

Discriminative Training of GMM-based systems

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 - the model is correct (i.e. the true data source is an HMM)
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- Discriminative training:
 - Focus on learning *boundaries* between classes
 - Consider incorrect word sequences as well as correct word sequences
 - This is related to direct optimisation of the posterior probability of the words given the acoustics $P(W | \mathbf{X})$

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Discriminative training criteria

- **Minimum classification error (MCE)**
 - Correct parameters if misrecognition occurs
 - Discriminant function is the difference between the log likelihood of the correct sentence and the average likelihood of incorrect competitors
 - Used mainly for small vocabularies
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- **Minimum Bayes Risk (MBR)**
 - Optimise the word error rate rather than a likelihood ratio
 - Use the string edit distance between competing and reference utterances
 - Minimum phone error (MPE) training

Maximum likelihood estimation (MLE)

- Maximum likelihood estimation (MLE) sets the parameters so as to maximize an objective function F_{MLE} :

$$F_{\text{MLE}} = \sum_{u=1}^U \log P_{\lambda}(\mathbf{X}_u | M(W_u))$$

for training utterances $\mathbf{X}_1 \dots \mathbf{X}_U$ where W_u is the word sequence given by the transcription of the u th utterance, $M(W_u)$ is the corresponding HMM, and λ is the set of HMM parameters

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- This objective function can be maximised by the EM algorithm (Forward-Backward algorithm when applied to HMMs)

MLE — Updating the mean

- Update equation for the mean vector $\boldsymbol{\mu}^{jm}$ for Gaussian component m of GMM associated with state s_j is:

$$\hat{\boldsymbol{\mu}}^{jm} = \frac{\sum_{u=1}^U \sum_{t=1}^T \gamma_t^u(s_j, m) \mathbf{x}_t^u}{\sum_{u=1}^U \sum_{t=1}^T \gamma_t^u(s_j, m)}$$

where $\gamma_t^u(s_j, m)$ is the probability of the model occupying mixture component m of state j at time t given training sentence \mathbf{X}_u .

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- Some extra notation:

$$\Theta_{jm}^u(M) = \sum_{t=1}^T \gamma_t^u(s_j, m) \mathbf{x}_t^u \quad \Gamma_{jm}^u(M) = \sum_{t=1}^T \gamma_t^u(s_j, m)$$

$$\hat{\mu}^{jm} = \frac{\sum_{u=1}^U \Theta_{jm}^u(M(W_u))}{\sum_{u=1}^U \Gamma_{jm}^u(M(W_u))}$$

Maximum mutual information estimation

- Maximum mutual information estimation (MMIE) aims to directly maximise the posterior probability (sometimes called conditional maximum likelihood). Using the same notation as before, with $P(w)$ representing the language model probability of word sequence w :

$$\begin{aligned} F_{\text{MMIE}} &= \sum_{u=1}^U \log P_{\lambda}(M(W_u) | \mathbf{X}_u) \\ &= \sum_{u=1}^U \log \frac{P_{\lambda}(\mathbf{X}_u | M(W_u))P(W_u)}{\sum_{w'} P_{\lambda}(\mathbf{X}_u | M(w'))P(w')} \end{aligned}$$

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Maximum mutual information estimation

- **Numerator:** $P_\lambda(\mathbf{X}_u | M(W_u))P(W_u)$
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- **Denominator:** $\sum_{w'} P_\lambda(\mathbf{X}_u | M(w'_u))P(w'_u)$
the total likelihood of the data given all possible word sequences — obtained by summing over all possible word sequences estimated by the full acoustic and language models in recognition (M_{den}):

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- The objective function F_{MMIE} is optimised by making the correct word sequence likely (maximise the numerator), and all other word sequences unlikely (minimise the denominator)

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- No EM-based optimization approach for F_{MMIE}
- Gradient-based approaches are straightforward but slow
- Approximation: Extended Baum-Welch (EBW) algorithm provides update formulae similar to forward-backward recursions used in MLE.
- Extended Baum-Welch — Updating the mean:

$$\hat{\mu}^{jm} = \frac{\sum_{u=1}^U \left[\Theta_{jm}^u(M_{\text{num}}) - \Theta_{jm}^u(M_{\text{den}}) \right] + D\mu^{jm}}{\sum_{u=1}^U \left[\Gamma_{jm}^u(M_{\text{num}}) - \Gamma_{jm}^u(M_{\text{den}}) \right] + D}$$

- Can interpret D as a weight between old and new estimates; in practice D estimated for each Gaussian to ensure variance updates are positive

- Computing $\Theta_{jm}^u(M_{\text{den}})$ involves summing over all possible word sequences — estimate by generating lattices, and summing over all words in the lattice
- In practice also compute numerator statistics using lattices (useful for summing multiple pronunciations)
- Generate numerator and denominator lattices for every training utterance
- Denominator lattice uses recognition setup (with a weaker language model)
- Each word in the lattice is decoded to give a phone segmentation, and forward-backward is then used to compute the state occupation probabilities
- Lattices not usually re-computed during training

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- $A(W, W_u)$ is the phone transcription accuracy of the sentence W given the reference W_u
- F_{MPE} is a weighted average over all possible sentences w of the raw phone accuracy
- Although MPE optimizes a phone accuracy level, it does so in the context of a word-level system: it is optimized by finding probable sentences with low phone error rates

Example: meeting speech recognition

WER for HMM/GMM system

System	Training criterion	WER/%
Baseline	ML	28.7
SAT	ML	27.6
SAT	MPE	24.5

Sequence training of hybrid HMM/DNN systems

- Can train HMM/NN systems using a MMI-type objective function (e.g. Bridle and Dodd, 1991)
- Forward- and back-propagation equations are structurally similar to forward and backward recursions in HMM training
- Was not used in practice, for another 20 years...
- Now used for DNN systems (e.g. Vesely et al, 2013)
- The tricky parts are in the optimisation and in the use of lattices to compute the denominator term...

- Discriminative methods optimize a criterion other than maximum likelihood (eg more directly related to the error rate)
- But, we still want to optimize all parameters according to a consistent criterion
 - MMI — directly optimise the posterior probability of the word sequence given the data
 - MPE — scale the posterior word sequence probability by an estimate of the phone error rate
- Discriminative training has a number of technical issues relating to smoothing the parameter updates

- Sec 27.3.1 of: S Young (2008). [HMMs and Related Speech Recognition Technologies](#), in *Springer Handbook of Speech Processing*, J Benesty, MM Sondhi and Y Huang (eds), chapter 27, 539–557.
- NN sequence training:
 - Bridle & Dodd (1991), [An Alphanet approach to optimising input transformations for continuous speech recognition](#), Proc IEEE ICASSP
 - Vesely et al (2013), [Sequence-discriminative training of deep neural networks](#), Proc Interspeech