ANLP 2016

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Tutorial Exercise Set 1 (for tutorial groups in week 2)

This week’s tutorial sheet is primarily aimed at students who have less background in probability theory, to make sure that you have gone through the reading material and are learning to solve problems on your own. If this material is entirely new to you, don’t expect that you will necessarily have absorbed all of it by now (this will take some time), but you should definitely try to work through these exercises and come with specific questions if you have trouble.

Priority will be given in tutorial sessions to going over exercises 1-3 unless all students in the group are happy to skip them. However, we will try to leave some time to discuss the final two problems as well.

Exercise 1.
Suppose we have a group of first- and second-year students, each of whom comes from either the UK, Germany, or China. We choose a student uniformly at random from this group. Let $F = \text{“the student is in first year”}$, $U = \text{“the student is from the UK”}$, $C = \text{the student is from China}$, and $G = \text{“the student is from Germany”}$. For this group of students, $P(U) = 0.6$, $P(G) = 0.3$, $P(C) = 0.1$, $P(F | U) = 0.7$, $P(F | G) = 0.5$, $P(F | C) = 0.6$.

a) What is the probability that we’ve chosen a first-year student?

b) What is the probability that the student is from the UK if it is a first-year student?

Exercise 2.
(Exercise 4.6 from the Basic Probability Theory tutorial)
Suppose I want to choose a two-word name for a rock band via a random process. The first word will be chosen with uniform probability from the set \{yellow, purple, sordid, twisted\}. The second word will be either quake, with probability 1/3, or revolution, with probability 2/3.

a) What’s the sample space for this experiment? How many outcomes are in it?

b) If I choose the first and second words independently, what is the probability that my rock band will be called yellow revolution?

c) Instead, I decide to condition the second word on the first. If the first word is a color, then I’ll pick quake as the second word with probability 1/6. Assuming I still want the overall probability of a name with quake to be 1/3, what is the probability of quake if the first word is not a color? (Hint: use a joint probability table to help you answer this question. You may not need to fill in the entire table.)

Exercise 3.
Suppose I decide to probabilistically generate a “word”, which can contain only characters in the set \{a, b, c, d, e\}. To generate the word, I start by generating the character a. Then, with probability $q$, I generate a single b and stop, otherwise I choose one of the other four characters (a, c, d, e) uniformly at random and keep going. I continue this process, always either generating a single b with probability $q$ and stopping, or choosing one of the other four characters uniformly at random and continuing.

a) What are the possible words I might generate using this process? Draw an FSA that accepts all and only these words.
b) If $L$ is a random variable representing the length of a word, give an equation for $P(L = n)$.

c) If $q = 0.3$, what is the probability that my generated word has 4 characters? What is the probability of generating the word aaab?

d) If $q = 0.3$, what is the probability of generating the word aaab given that I generate a 4-character word?

**Exercise 4.**
In lecture 3, there is an example of an FSA for English derivational morphology that looks like this and generates words like *wordy, wordification*, etc. (assuming that spelling changes are fixed up by another FSA that applies afterward).

**Exercise 5.**
The transducer from J&M Fig 3.17 is reproduced below. (‘other’ = none of \{z,s,x,^,\#,\epsilon\}).

a) What sequence of states would we go through to create the correct plural form for *axle^s#*? For *lass^s#*?

b) Can you think of any words that cause the transducer to go from state $q_2$ to $q_5$ and then continue on to an accepting (end) state? If not, can you at least say what properties would such a word need to have?