## Accelerated Natural Language Processing 2016

# Lecture 17: Words in PCFGs, collocations and mutual information

Henry S. Thompson 7 November 2016

#### **1. Another big problem with simple PCFGs**

For a given structural ambiguity, say PP attachment

• A simple PCFG always makes the same choice

Consider the two alternative parses we would get from the Treebank grammar for *Mr Vinken is chairman of Elsevier*:





### 2. PCFG example, cont'd

How did we get those two analyses?

• Here's a top-down parse trace using Penn Treebank rules:

 $S \rightarrow NP-SBJ \vee P$   $NP-SBJ \rightarrow NNP NNP$   $NNP \rightarrow Mr$   $NNP \rightarrow Vinken$   $p^{5} VP \rightarrow VBZ NP-PRD$   $VBZ \rightarrow is$   $p^{4} NP-PRD \rightarrow NP PP$   $NP \rightarrow NN$   $p^{1} NN \rightarrow chairman$   $p^{3} PP \rightarrow IN NP$   $IN \rightarrow of$   $NP \rightarrow NNP$  $p^{2} NNP \rightarrow Elsevier$   $S \rightarrow NP-SBJ \vee P$   $NP-SBJ \rightarrow NNP NNP$   $NNP \rightarrow Mr$   $NNP \rightarrow Vinken$   $p^{7} VP \rightarrow VBZ NP-PRD PP$   $VBZ \rightarrow is$   $p^{6} NP-PRD \rightarrow NP$   $NP \rightarrow NN$   $p^{1} NN \rightarrow chairman$   $p^{3} PP \rightarrow IN NP$   $IN \rightarrow of$   $NP \rightarrow NNP$  $p^{2} NNP \rightarrow Elsevier$ 

### PP attached to NP-PRD

PP attached to VP

So the only difference is the probabilities of the rules highlighted in red

• p4 and p5 versus p6 and p7

And those will *always* give the same answer

- Depending on the relative magnitude of p4\*p5 vs p6\*p7
- Regardless of what the individual words and their probabilities are
- Because whatever the words
- p1, p2 and p3 are the *same* for both parses
- Compare, for instance, chairman at the moment with chairman for life

We really need to pay attention to the probability of those words being tightly or loosely connected

### 3. Paying attention to words

Improving our approach to probabilistic grammar requires paying more attention to individual *words* 

• Let's explore how we might do that a bit more

Back to bigrams, but in a little more detail

• It turns out that not all bigrams are created equal

Here are the top 10 bigrams from Herman Melville's famous American novel *Moby Dick*:

```
of the (1879)
in the (1182)
to the (731)
from the (440)
the whale (407)
of his (373)
and the (370)
on the (359)
of a (334)
at the (330)
to be (329)
```

Aside from *the whale*, these are all made up of very high-frequency closed-class items

The highest bigram of open-class items doesn't come until position 27: *sperm whale*, with frequency 182

None-the-less if feels as if there's something particularly interesting about that one. . .

#### 4. Collocations

"You shall know a word by the company it keeps" (J. R. Firth)

One of the things we evidently know about our language is what words go with what

- strong tea, not powerful tea
- powerful enemies, not strong enemies
- tall flagpole, not long flagpole
- *long railing*, not *tall railing*

Choosing the right word from among a set of synonyms is a common problem for secondlanguage learners

- *un froid vive* is not (per Microsoft translate) *a bright cold*, but rather *a piercing cold*
- Likewise универсальный магазин is not universal store but department store

Or consider the old (linguists') joke:

• If a maternity dress is what a woman wears when she is pregnant, what is a paternity suit?

#### 5. What measure to find collocations?

The name for an 'interesting' pair is **collocation** 

How can we separate the interesting pairs from the dull ones?

We could try just throwing out the 'little words'

- Typically called 'stop words', see e.g. corpus.stopwords.word('english') in NLTK
- But that still isn't quite getting at what we want: *sperm whale* (182)

```
white whale (106)
moby dick (84)
old man (81)
captain ahab (62)
right whale (57)
mast head (49)
mast heads (37)
ye see (35)
whale ship (34)
```

Some of these feel special (*right whale*, *moby dick*), but others (*old man* in particular) just seem ordinary

- They are encoding transparent: we would expect their meaning to be formed from those words
- They're not 'terms' in the sense of 'terminology'

# 6. Normalising by expection: mutual information

What we want is some way of factoring in frequency more generally

- To take care of more than just some pre-determined list of stop words
- and to downgrade old man and similar cases

Conditional and joint probability are the answer

- Remember that if two events are independent, the conditional probability is the same as the unconditional
  - **P(Y|X)** is just **P(Y)**
- so the joint probability is just the product of the two event probabilities
  - **P(X,Y)** is defined as **P(X)P(Y|X)**
  - So if X and Y are independent, that's P(X)P(Y)

One way of getting at our intuition might be to say we're looking for cases where the two probabilities are *not* independent

Now the bigram frequency gives us an MLE of the joint probability directly

So the *ratio* of that probability, to what it would be if they were independent, would be illuminating:

Pointwise mutual information  $\log_2\left(\frac{P(X, Y)}{P(X)P(Y)}\right)$ 

Terminology note: Strictly speaking we should distinguish between **pointwise mutual information** and **mutual information** as such. The latter is a measure over *distributions*, as opposed to individuals.

 But below, and often in the literature, we will use **mutual information** for the measure defined above, when it is clear from context that it's individuals we're concerned with.

### 7. Mutual information example

Let's compare the most frequent bigram (*of the*) with the first interesting one we saw, *sperm whale* 

```
>>> f[('of', 'the')]
1879
>>> u['of']
6609
>>> u['the']
14431
>>> 1879.0/218360
0.0086050558710386513
>>> (6609.0 * 14431)/(218361*218361)
0.0020002396390988637
>>> log((1879.0/218360)/((6609.0 * 14431)/(218361*218361)),2)
2.105011706733956
>>> f[('sperm','whale')]
182
>>> u['sperm']
244
>>> u['whale']
1226
>>> 182.0/218361
0.00083348216943501818
>>> (244.0*1226) / (218361*218361)
6.2737924534150313e-06
>>> log((182.0/218361)/((244.0*1226)/(218361*218361)),2)
7.0536697225202696
```

Simply put, the mutual information between *sperm* and *whale* is 5 binary orders of magnitude greater than that between *of* and *the* 

Why are we using log base 2?

· Because we traditionally measure information in bits

#### 8. Collocations and machine translation

We can use the same approach to build a translation lexicon

Instead of bigrams within a single text

- Co-occurence in aligned units of a bilingual text
- We treat sentences as sets of words
- And construct a distribution of pairs of words, one from each set for each pair of sentences
- Here are the top 30 pairs from a corpus of 4600 sentence pairs from the European Parliament debates, French and English versions:

```
[((u'commission', u'commission'), 113),
((u'rapport', u'report'), 84),
 ((u'régions', u'regions'), 71),
 ((u'parlement', u'parliament'), 66),
((u'politique', u'policy'), 62),
((u'voudrais', u'like'), 58),
((u'président', u'president'), 57),
 ((u'fonds', u'funds'), 52),
 ((u'monsieur', u'president'), 50),
 ((u'union', u'union'), 48),
 ((u'états', u'states'), 46),
 ((u'membres', u'member'), 46),
((u'états', u'member'), 46),
 ((u'développement', u'development'), 44),
 ((u'membres', u'states'), 43),
 ((u'également', u'also'), 42),
 ((u'structurels', u'structural'), 41),
((u'fonds', u'structural'), 41),
((u'structurels', u'funds'), 40),
((u'cohésion', u'cohesion'), 38),
((u'voudrais', u'would'), 38),
 ((u'européenne', u'european'), 37),
((u'orientations', u'guidelines'), 37),
 ((u'commission', u'would'), 36),
((u'madame', u'president'), 34),
((u'groupe', u'group'), 33),
((u'commissaire', u'commissioner'), 33),
 ((u'présidente', u'president'), 32),
 ((u'sécurité', u'safety'), 32),
 ((u'transports', u'transport'), 30)]
```

#### Pretty good

And would be better if we had done monolingual collocation detection first!

#### 9. Words, heads and grammar

We mentioned the idea of the **head** of a constituent in earlier lectures

- Maybe organising our grammar in a completely different way would help with the attachment problem
- Because something like mutual information between heads might be just what we need

Approaches to grammar which focus on heads are called **dependency** grammars

The standard form of diagram shows where this name comes from:

Mr Vinken is chairman of Elsevier

(Green for the preferred attachment, red for the less likely one)

### 10. Dependency grammar

Dependency grammars don't have rules in the way that a CFG does

- But they do have categories
- · And category-specific ways of identifying heads

A given approach to dependency grammar will also involve an inventory of relations

- Not just 'depends'
- But e.g. subj, obj, nmod, pmod:



Dependency graphs are not required to avoid crossings

- So they can directly represent long-distance dependencies
- And work well for case-marked, free-constituent-order languages

#### 11. Lexicalised PCFG

It's possible to add some of the benefits of dependency grammar to PCFGs

• By decorating categories in the tree with their head



We can't do statistics directly on these augmented categories

• The space is too large to give anything other than very small numbers

But a range of techniques have been developed in the last few years to work around this

• Sharon will come back to this in a few weeks

#### 12. Putting words first: Categorial grammar

Categorial grammar represents a different approach to putting words at the centre of things

• Albeit one which still gives linear order a key role

In the simplest form of CG, all we need is a lexicon like this

```
N: duck, cat, ...
NP/N: the, a, ...
S\NP: ran, slept, ...
(S\NP)/NP: saw, liked
```

Where we read e.g. NP/N as the category for things which combine with an N to their *right* to produce an NP

- And  $s \in \mathbb{NP}$  as the category for things which combine with an  $\mathbb{NP}$  to their left to produce an s

In the obvious way this gives us the following derivation for the cat saw a duck:



The arrows next to the derivation steps identify which of the (meta-)rules was used for that step:

#### forward combination (>)

 $X/Y Y \rightarrow X$ 

#### backward combination (<)</pre>

 $X X Y \rightarrow X$ 

These are the only two rules, or rule schemata, needed for the simplest categorial grammars