# Large vocabulary ASR

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#### Automatic Speech Recognition – ASR Lecture 9 10 February 2020

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### HMM Speech Recognition



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# The Search Problem in ASR

Find the most probable word sequence \$\hat{W} = w\_1, w\_2, \ldots, w\_M\$ given the acoustic observations \$\mathbf{X} = \mathbf{x}\_1, \mathbf{x}\_2, \ldots, \mathbf{x}\_T\$:

$$\hat{W} = \arg \max_{W} P(W|\mathbf{X})$$
  
=  $\arg \max_{W} \underbrace{p(\mathbf{X} \mid W)}_{\text{acoustic model language model}} \underbrace{P(W)}_{\text{language model}}$ 

- Use pronuniciation knowledge to construct HMMs for all possible words
- Finding the most probable state sequence allows us to recover the most probable word sequence
- Viterbi decoding is an efficient way of finding the most probable state sequence, but even this is infeasible as the vocabulary gets very large or when a stronger language model is used

# Recap: the word HMM



HMM naturally generates an alignment between hidden states and observation sequence

# Viterbi algorithm for state alignment



Viterbi algorithm finds the best path through the trellis – giving the highest p(X, Q).

# Simplified version with one state per phone



## Isolated word recognition



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# Viterbi algorithm: isolated word recognition



- Even worse when recognising connected words...
- The number of words in the utterance is not known
- Word boundaries are not known: any of the V words may potentially start at each frame.

### Connected word recognition



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# Viterbi algorithm: connected word recognition



Add transitions between all word-final and word-initial states

### Connected word recognition



Viterbi decoding finds the best word sequence

BUT: have to consider  $|V|^2$  inter-word transitions at every time step

#### Connected word recognition



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- So far we've estimated HMM transition probabilities from audio data, as part of the acoustic model
- Transitions between words rightarrow use a language model
- *n*-gram language model:

$$p(w_i|h_i) = p(w_i|w_{i-n}, \ldots, w_{i-1})$$

• Integrate the language model directly in the Viterbi search

#### Incorporating a bigram language model



#### Incorporating a bigram language model



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#### Incorporating a trigram language model



Need to duplicate HMM states to incorporate extended word history

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### Computational Issues

- Viterbi decoding performs an exact search in an efficient manner
- But exact search is not possible for large vocabulary tasks
  - Long-span language models and the use of cross-word triphones greatly increase the size of the search space
- Solutions:
  - Beam search (prune low probability hypotheses)
  - Tree structured lexicons
  - Language model look-ahead
  - Dynamic search structures
  - Multipass search (→ two-stage decoding)
  - Best-first search ( $\rightarrow$  stack decoding / A<sup>\*</sup> search)

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- An alternative approach: Weighted Finite State Transducers (WFST)

# Pruning



During Viterbi decoding, don't propagate tokens whose probability falls a certain amount below the current best path

Result is only an approximation to the best path

#### Tree-structured lexicon



Figure adapted from Ortmans & Ney, "The time-conditioned approach in dynamic programming search for LVCSR"

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#### Tree-structured lexicon



Reduces the number of state transition computations

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For clarity, not all the connections are shown

- Aim to make pruning more efficient
- In tree-structured decoding, look ahead to find out the best LM score for any words further down the tree
- This information can be pre-computed and stored at each node in the tree
- States in the tree are pruned early if we know that none of the possibilities will receive good enough probabilities from the LM.

- Weighted finite state automaton that transduces an input sequence to an output sequence (Mohri et al 2008)
- States connected by transitions. Each transition has
  - input label
  - output label
  - weight
- Weights use the *log semi-ring* or *tropical semi-ring* with operations that correspond to multiplication and addition of probabilities
- There is a single start state. Any state can optionally be a final state (with a weight)
- Used by Kaldi

### Weighted Finite State Acceptors





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## Weighted Finite State Transducers

Acceptor



Transducer



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### Weighted Finite State Transducers



Transducer



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#### The HMM as a WFST





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# Composition Combine transducers $T_1$ and $T_2$ into a single transducer acting as if the output of $T_1$ was passed into $T_2$ .

Determinisation Ensure that each state has no more than a single output transition for a given input label

Minimisation transforms a transducer to an equivalent transducer with the fewest possible states and transitions

# Applying WFSTs to speech recognition

• Represent the following components as WFSTs

	transducer	input sequence	output sequence
G	word-level grammar	words	words
L	pronunciation lexicon	phones	words
С	context-dependency	CD phones	phones
Н	HMM	HMM states	CD phones

- Composing *L* and *G* results in a transducer *L*  $\circ$  *G* that maps a phone sequence to a word sequence
- $H \circ C \circ L \circ G$  results in a transducer that maps from HMM states to a word sequence

- Ortmanns and Ney (2000). "The time-conditioned approach in dynamic programming search for LVCSR". In IEEE Transactions on Speech and Audio Processing, Vol. 8, No. 6.
- Mohri et al (2008). "Speech recognition with weighted finite-state transducers." In Springer Handbook of Speech Processing, pp. 559-584. Springer.

http://www.cs.nyu.edu/~mohri/pub/hbka.pdf

• WFSTs in Kaldi. http://danielpovey.com/files/Lecture4.pdf