**System 5 Introduction**

Is there a Wedge in this 3D scene?

Data a stereo pair of images!

3D part recognition using geometric stereo

**Binocular Stereo**

Goal: build 3D scene description (e.g., depth) given two 2D image descriptions

Useful for: obstacle avoidance, grasping, object location

Key principle: triangulation

**Stereo vision - a solution**

1) **Feature extraction**

2) **Feature matching**:

3) **Triangulation**:

Given two 2D images of an object, how can we reconstruct 3D awareness of it?
Possible image features

1) Edge fragments

2) Edge structures (e.g., vertical indoor lines)

System 5 Overview

1. Feature extraction:
   - Canny edge detector
   - RANSAC straight line finding
   - SIFT point features

2. Feature matching:
   - Stereo correspondence matching lines
   - SIFT points

3. Triangulation:
   - 3D line feature position estimation

4. 3D Object recognition:
   - 3D geometric model
   - Model-data matching
   - 3D pose estimation

Edge Detector Introduction

- Edge detection: find pixels at large changes in intensity
- Much historical work on this topic in computer vision (Roberts, Sobel)
- Canny edge detector first modern edge detector and still commonly used today
- Edge detection never very accurate process: image noise, areas of low contrast, a question of scale. Humans see edges where none exist.
**Canny Edge Detector**

Four stages:
1. Gaussian smoothing: to reduce noise and smooth away small edges
2. Gradient calculation: to locate potential edge areas
3. Non-maximal suppression: to locate “best” edge positions
4. Hysteresis edge tracking: to locate reliable, but weak edges

**Canny: Gaussian Smoothing**

Convolve with a 2D Gaussian

\[
\text{mask}(r, c) = \frac{1}{2\pi\sigma} e^{-\frac{r^2+c^2}{2\sigma^2}}
\]

Larger \(\sigma\) gives more smoothing - low pass filter

**Gaussian Smoothing Examples**

\(\sigma = 2\)

\(\sigma = 4\)
Conservative Smoothing
Gaussian smoothing inappropriate for salt&pepper/spot noise

Noisy image  Gauss smooth  Conservative

Canny: Gradient Magnitude Calculation

$G(r, c)$ is smoothed image

Compute local derivatives in the r and c directions as $G_r(r, c), G_c(r, c)$:

Edge gradient: $\nabla G(r, c) = (G_r(r, c), G_c(r, c))$

Gradient magnitude:

$$H(r, c) = \sqrt{G_r(r, c)^2 + G_c(r, c)^2}$$

$$\approx |G_r(r, c)| + |G_c(r, c)|$$

Gradient direction

$$\theta(r, c) = \arctan(G_r(r, c), G_c(r, c))$$

$$G_r(r, c) = \frac{\partial G}{\partial r} = \lim_{h \to 0} \frac{G(r + h, c) - G(r, c)}{h}$$

$$\approx G(r + 1, c) - G(r, c)$$

σ controls amount of smoothing
Smaller σ gives more detail & noise
Larger σ gives less detail & noise

σ = 2  σ = 4
Canny: Non-maximal Suppression

Where exactly is the edge? peak of gradient
Suppress lower gradient magnitude values: need to check ACROSS gradient

\[
\begin{align*}
0 & 0 3 12 4 0 \\
0 & 0 6 10 2 0 \\
0 & 2 8 7 1 0 \\
0 & 3 11 4 0 0 \\
\end{align*}
\]

Canny: Hysteresis Tracking

Start edges at certainty: \( H > \tau_{\text{start}} \)
Reduce requirements at connected edges to get weaker edges: \( H > \tau_{\text{continue}} \)

Matlab has Canny:
\[
\text{edge(leftr,'canny',[0.08,0.2],3)};
\]
Midlecture Problem
Where might the Canny edge detector find edges in this image?

Finding Lines from Edges
RANSAC: Random Sample and Consensus

Model-based feature detection: features based on some \textit{a priori} model

Works even in much noise and clutter

Tunable failure rate

Assume

- Shape of feature determined by $T$ true data points
- Hypothesized feature is valid if $V$ data points nearby

RANSAC Pseudocode

\begin{verbatim}
for i = 1 : Trials
    Select T data points randomly
    Estimate feature parameters
    if number of nearby data points $> V$
        return success
    end
end
return failure
\end{verbatim}

RANSAC Termination Limit

$p_{\text{all-f}}$ is probability of algorithm failing to detect a feature

$p_1$ is probability of a data point belonging to a valid feature

$p_d$ is probability of a data point belonging to same feature

Algorithm fails if Trials consecutive failures

$$p_{\text{all-f}} = (p_{\text{one-f}})^{\text{T}rials}$$

Success if all needed $T$ random data items are valid

$$p_{\text{one-f}} = 1 - p_1(p_d)^{T-1}$$

Solving for expected number of trials:

$$\text{T}rials = \frac{\log(p_{\text{all-f}})}{\log(1 - p_1(p_d)^{T-1})}$$
RANSAC Line Detection

Line model: infinite line through 2 points ($T = 2$)
$T = 2$ edge points randomly chosen
Accept if $V = 80$ edge points within 3 pixels

$P_{a1} - P_{a1} = 0.001$, $P_{a1} = 0.1$, $P_{a1} = 0.01$, Trials = 688

Mostly accurate lines, but don’t know endpoints

Finding line segments

Some random data crossings
Want to find approximate observed start and end of true segment

1. Project points $\{x_i\}$ onto ideal line thru point $p$ with direction $\lambda_i$:

$$\lambda_i = (x_i - p) \cdot a$$
Projected point is $p + \lambda_i a$

2. Remove points not having 43 neighbor points within 45 pixels distance

3. Endpoints are given by smallest and largest remaining $\lambda_i$.

Found line segments

SIFT Features

SIFT: Scale Invariant Feature Transform
Image point feature + local description
(128 vector)
Sparse, reasonably distinguishable points
Invariant to translation, rotation, scale, some 3D
Example feature locations

Matching Applications

Matchable features for:
- Object recognition
- Model-data alignment
- Image registration
- Stereo matching

Four Step Algorithm

1. Detect extremal points in scale space
2. Accurate keypoint localization
3. Feature orientation estimation
4. Keypoint descriptor calculation

Scale Space Smoothing

Gaussian smoothing via convolution

\[ L(x, y, \sigma) = G(x, y, \sigma) \circ I(x, y) \]

\[ G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2+y^2)/2\sigma^2} \]

Difference of Gaussians:

\[ D(x, y, n) = L(x, y, 2^n) - L(x, y, 2^{n-1}) \]

where \( n = 1 \ldots N \)

\( S = 3 \) best
Scale Space

Point Extrema

Pick extremal points larger/smaller than their 26 neighbours:

Subpixel Extrema Localization

Hessian:

\[
H = \begin{bmatrix}
\frac{\partial^2 D}{\partial x^2} & \frac{\partial^2 D}{\partial x \partial y} & \frac{\partial^2 D}{\partial x \partial \sigma} \\
\frac{\partial^2 D}{\partial x \partial y} & \frac{\partial^2 D}{\partial y^2} & \frac{\partial^2 D}{\partial y \partial \sigma} \\
\frac{\partial^2 D}{\partial x \partial \sigma} & \frac{\partial^2 D}{\partial y \partial \sigma} & \frac{\partial^2 D}{\partial \sigma^2}
\end{bmatrix}
\]

Optimal position is \((x, y, \sigma) + \hat{x}\), where

\[
\hat{x} = -H^{-1} \begin{bmatrix}
\frac{\partial D}{\partial x} \\
\frac{\partial D}{\partial y} \\
\frac{\partial D}{\partial \sigma}
\end{bmatrix}
\]
**Low Contrast Extrema Pruning**

Predict DoG value at extrema:

\[ p = |D(x, y, \sigma) + \frac{1}{2} \left[ \frac{\partial D}{\partial x}, \frac{\partial D}{\partial y}, \frac{\partial D}{\partial \sigma} \right] \hat{x} | \]

Reject if \( p < 0.03 \)

**Unstable Point Extrema Pruning**

Let

\[ H = \begin{bmatrix} \frac{\partial^2 D}{\partial x^2} & \frac{\partial^2 D}{\partial x \partial y} \\ \frac{\partial^2 D}{\partial x \partial y} & \frac{\partial^2 D}{\partial y^2} \end{bmatrix} \]

Reject if \( \det(H) < 0 \) or

\[ \frac{\text{trace}(H)^2}{\det(H)} > \tau \text{ (e.g. 12)} \]

Rejects points that can slide along an edge

**Getting Rotation Invariance**

Local orientation \( \hat{\theta} \) estimation

Use keypoint scale \( \sigma \)

Let \( \vec{v} = \nabla L(r, s, \sigma) \) for \((r, s) \in \text{neigh}(x, y)\)

Compute strength \( m = |\vec{v}| \) and \( \theta = \text{direction}(\vec{v}) \)

Compute histogram of \( \theta \) values weighted by \( m \)

Pick top peak direction \( \hat{\theta} \) in histogram for feature orientation

**Local Descriptor Computation**

Use 16 \( \times \) 16 neighbourhood about feature point

Subdivided into 16 \( 4 \times 4 \) pixel blocks

Create an 8 orientation histogram for each block \( \rightarrow 128 \) vector

Compute gradient orientation at each point

Rotate all orientations by \( \hat{\theta} \) (for invariance)

Add to histogram weighted (details in paper)

Normalize 128 vector to unit length for illumination invariance

Descriptor similarity using Euclidean distance
Descriptor Example

4 histograms from 8 × 8 neighbourhood about feature point:

Example Points

Rotation & Scale Invariance

SIFT Summary

- Sparse, distinctive point features
- Translation independent by using local histogram
- Rotation independent by orientation adjustment
- Scale independent by extremal scale estimation
- Illumination independent by descriptor normalisation
- Widely used
- Real-time implementation possible
SIFT References

en.wikipedia.org/wiki/Scale-invariant_feature_transform

Stereo Overview

Stereo Correspondence Problem

Which feature in left image matches a given feature in the right?

LEFT

RIGHT

WHICH?

Different pairings give different depth results
Often considered the key problem of stereo

Constraining Matches: Edge Direction

Match features with nearly same orientation
Constraining Matches: Edge Contrast

Match features with nearly same contrast across edge

Constraining Matches: Feature Shape

Match features with nearly same length

Constraining Matches: Uniqueness and Smoothness

Smoothness: match features giving nearly same depth as neighbors

Uniqueness: a feature in one image can match from the other image:

- 0 - occlusion
- 1 - normal case
- 2+ - transparencies, wires, vines, etc from coincidental alignments

Midlecture Problem

Which stereo correspondence constraint would you use to reject these matches?
Image Projection Geometry

Pinhole camera model: Matrix $P_i$ projects 3D point $\vec{v} = (x, y, z, 1)'$ onto image point $\vec{u}_i = (r_i, c_i, 1)'$.

Notice use of homogeneous coordinates in 2D and 3D.

Projection matrix $P_i$ decomposes as

$$P_i = K_i R_i [I - e_i']$$

where $R_i$ : orientation of camera (3 degrees of freedom)
$e_i = (e_{xi}, e_{yi}, e_{zi})'$ : camera center in world (3 DoF)

$K_i$ : camera intrinsic calibration matrix =

$$
\begin{bmatrix}
    f_{mi} & s_i & r_{0i} \\
    0 & f_{ci} & c_{0i} \\
    0 & 0 & 1
\end{bmatrix}
$$

$f_i$ : camera focal length in mm
$m_{ri}, m_{ci}$ : row, col pixels/mm conversion on image plane
$r_{0i}, c_{0i}$ : where optical axis intersects image plane
$s_i$ : skew factor

12 parameters (11 Degrees of Freedom) per camera.

Constraining Matches: Epipolar Geometry

Feature $\vec{p}_l$ in left image lies on a ray $\vec{r}$ thru space.
$\vec{r}$ projects to an epipolar line $e$ in the right image, along which the matching image feature must lie.

If images are ‘rectified’, then the epipolar line is an image row. Reduces 2D search to 1D search.

Images are linked by the Fundamental matrix $F$

Matched points satisfy $\vec{p}_l^t F \vec{p}_r = 0$

(Points are in homogeneous coordinates, $F$ is $3 \times 3$)
Stereo Matching Results

Maximally consistent set of matches
Based on local and epipolar constraints

Estimating the Fundamental matrix

Assume \( N \geq 7 \) matched points \( \vec{u}_i : \vec{v}_i, i = 1 \ldots N \) in 2 images
Each should satisfy \( \vec{u}_i^T F \vec{v}_i = 0 \)
Noisy, so use a least squares algorithm. Expanding \( \vec{u}_i^T F \vec{v}_i \) gives an equation in \( N \) variables:

\[
[u_{ix} v_{iy}, u_{ix} v_{iy}, u_{ix}, u_{iy}, v_{ix}, u_{iy}, v_{ix}, v_{iy}, 1]^T \vec{f} = A_i \vec{f} = 0
\]
when we unfold

\[
F = \begin{bmatrix} f_{11} & f_{12} & f_{13} \\ f_{21} & f_{22} & f_{23} \\ f_{31} & f_{32} & f_{33} \end{bmatrix}
\]

into \( \vec{f} = (f_{11}, f_{12}, f_{13}, f_{21}, f_{22}, f_{23}, f_{31}, f_{32}, f_{33})' \).

Then we stack the \( A_i \) up as:

\[
A \vec{f} = \begin{bmatrix} A_1 \\ \vdots \\ A_N \end{bmatrix} \vec{f} = 0
\]

Solve for \( \vec{f} \): svd(\( A \)) = \( UDV' \), \( \vec{f} = V(:, 9) \) (Plus some numerical fixes)

Not numerically best algorithm, but simple to understand
See Hartley and Zisserman Chapter 10

Epipoles

Line connecting the 2 camera centres intersects the image planes

Estimate epipoles \( \vec{e}_l, \vec{e}_r \), by exploiting \( \vec{e}_l^T F = F \vec{e}_r = \vec{0} \)

Solve 3 equations
in 2 variables for unknown epipoles \( (e_{lx}, e_{ly}, 1)F = (e_{rx}, e_{ry}, 1)' = \vec{0} \)
\( e_R = \text{null}(F, 'r'); e_L = e_R/e_R(3) \) \( eL = \text{null}(F'); eL = eL/eL(3) \)
Estimating Projection Matrices

Use the epipoles

\[ P_L = K_L \cdot \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \]

\[ P_R = K_R \cdot \begin{bmatrix} 0 & -1 & e_{ry} \\ 1 & 0 & -e_{rx} \\ -e_{ry} & e_{rx} & 0 \end{bmatrix} \cdot F \cdot \vec{e}_r \]

3D Line Calculation

**Aim:** recovery of 3D line positions

**Assume:** line successfully matched in L & R images

1. Compute 3D plane that goes through image line and camera origin
2. Compute intersection of 3D planes from 2 cameras (which gives a line)

3D Plane Intersection → 3D Line

Let \( \vec{l}_L \) and \( \vec{l}_R \) be the left and right image lines (2D, but in homogeneous coordinates)

3D line represented by \( 2 \times 4 \) matrix:

\[
L = \begin{bmatrix} \vec{p}_L P_L \\ \vec{p}_R P_R \end{bmatrix}
\]
### Matched Lines

![Matched Lines Diagram]

### 3D Line Equations

<table>
<thead>
<tr>
<th>Number</th>
<th>Pairs</th>
<th>direction</th>
<th>point</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>L1:R4</td>
<td>(-0.82, 0.08,-0.56)</td>
<td>(9.1,2.0,-13.0)</td>
</tr>
<tr>
<td>2</td>
<td>L5:R11</td>
<td>( 0.61,-0.06, 0.78)</td>
<td>(-125.3,98.6,107.1)</td>
</tr>
<tr>
<td>3</td>
<td>L6:R7</td>
<td>(-0.28,-0.95,-0.03)</td>
<td>(0.9,-10.6,294.4)</td>
</tr>
<tr>
<td>4</td>
<td>L7:R2</td>
<td>( 0.07,-0.62,-0.77)</td>
<td>(48.3,-97.0,82.9)</td>
</tr>
<tr>
<td>5</td>
<td>L8:R5</td>
<td>(-0.18,-0.45, 0.87)</td>
<td>(114.8,91.8,72.1)</td>
</tr>
<tr>
<td>6</td>
<td>L10:R12</td>
<td>(-0.50,-0.73, 0.44)</td>
<td>(71.5,77.0,208.8)</td>
</tr>
<tr>
<td>7</td>
<td>L11:R10</td>
<td>( 0.79,-0.20, 0.57)</td>
<td>(-98.4,57.2,154.6)</td>
</tr>
<tr>
<td>8</td>
<td>L12:R3</td>
<td>( 0.11,-0.69,-0.70)</td>
<td>(110.4,-123.6,140.1)</td>
</tr>
</tbody>
</table>

### Projected Stereo Line Positions

A little off, but: 1) calibration errors, 2) didn’t account for lens distortion

### Angles Between Lines

<table>
<thead>
<tr>
<th>3D line 1</th>
<th>3D line 2</th>
<th>Angle</th>
<th>True</th>
</tr>
</thead>
<tbody>
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<td>2</td>
<td>3</td>
<td>1.4347</td>
<td>1.57</td>
</tr>
<tr>
<td>2</td>
<td>4</td>
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<tr>
<td>2</td>
<td>5</td>
<td>0.9281</td>
<td>1.57</td>
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<tr>
<td>2</td>
<td>6</td>
<td>1.4863</td>
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</tr>
<tr>
<td>2</td>
<td>7</td>
<td>0.3023</td>
<td>0.00</td>
</tr>
<tr>
<td>2</td>
<td>8</td>
<td>1.1186</td>
<td>1.57</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
<td>0.9180</td>
<td>0.71</td>
</tr>
<tr>
<td>3</td>
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<td>5</td>
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<td>7</td>
<td>8</td>
<td>1.3918</td>
<td>1.57</td>
</tr>
</tbody>
</table>
3D Edge Based Recognition Pipeline

- 3D Stereo Edge Data
- Geometric Model
- Verification Failure (redo matching)
- Model Matching
- Pose Estimation
- Verification

Recognition: True/False
Position: translation/rotation

3D Edge Based Recognition

Match 3D data edges to 3D wireframe model edges

Model =
- (0,0,0)-(67,0,0)
- (0,0,0)-(0,0,46)
- (67,0,0)-(67,0,46)
- (0,67,0)-(0,67,46)
- (0,0,46)-(0,67,46)
- (67,0,0)-(0,67,0)
- (67,0,46)-(0,67,46)

3D Model Matching

Use Interpretation Tree algorithm: match edges, Limit = 5

Unary test: similar length $|l_m - l_d| < \tau(l_m + l_d)$

Binary test: similar angle between pairs: $|\theta_m - \theta_d| < \tau_a$

Matching Performance

144 interpretation tree matches thru to pose estimation and verification

Two valid solutions found (symmetric model rotated 180 degrees)

<table>
<thead>
<tr>
<th>Segment</th>
<th>Model 1</th>
<th>Model 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>M8</td>
<td>M9</td>
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<tr>
<td>4</td>
<td>M2</td>
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<td>M7</td>
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<tr>
<td>7</td>
<td>M3</td>
<td>M3</td>
</tr>
<tr>
<td>8</td>
<td>M7</td>
<td>M1</td>
</tr>
</tbody>
</table>
### 3D Pose Estimation

**Given:** matched line directions \{ (\vec{m}_i, \vec{d}_i) \} and points on corresponding lines (but not necessarily same point positions) \{ (\vec{a}_i, \vec{b}_i) \}

**Rotation** (matrix \( R \)): estimate rotation from matched vectors (same as previous task) except:
1) use line directions instead of surface normals
2) don’t know which \( \pm \) direction for edge correspondence: try both for each matched segment
3) if \( \text{det}(R) = -1 \) then need to flip symmetry
4) verify rotation by comparing rotated model and data line orientations

### 3D Translation Estimation

Given \( N \) paired model and data segments, with point \( \vec{a}_i \) on model segment \( i \) and \( \vec{b}_i \) on data segment \( i \)

Direction \( \vec{d}_i \) of data segment \( i \)

Previously estimated rotation \( R \)

\[
\vec{d}'_i = R \vec{d}_i
\]

\( \vec{t} = \vec{t} - \vec{b} - \vec{d}'_i \) (\( \vec{d}'_i \) is translation error to minimize)

Goal: find \( \vec{t} \) that minimizes \( \sum \lambda_i \vec{t} \lambda_i \)

How:
\[
\begin{align*}
L &= \sum_i (I - \vec{d}_i \vec{d}'_i)' (I - \vec{d}_i \vec{d}'_i) \\
\vec{n} &= \sum_i (I - \vec{d}_i \vec{d}'_i)' (I - \vec{d}_i \vec{d}'_i) (R \vec{a}_i - \vec{b}_i) \\
\vec{t} &= L^{-1} \vec{n}
\end{align*}
\]

Verify translation by comparing perpendicular distance of transformed model endpoints to data line

287 verify attempts (2 successes)
Discussion

- Hard to find reliable edges/lines, but Canny finds most reasonable edges and RANSAC can put them together for lines
- Given enough stereo correspondence constraints, can get reasonably correct correspondences
- Large features help stereo matching but require more preprocessing
- Stereo geometry easy but needs accurate calibration: not always easy, but now possible to autocalibrate using 7 matched points
- Binocular feature matching stereo gives good 3D at corresponding features, but nothing in between: use scan line stereo?

Dense Depth Data

**Problem:** have depth only at triangulated feature locations

**Solution 1:** Linear interpolate known values at all other pixels

**Solution 2:** Correlation-based stereo

- Use pixel neighborhoods as features
- Triangulate depth at every pixel
- But needs to find matching pixel - not easy

Correlation based stereo

- Use stereo image pair
- Features are neighborhoods at each pixel
- Match using similarity metric: SSD - Sum of Squared Differences (of pixel values) of left image at \((u, v)\) to right image at \((r, s)\):

\[
SSD(u, v, r, s) = \sum_{i=-N/2}^{N/2} \sum_{j=-N/2}^{N/2} (L(u+i, v+j) - R(r+i, s+j))^2
\]

Finding best match

For each scanline on rectified image pair:

1. Build array of all possible matching scores
2. Dynamic programming finds lowest cost path (bright line thru middle of array above - optimisation problem)
What We Have Learned

Feature based stereo:
- Feature detection: Canny & RANSAC
- Stereo matching: local & epipolar constraints
- Triangulation & 3D: epipolar geometry
- Recognition: IT algorithm & verification

Correlation based stereo: similar but using pixel neighbourhoods

The Course

- intensity, stereo and range sensors
- Feature detection: curve segmentation, Canny edges, plane region growing, RANSAC line detector, least square estimation
- Geometric coordinate systems, modeling, recognition and pose estimation: 2D and 3D
- Matching algorithms: Interpretation Tree
- Match verification by feature alignment
- Point distribution modelling for variable shapes