Advanced Vision

School of Informatics UG4/MSc - 2012/13

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Research Interests:

3D computer vision/video analysis

AV: 2D Coordinate Systems

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Types of Visual Sensing



1. RGB:



2. Greyscale:

Problem of Vision - complexity





Human Vision:

- Builtin 3D stereo & video
- Excellent visual reasoning
- Not well understood





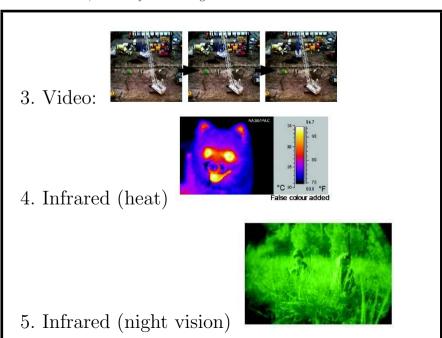
Computer Vision:

- Hard to get quality 3D
- Noise (environment, sensor)
- Limited, static viewpoints
- Low relative resolution
- Well understood, limited algorithms

AV: 2D Coordinate Systems

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6. 3D capture (static)



7. 3D capture (video)

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Review of 2D coordinate geometry

- 1. Object and Scene Coordinate Systems
- 2. Coordinate System Transformations
- 3. Homogeneous Coordinates I
- 4. Multiple Reference Frame Transformations
- 5. Simple 2D Rigid Part Modeling

AV: Six Visual Systems

- 1. Orthographically viewed rigid 2D objects
- 2. Orthographically viewed non-rigid 2D objects
- 3. Video change detection & tracking
- 4. Video: human behaviour analysis
- 5. Recognising 3D objects from range data
- 6. Recognising 3D objects from stereo data

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Object and Scene Coordinate Systems

Issues:

- + Want to describe object features independently of the object's position.
- + Want to specify object position and orientation within scene



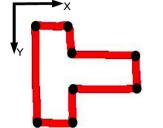
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Why? Generic Model Vs. Specific Position





Generic:

Specific:

Object geometric Scene position in

model, aligned

pixels, not aligned

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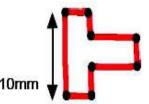
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Object and Scene Coordinate Systems III

(c,r) in image (eg. in pixels) relates to (x,y) in scene (eg. in mm) using column, row scale factors ρ_c, ρ_r : $(x, y) = (\rho_c c, \rho_r r)$

178 pixels

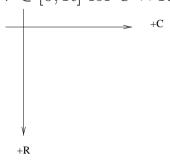




Object and Scene Coordinate Systems II

Solution: Use separate object and scene coordinate systems and link by reference frame transformations

Use image coordinate system $(c, r), c \in [0, C]$, $r \in [0, R]$ for $C \times R$ image (for convenience)



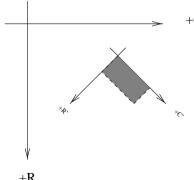
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Object and Scene Coordinate Systems IV

Use separate coordinate systems for object and scene

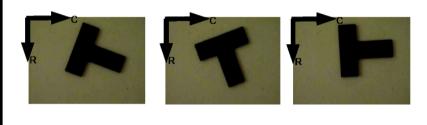


Also - image and camera coordinate systems

Coordinate System Transformations I

Placement of object relative to scene requires a coordinate system transformation

In 2D, need 1 rotation angle θ and $\vec{t} = (t_c, t_r)'$ translation (' is for transposing a row vector to a column vector and *vice versa*)



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Coordinate System Transformations III

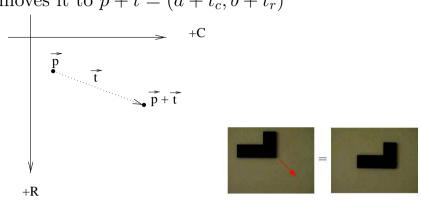
If θ is the rotation angle, let

$$R = \begin{bmatrix} cos(\theta) & -sin(\theta) \\ sin(\theta) & cos(\theta) \end{bmatrix}$$

Sometime see $sin(\theta)$ and $-sin(\theta)$ swapped. A matter of convention about direction of rotation.

Coordinate System Transformations II

 $\vec{p} = (a, b)'$ is a point in the 2D coord system Translation of point $\vec{p} = (a, b)'$ by $\vec{t} = (t_c, t_r)'$ moves it to $\vec{p} + \vec{t} = (a + t_c, b + t_r)'$



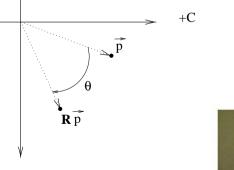
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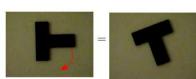
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Coordinate System Transformations IV

Rotation of point $\vec{p} = (a, b)'$ by R moves it to $R\vec{p} = (a \cdot cos(\theta) - b \cdot sin(\theta), a \cdot sin(\theta) + b \cdot cos(\theta))'$

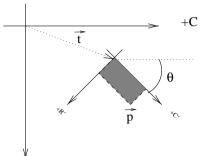




 θ positive is clockwise rotation (other definition common)

Complete Transformations

Rotation & Translations: $R\vec{p} + \vec{t}$



If the object local coordinate system starts at (0,0), then the rotation & translation specify its position

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Homogeneous Coordinates I

Instead of 2 operations to implement the transformation, often only one operation based on homogeneous coordinates (more advanced form in later lectures)

- 1) Extend points $\vec{p} = (a, b)'$ to $\vec{P} = (a, b, 1)'$
- 2) Extend vectors $\vec{d} = (u, v)'$ to $\vec{D} = (u, v, 0)'$
- 3) Combine rotation and translation into one 3×3 matrix

$$T = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & t_c \\ \sin(\theta) & \cos(\theta) & t_r \\ 0 & 0 & 1 \end{bmatrix}$$

Full transformation of \vec{p} is now $T\vec{P}$

Midlecture Problem

What is the position resulting from rotating the point $\vec{x} = (10, 20)'$ by $\frac{\pi}{2}$ and translating the result by $\vec{t} = (-10, 30)'$?

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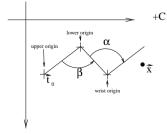
Multiple Transformations

Given 2 joint robot arm whose joint angles are α and β

 $\mathcal{T}_w(\alpha)$ is the wrist joint position relative to the lower arm

 $T_l(\beta)$ is the lower arm position relative to the upper arm

The arm is at position T_0



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Multiple Transformations II

Then, a wrist coordinate point \vec{x} at the tip of the robot is at

$$\vec{y} = T_0 T_l(\beta) T_w(\alpha) \vec{x}$$

Can also easily invert positions:

$$\vec{x} = (T_w(\alpha))^{-1} (T_l(\beta))^{-1} (T_0)^{-1} \vec{y}$$

is the wrist coordinates of scene point \vec{y}

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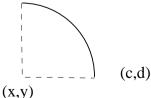
Polycurve / Polyline Modeling

Set of vertices connected by line / curve segments

Line segment: (a,b) -L- (c,d)

Arc segment: (a,b) -arc(x,y) - (c,d)

(a,b)



Arbitrary position in local object-centered coordinate system

Geometric Shape Model

Here: rigid, piecewise linear / circular boundary segments

Options:

- Region representation: pixel list, quadtree
- Boundary representation
 - Curve
 - * Set of boundary segments
 - * Pixel list / chain code (incremental pixel list)
 - Vertices

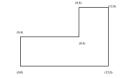
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Example Models

(0,0)-L-(12,0)-L-(12,8)-L-(8,8)-L-(8,4)-L-(0,4)-L-(0,0)

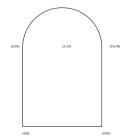








(0,0) -L- (10,0) -L- (10,10) -arc(5,10)- (0,10) -L- (0,0)



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What We Have Learned

- 1. Review of Coordinate Systems Transformations
- 2. Introduction to Homogeneous Coordinates
- 3. Simple 2D Rigid Part Modeling

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