters

parameter	L1 cache	memory
Size	4KB-64KB	128MB-1TB
block/page	16-128 bytes	4KB-4GB
hit time	1-3 cycles	100-300 cycles
miss penalty	8-300 cycles	1M-10M cycles
miss rate	0.1-10%	0.00001-0.001%

**H&P 5/e  
Fig. B.20**

- Modern OS's support several page sizes for flexibility. On Linux:
  - Normal pages: 4KB
  - Huge pages: 2MB or 1GB
- Virtual Memory miss is called a **page fault**

<sup>1</sup> *Note: these parameters are due to a combination of physical memory organization and virtual memory implementation*



# Virtual Memory Policies

---

- Block identification: finding the correct page frame
  - Assigning tags to memory page frames and comparing tags is impractical
  - OS maintains a table that maps all virtual pages to physical page frames: **Page Table (PT)**
  - The OS updates the PT with a new mapping whenever it allocates a page frame to a virtual page
  - PT is accessed on a memory request to translate virtual to physical address → inefficient!
    - Solution: cache translations (TLB)
  - One PT per process and one for the OS



# Virtual Memory Policies

---

- Block placement: location of a page in memory
  - More freedom → lower miss rates, higher hit and miss penalties
  - Memory access time is already high and memory miss penalty (i.e., disk access time) is huge ⇒ must minimize miss rates
  - As a result, memory is fully associative → a virtual page can be located in any page frame
    - No conflict misses
    - Important to reduce time to find a page in memory (hit time)
  - To place new pages in memory, OS maintains a list of free frames
  
- Block placement may be constrained by use of translated virtual address bits when indexing the cache (see later)

# Virtual Memory Policies

---

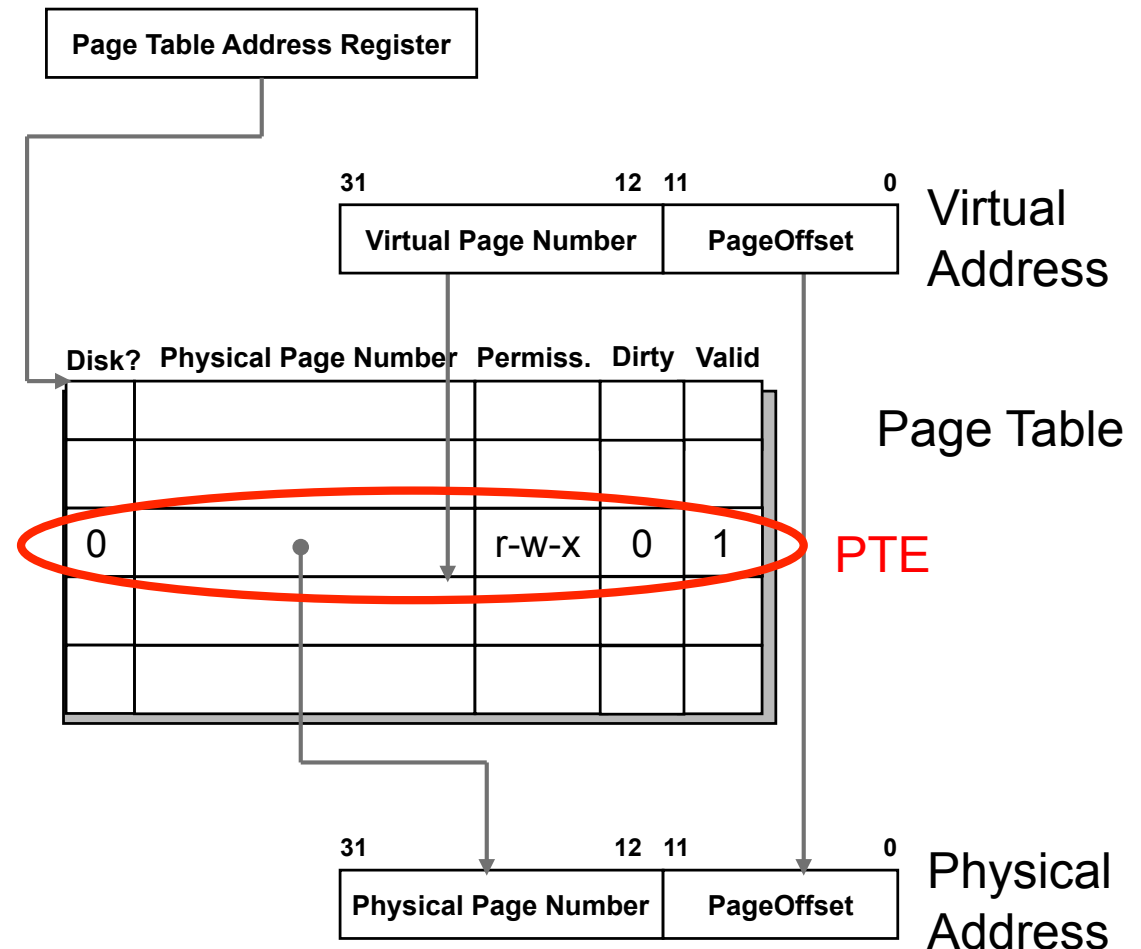
- Block replacement: choosing a page frame to reuse
  - Minimize misses (page faults) → LRU policy
    - True LRU expensive – must minimize CPU time of the algorithm
    - Simple solution: OS sets a Used bit whenever a page is accessed in a time quantum. In the next quantum, any page with its Used bit clear is eligible for replacement.
      - This requires 2 sets of Used bits
  - Minimize write backs to disk → give priority to **clean** pages
  
- Write strategy: what happens when a page is written
  - Write-through: would mean writing the cache block back to disk whenever the page is updated in main memory
    - not practical due to latency and bandwidth considerations (~4 orders of magnitude latency gap between memory & disk)
  - Write-back: the norm in today's virtual memory systems
    - OS tracks modified pages through the use of Dirty bits in page table entries



# Page Tables and Address Translation

## Page Table Entry (PTE):

- Track access permissions for each page
  - Read, Write, Execute
- Bit indicates if page is on disk, in which case Physical Page Number indicates location within swap file
- “Dirty” bit indicates if there were any writes to the page
- 4B per PTE in this example





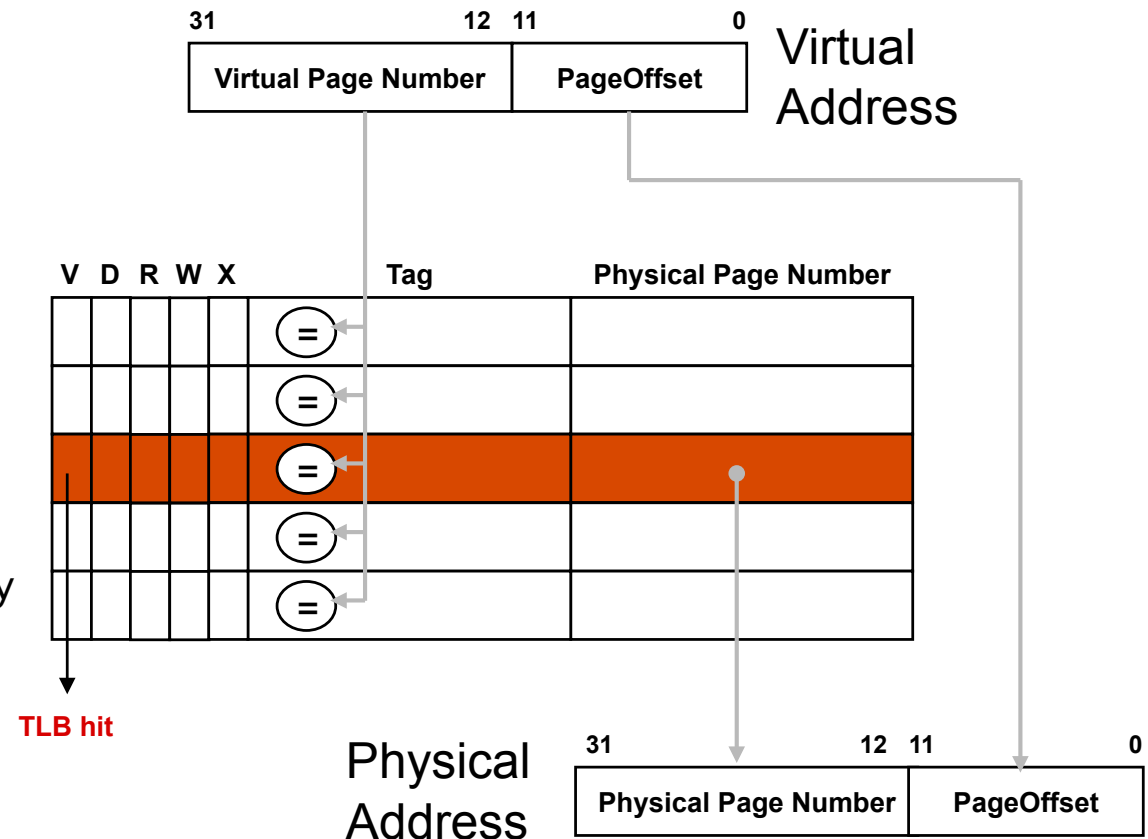
# Making Page Tables space-efficient

---

- The number of entries in the table is the number of virtual pages → many!
  - e.g., 4KB pages
    - $2^{20}=1\text{M}$  entries for a 32b address space → need 4MB/process
    - $2^{52}$  entries for a 64b address space → petabytes per process!
  - Solution:
    - Exploit the observation that the virtual address space of each process is sparse → only a fraction of all virtual addresses actually used
    - hash virtual addresses to avoid maintaining a map from each virtual page (many) to physical frame (few).
    - Resulting structure is called the **inverted page table**
- Other (complementary) solutions:
  - Store PTs in the virtual memory of the OS, and swap out recently unused portions
  - Use large pages

# Fast address translation: TLB

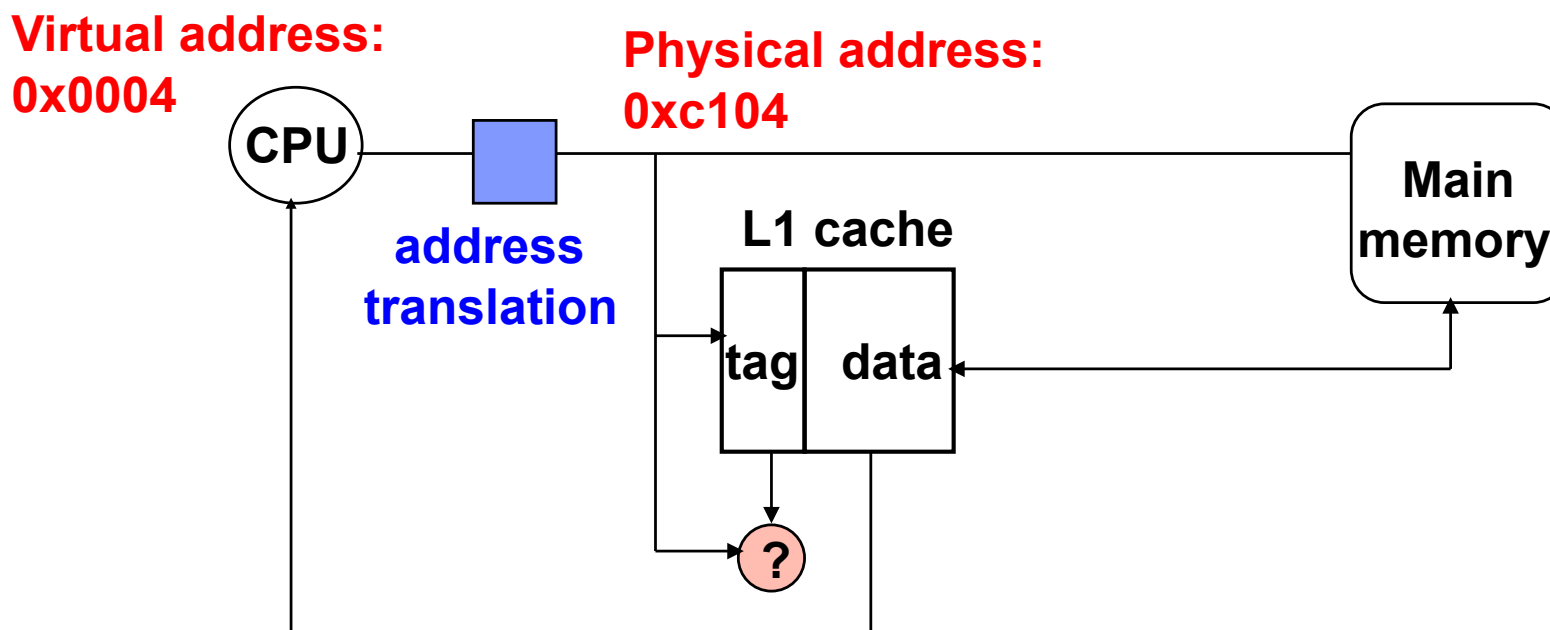
- Typically a small, fully-associative cache of Page Table Entries (PTE)
- Tag given by VPN for that PTE
- PPN taken from PTE
- Valid bit required
- D bit (dirty) indicates whether page has been modified
- R, W, X bits indicate Read, Write and Execute permission
- Permissions are checked on every memory access
- Physical address formed from PPN and Page Offset
- TLB Exceptions:
  - TLB miss (no matching entry)
  - Privilege violation
- Often separate TLBs for Instruction and Data references



# How to address a cache in a virtual-memory system

Option 1: **physically-addressed caches** → perform address translation before cache access

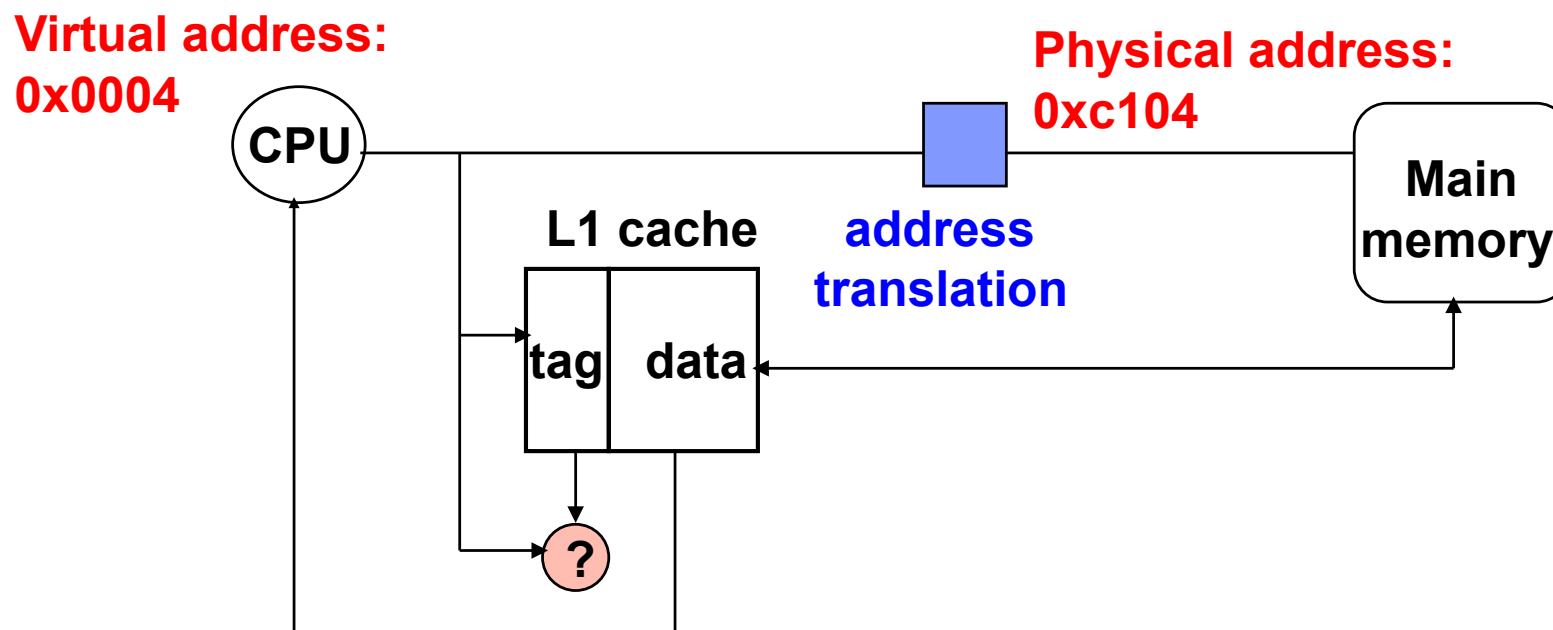
- Hit time is increased to accommodate translation ☹️



# How to address a cache in a virtual-memory system

Option 2: **virtually-addressed caches** → perform address translation after cache access if miss

- Hit time does not include translation 😊
- Aliases ☹️



# Problems with virtually addressed caches

---

- Virtually tagged data cache problems:
  - A program may use different virtual addresses pointing to the same physical address (Aliases or Synonyms)
    - Two copies could exist in the same data cache
    - Writing to copy 1 would not be reflected in copy 2
    - Reading copy 2 would get stale data
    - Thus, does not provide a coherent view of memory
  - Also, must be able to distinguish across different processes: same VA, different PA (Homonyms)

# Solutions for handling homonyms and synonyms

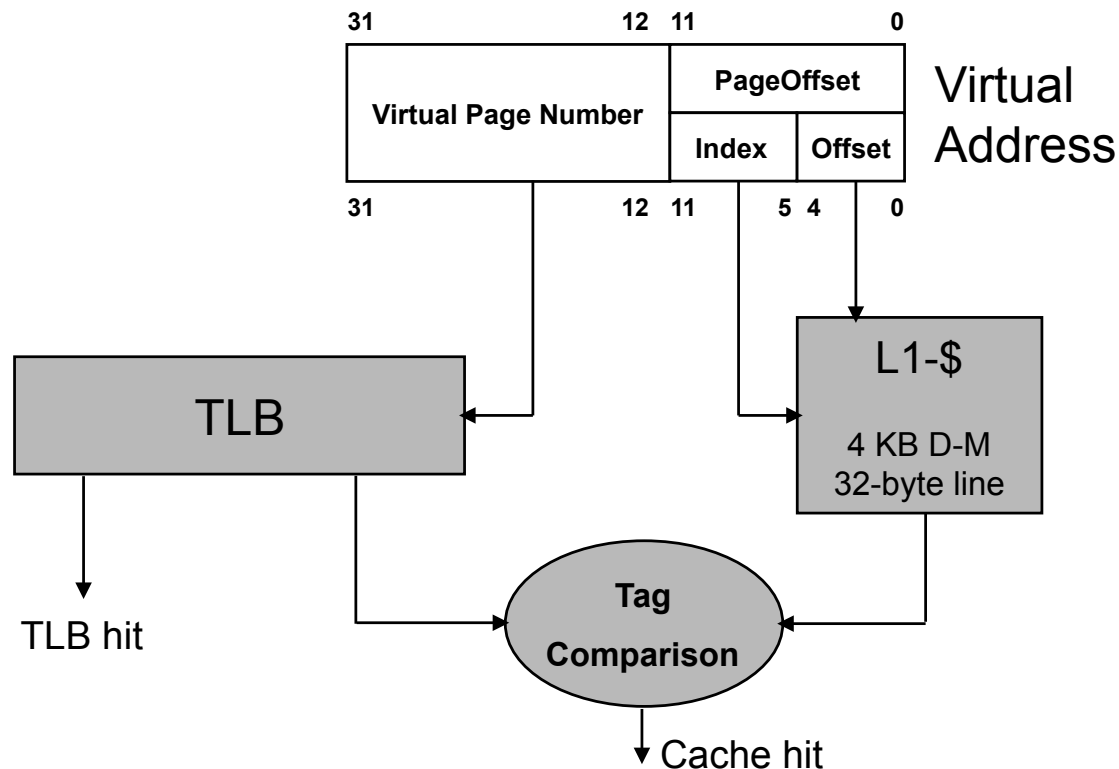
---



- Flush cache on context switch or add process ID to each tag
  - Will solve the homonym problem
  - But will not solve the synonym problem.
- Use physically addressed caches
  - Will solve homonym problem.
  - Will also solve synonym problem.
    - Synonyms all have same physical address, thus one copy exists in each cache
  - Implication: need to do address translation before accessing cache.
- Use physically addressed tags?
  - Must translate addresses before cache tag check
  - May still be able to index cache using non-translated low-order address bits under certain circumstances.

# VI-PT: translating in parallel with L1-\$ access

- Access TLB and L1-\$ in parallel
- Requires that L1-\$ index be obtained from the non-translated bits of the virtual address.
- This constraint in the number of bits available for the index limits the size of the cache!**



**IMPORTANT:**  
 If the cache Index extends beyond bit 11, into the translated part of the address, then translation must take place before the cache can be indexed





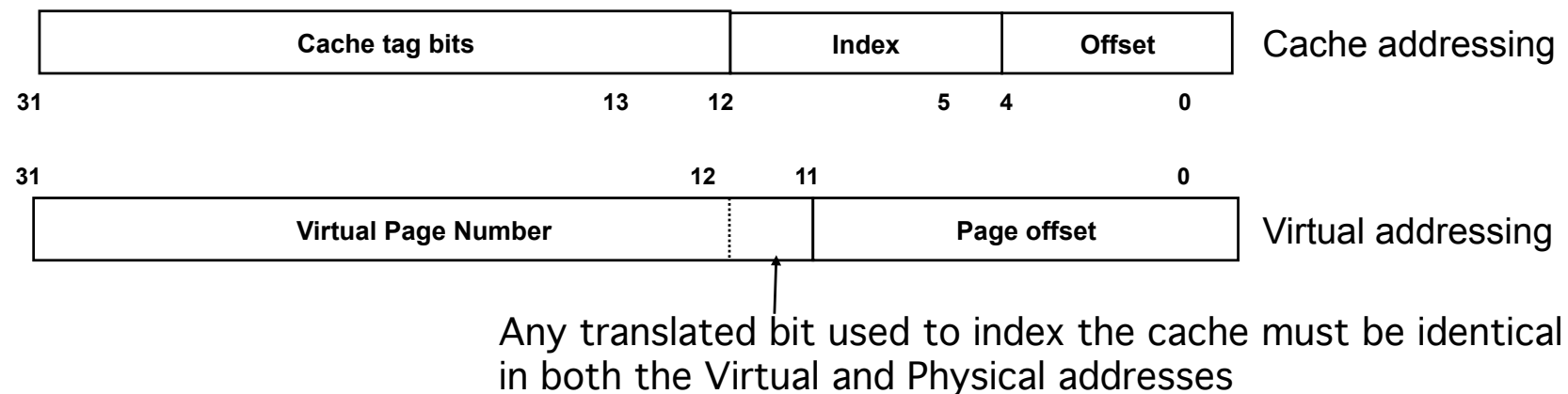
# Coping with large VI-PT caches

---

- Multi-way caches: multiple blocks in the same set
  - E.g., Intel Haswell: 32KB 8-way cache w/ 4KB pages
  - High associativity affords large capacity
- Check other potential sets for aliases on a miss
  - E.g., AMD Opteron: 64KB 2-way cache w/ 4KB pages
  - on a miss, 7 add'l cycles to check for aliases in other sets
- Larger page size: more bits available for the index
  - Not a universal solution, since most OS' normal page size is 4-8KB

# Coping with large VI-PT caches (con'd)

- Rely on page allocator in the O/S to allocate pages such that the translation of index bits would always be an identity relation
  - Hence, if virtual address A translates to physical address P, then Page Allocator must guarantee that:  $V[12] == P[12]$
  - This approach is referred to as “page coloring”.



# Summary: how to address a cache

---

- **PI-PT** : Physically indexed, physically tagged
  - Translation first; then cache access
  - Con: Translation occurs in sequence with L1-\$ access → high latency
- **VI-VT** : Virtually indexed, virtually tagged
  - L1-\$ indexed with virtual address, tag contains virtual address
  - Con: Cannot distinguish synonyms/homonyms in cache
  - Pro: Only perform TLB lookup on L1-\$ miss
- **VI-PT** : Virtually indexed, physically tagged
  - L1-\$ indexed with virtual address, or often just the un-translated bits
  - Translation must take place before tag can be checked
  - Con: Translation must take place on every L1-\$ access
  - Pro: No synonyms/homonyms in the cache
- **PI-VT** : Physically indexed, virtually tagged
  - Not interesting