Applied Databases

Lecture 12
*Online Pattern Matching on Strings*

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*University of Edinburgh - March 2nd, 2017*
Outline

First → some comments wrt Assignment 1

1. Naive Method
2. Automaton Method
3. Knuth-Morris-Pratt Algorithm
4. Boyer-Moore Algorithm
Assignment 1

Automation works correctly and independently of VM: 1 Point
Program compiles and produces some non-empty csv-files: 4 Points
Program successfully loads some data into the database: 1 Point
Data loaded into database is correct, given the DB design: 2 Point
drop.sql: Works correctly without error: 0.5 Points
SQL-scripts have no (or only minor) syntax errors: 0.5 Points
Database does not use any NULL-Values: 2 Points
Long descriptions are correctly truncated: 1 Point
Duplicate entries are correctly removed in the csv-files: 1 Point
All Queries correct: 3.5 Points

16.5 Points

Theoretical Part (schema design & normal forms): 3.5 Points

We are still marking these.
Marks will be finalized by tomorrow (Friday) evening.
Assignment 1

Marks so far (out of 16.5 Points) – #submissions = 51
Assignment 1

[Bar chart showing the distribution of different categories such as All Queries, Duplicates removed, Correct Truncation, No nulls, No sql error, Loads correctly, Loads something, Compiles and Creates csv, and Automation, with color codes for different percentages.]
Marking of Assignment 1

→ relational schema design (3.5 points)
  
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ item-category: many-to-many relationship

table has_category(item_id, category)

→ primary key (item_id, category)
→ consequence: there cannot be duplicates!
→ original XML has such duplicates!

must be detected and eliminated by your program (not through mySQL)
Marking of Assignment 1

→ relational schema design (3.5 points)
  
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ item-category: many-to-many relationship

<table>
<thead>
<tr>
<th>Item ID</th>
<th>Name</th>
<th>Category</th>
</tr>
</thead>
<tbody>
<tr>
<td>1310018094</td>
<td>2 lanzar 10&quot; DC subs 1000 watt subwoofers</td>
<td>Consumer Electronics, Car Audio &amp; Electronics, Subwoofers, Subwoofers, 10 Inch</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$175.00</td>
</tr>
</tbody>
</table>

has exactly four categories, not five!
Bid Table

→ relational schema design (3.5 points)
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ bid table
  – item_id
  – bidder_id
  – time
  – amount

→ keys of this table?
Bid Table

→ relational schema design (3.5 points)
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ bid table
  – item_id
  – bidder_id
  – time
  – amount

not keys:

1) (item_id, bidder_id) – bidder can bid multiple times for same item!
Bid Table

→ relational schema design (3.5 points)
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ bid table
  – item_id
  – bidder_id
  – time
  – amount

not keys:

1) (item_id, bidder_id) – bidder can bid multiple times for same item!
2) (bidder_id, time) – bidder can make multiple bids at same time!
   (e.g., multiple times logged in, bidding per software, etc.)
Bid Table

→ relational schema design (3.5 points)
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ bid table
  – item_id
  – bidder_id
  – time
  – amount

→ is this a key?

(item_id, bidder_id, time)
Bid Table

→ relational schema design (3.5 points)
  
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ bid table
  
  – item_id
  – bidder_id
  – time
  – amount

→ is this a key?

(item_id, bidder_id, time)

NO! → It is not minimal
Bid Table

→ relational schema design (3.5 points)
  
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ bid table
  
  – item_id
  – bidder_id
  – time
  – amount

→ is this a key?

\( (\text{item}_\text{id}, \text{bidder}_\text{id}, \text{time}) \)

NO! → It is not minimal

Correct keys:

→ \( (\text{item}_\text{id}, \text{time}) \)
Bid Table

→ relational schema design (3.5 points)
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ bid table
  – item_id
  – bidder_id
  – time
  – amount

→ is this a key?

(defn item_id, bidder_id, time)

NO! → It is not minimal

Correct keys:

→ (item_id, time)

Any other keys?
Bid Table

→ relational schema design (3.5 points)
  – NULL or pseudo-NULLs (0.5 points)
  – optionals of DTD correctly implemented (0.5 points)
  – correct Primary Key for each table (0.25 = one error, 0.5 = two errors)

→ bid table
  – item_id
  – bidder_id
  – time
  – amount

→ is this a key?

(items_id, bidder_id, time)

NO! → It is not minimal

Correct keys:

→ (item_id, time)
→ (item_id, amount)
Marking of Assignment 1

→ relational schema design (3.5 points)

- NULL or pseudo-NULLs (0.5 points)
- optionals of DTD correctly implemented (0.5 points)
- correct Primary Key for each table (0.25 = one error, 0.5 = two errors)
- correct Functional Dependencies (0.5 points)
- 4NF (0.5 points)
  [ either you claim 4NF/BCNF but it isn’t, or vice versa ]

<= 2.5 penalty points

If you wrote **something** for this part, you obtain 1 Point by default! :-}
Marking of Assignment 1

Queries

E.g., Number 3:

SELECT COUNT(y.item_id) FROM
  (SELECT item_id, COUNT(item_id) as count
   FROM has_category GROUP BY item_id) y
WHERE y.count=4;

→ assumes duplicate-free has_category table

→ if has_category has duplicates, how to write the query?
Answers to Queries

Queries

1) Find the number of users in the database.  
   **13422**
2) Find the number of items in "New York".  
   **103**
3) Find the number of auctions belonging to exactly four categories.  
   **8365**
4) Find the ID(s) of current (unsold) auction(s) with the highest bid.  
   **1046740686**
5) Find the number of sellers whose rating is higher than 1000.  
   **3130**
6) Find the number of users who are both sellers and bidders.  
   **6717**
7) Find the number of categories that include at least one item with a bid of more than $100.  
   **150**
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2. (A) Schemas. \[Bookwork: 4 \times 1.5 = 6 \text{ marks}\]

(1) A functional dependency means that some columns determine the values of other columns. Consider a table with columns Street, City, and ZipCode. List all the functional dependencies for this table. (this is for the US, where a ZipCode does not determine a street).

(2) Explain what is a superkey, what is a key, and what is a primary key.

(3) List all keys for a table of biddings of an online bidding system (where the same bidder can make multiple bids at a time) with column names ItemID, BidderID, Time, and Amount.

(4) Explain what a multi-valued dependency is, and give an example of one (that is not a functional dependency).
Full-Text Search

- tokenize natural language documents
- build inverted files

- execute keyword-queries over inverted files
- rank results according to TF-IDF-based scoring
Full-Text Search

→ tokenize natural language documents
→ build inverted files
→ execute keyword-queries over inverted files
→ rank results according to TF-IDF-based scoring

Limits of this approach:
→ search over DNA sequences
→ huge sequences over C, T, G, A (ca. 3.2 billion)
→ no spaces, no tokens....
Pattern Matching on Strings

→ search over DNA sequences
→ huge sequence over C, T, G A (ca. 3.2 billion)
→ no spaces, no tokens....

Given
– a long string \(T\) (text)  
– a short string \(P\) (pattern)

Problem 1: find all occurrences of \(P\) in \(T\)
Problem 2: count #occurrence of \(P\) in \(T\)
Pattern Matching on Strings

→ search over DNA sequences
→ huge sequence over C, T, G A (ca. 3.2 billion)
→ no spaces, no tokens....

Given
– a long string $T$ (text) [ often: over a fixed alphabet ]
– a short string $P$ (pattern)

Problem 1: find all occurrences of $P$ in $T$
Problem 2: count #occurrence of $P$ in $T$

Two versions:

→ offline = we may index $T$, before running the search
→ online = directly run search (e.g., $T$ not stored, comes in a stream)
  [ we may “index” $P$, this is called “preprocessing” ]
Pattern Matching on Strings

Highlights

**Online Search:** $O(|T|)$ time with $O(|P|)$ preprocessing

**Offline Search:** $O(|P| + \text{#occ})$ time with $O(|T|)$ preprocessing

---

Given

- a long string $T$ (text)
- a short string $P$ (pattern)

Problem 1: find all occurrences of $P$ in $T$

Problem 2: count #occurrence of $P$ in $T$

---

Two versions:

- **offline** = we may index $T$, before running the search
- **online** = directly run search (e.g., $T$ not stored, comes in a stream)
  
  [ we may “index” $P$, this is called “preprocessing” ]
Online Pattern Matching on Strings

Given
– short string P (pattern)
– long string T (text)

\[ \rightarrow \text{may preprocess P!} \]

Problem 1: find all occurrences of P in T
Problem 2: count #occurrence of P in T

1) Automaton Method
   \[ \rightarrow \text{build “match automaton A” for P and run A over T} \]

2) Knuth-Morris-Pratt Algorithm
   \[ \rightarrow \text{build jump-table for P and use it when traversing T} \]

3) Boyer-Moore Algorithm
   \[ \rightarrow \text{similar to KMP, but match } \textit{backwards} \text{ in P} \]
1. Naive Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{cccc} a & b & a & b & c \end{array}$

$T = \begin{array}{cccccccccccc} a & b & a & b & a & a & b & a & b & c & a & b & a & b & a & b & a & a & b & c \end{array}$

$\rightarrow at each position in T, try to match P$
1. Naive Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{cccccc}
    a & b & a & b & c \\
\end{array}$

$T = \begin{array}{cccccccccccccccc}
    a & b & a & b & a & a & b & a & b & c & a & b & a & b & a & b & a & a & b & c \\
    a & b & a & b & c \\
\end{array}$

$\rightarrow$ at each position in $T$, try to match $P$

$\text{Pos}=1$: mismatch ($|P|=5$ comparisons needed)
1. Naive Method

Given Pattern P, Text T, find all occurrences of P in T.

\[
P = \begin{array}{cccccc}
a & b & a & b & c \\
\end{array}
\]

\[
T = \begin{array}{cccccccccccccccc}
a & b & a & b & a & a & b & a & b & c & a & b & a & b & a & b & a & a & b & c \\
\end{array}
\]

→ at each position in T, try to match P

Pos=1: mismatch (|P|=5 comparisons needed)
Pos=2: mismatch (1)
1. Naive Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{cccccc} a & b & a & b & c \\ \end{array}$

$T = \begin{array}{ccccccccccccccccccccccc} a & b & a & b & a & a & b & b & a & b & c & a & b & a & b & a & b & a & b & a & b & a & b & c \end{array}$

$\rightarrow$ at each position in $T$, try to match $P$

Pos=1: mismatch ($|P|=5$ comparisons needed)
Pos=2: mismatch (1)
Pos=3: mismatch (4)
1. Naive Method

Given Pattern P, Text T, find all occurrences of P in T.

\[ P = \text{[a b a b c]} \]

\[ T = \text{[a b a b a a b a b a b a b a b a b a b a b]} \]

\( \Rightarrow \) at each position in T, try to match P

Pos=1: mismatch
Pos=2: mismatch
Pos=3: mismatch
....
Pos=6: match!

Result List: \[ [6] \]
1. Naive Method

Given Pattern P, Text T, find all occurrences of P in T.

\[
P = \begin{array}{cccccc}
a & b & a & b & c \\
\end{array}
\]

\[
T = \begin{array}{cccccccccccccccc}
a & b & a & b & a & a & b & a & b & c & a & b & a & b & a & b & a & a & b & c \\
a & b & a & b & c \\
\end{array}
\]

**Worst-Case Time Complexity**

\[
m := |P| \\
n := |T|
\]

Naive takes \(m(n - m + 1)\) comparisons.

Thus, \(O(mn)\) time.
1. Naive Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \text{a b a b c}$

$T = \text{a b a b a a b a b c a b a b a b a a b c a b a b c}$

**Worst-Case Time Complexity**

$m := |P|$

$n := |T|$

Naive takes $m(n - m + 1)$ comparisons.

Thus, $O(mn)$ time.

**Questions**

Best-Case Complexity?

Average-Case Complexity? (on random strings)
1. Naive Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{cccccc} a & b & a & b & c \end{array}$

$T = \begin{array}{cccccccccccccccc} a & b & a & b & a & b & a & b & c & a & b & a & b & a & b & a & b & c \\ a & b & a & b & c \end{array}$

Worst-Case Time Complexity

$m := |P|$
$n := |T|$

Naive takes $m(n - m + 1)$ comparisons.

Thus, $O(mn)$ time.

---

**Note**

*Lower Bound on average:*
$O(n \log \frac{m}{m})$

[A. C. Yao 1979]
Some Definitions

Word $v$ is a **suffix** of word $w$, if $w = uv$ for some $u$.  (or: **postfix**)
(“proper suffix”, if $u$ is non-empty)

Word $u$ is a **prefix** of $w$, if $w = uv$ for some $v$.
(“proper prefix”, if $v$ is non-empty)

Word $u$ is a **factor** of $w$, if there are $v$ and $v'$ such that $w = vuv'$
2. Automaton Method

Given Pattern P, Text T, find all occurrences of P in T.

\[ P = \text{a b a b c} \]

\[ T = \text{a b a b a a b a b c a b a b a b a a b c} \]

\[ \textit{mismatch} \]

→ “mismatch” means “not a”

→ if character set C is known,
  then for every \( c \) in \( C - \{a\} \), we have one transition \( d(0, c) = 0 \)
2. Automaton Method

Given Pattern P, Text T, find all occurrences of P in T.

\[ P = a \ b \ a \ b \ a \ c \]

\[ T = a \ b \ a \ b \ a \ a \ b \ a \ b \ c \ a \ b \ a \ b \ a \ b \ a \ a \ b \ c \]

*mismatch* means "not a and not b"
2. Automaton Method

Given Pattern P, Text T, find all occurrences of P in T.

P = \[\begin{array}{c}
\text{a} \\
\text{b} \\
\text{a} \\
\text{b} \\
\text{c}
\end{array}\]

T = \[\begin{array}{c}
\text{a} \\
\text{b} \\
\text{a} \\
\text{b} \\
\text{a} \\
\text{b} \\
\text{c} \\
\text{a} \\
\text{b} \\
\text{a} \\
\text{b} \\
\text{a} \\
\text{b} \\
\text{a} \\
\text{b} \\
\text{c}
\end{array}\]
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{c}
  \text{a} \\
  \text{b} \\
  \text{a} \\
  \text{b} \\
  \text{c}
\end{array}$

$T = \begin{array}{c}
  \text{a} \\
  \text{b} \\
  \text{a} \\
  \text{b} \\
  \text{a} \\
  \text{b} \\
  \text{a} \\
  \text{b} \\
  \text{c}
\end{array}$
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = a b a b c$

$T = a b a b a a b a b a b c a b a b a b a a b c$

Diagram:

- Start at state 0.
- Move to state 1 on 'a'.
- Move to state 2 on 'b'.
- Move to state 3 on 'a'.
- Move to state 4 on 'b'.
- Move to state 5 on 'c'.

*Mismatch* at states:
- State 1
- State 2
- State 3

*a-transition* → *where should it go???
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \text{abaabc}$

$T = \text{aababbababcabababababc}$

→ why?
→ because $aba$ is the longest suffix of $ababa$, that is a prefix of $ababa$
2. Automaton Method

Given Pattern P, Text T, find all occurrences of P in T.

P = a b a b c

T = a b a b a a a b a b c a b a b a b a a a b c

\textit{mismatch}
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \text{a b a b c}$

$T = \text{a b a b a a b a b c a b a b a b a a b c}$

→ Deterministic Finite Automaton
→ $O(|P||S|)$ size, where $S = \text{alphabet}$
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{cccc}a & b & a & b & c\end{array}$

$T = \begin{array}{cccccccccccccccccccc}a & b & a & b & a & a & b & a & b & c & a & b & a & b & a & b & a & a & b & c\end{array}$

→ Deterministic Finite Automaton
→ $O(|P||S|)$ size, where $S =$ alphabet
→ simply run it in $O(|T|)$ time to determine all occurrences of $P$ in $T$
2. Automaton Method

Given Pattern P, Text T, find all occurrences of P in T.

P = a b a b c

T = a b a b a a b a b c a b a b a b a b a b c

mismatch

0 -> mismatch
0 -> 1
1 -> a
1 -> b
2 -> a
2 -> 3
3 -> a
3 -> b
4 -> b
4 -> 5
5
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \text{a b a b c}$

$T = \text{a b a b a a b a b c a b a b a b a a b c}$

![Automaton Diagram]

$mismatch$

$mismatch$
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \text{[a b a b c]}

T = \text{[a b a b a a b a b c a b a b a b a a b c]}

\text{mismatch}

\text{mismatch}
2. Automaton Method

Given Pattern P, Text T, find all occurrences of P in T.

\[ P = \begin{array}{cccc}
  a & b & a & b & c \\
\end{array} \]

\[ T = \begin{array}{cccccccccccccccccccc}
  a & b & a & b & a & a & b & b & b & c & a & b & a & b & a & b & a & a & b & c \\
\end{array} \]
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P =$ a b a b c

$T =$ a b a b a a b a b c a b a b a b a a b c

Diagram: Automaton transitions with mismatches indicated.
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$. 

$P = \begin{array}{cccccc} a & b & a & b & c \\ \end{array}$

$T = \begin{array}{cccccccccc} a & b & a & b & a & a & b & a & b & c & a & b & a & b & a & b & a & a & b & c \\ \end{array}$
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{cccccc} a & b & a & b & c \\ \end{array}$

$T = \begin{array}{cccccccccccccccccccc} a & b & a & b & a & a & b & a & b & c & a & b & a & b & a & b & a & a & b & c \\ \end{array}$

![Automaton Diagram]
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{cccccc}
\text{a} & \text{b} & \text{a} & \text{b} & \text{c} \\
\end{array}$

$T = \begin{array}{cccccccccccccccccccc}
\text{a} & \text{b} & \text{a} & \text{b} & \text{a} & \text{a} & \text{b} & \text{a} & \text{b} & \text{c} & \text{a} & \text{b} & \text{a} & \text{b} & \text{a} & \text{b} & \text{a} & \text{a} & \text{b} & \text{c} \\
\end{array}$

Diagram:

- Initial state 0
- Transition on 'a' to state 1
- Transition on 'b' to state 2
- Transition on 'a' to state 3
- Transition on 'b' to state 4
- Transition on 'c' to final state 5
- Mismatches occur at states 1, 2, and 3.
2. Automaton Method

Given Pattern $P$, Text $T$, find all occurrences of $P$ in $T$.

$P = \begin{array}{cccccc} a & b & a & b & c \end{array}$

$T = \begin{array}{cccccccccccc} a & b & a & b & a & a & b & a & b & c & a & b & a & b & a & b & a & a & b & c \end{array}$
2. Automaton Method

Given **Pattern** $P$, **Text** $T$, find all occurrences of $P$ in $T$.

$$P = \text{\begin{array}{cccccc} a & b & a & b & c \end{array}}$$

$$T = \text{\begin{array}{cccccccccccccccccccc} a & b & a & b & a & a & b & b & b & c & a & b & a & b & a & b & a & a & a & a & a & b & c \end{array}}$$

→ **Match!**
2. Automaton Method

Given Pattern $P$, how to build the automaton?

$$P = \begin{array}{cccc} 
\text{a} & \text{b} & \text{a} & \text{b} & \text{c} \\
1 & 2 & 3 & 4 & 5 
\end{array}$$

→ for state $k$ and symbol $x$, how to build transition $d(k, x)$?

→ length of the longest proper suffix of $P[1] \ldots P[x]x$ that is prefix of $P$

E.g. $d(4, a) = ?$
2. Automaton Method

Given Pattern P, how to build the automaton?

\[ P = \begin{array}{c}
  1 & 2 & 3 & 4 & 5 \\
  a & b & a & b & c \\
\end{array} \]

→ for state \( k \) and symbol \( x \), how to build transition \( d(k, x) \)?

→ length of the longuest proper suffix of \( P[1] \ldots P[x]x \) that is prefix of \( P \)

E.g. \( d(4, a) = ? \)

\[ P[1]\ldots P[4]a = \]

\[ ababa \]

proper suffix
2. Automaton Method

Given Pattern \( P \), how to build the automaton?

\[ P = \begin{array}{c}
  a & b & a & b & c \\
  1 & 2 & 3 & 4 & 5
\end{array} \]

→ for state \( k \) and symbol \( x \), how to build transition \( d(k,x) \)?

→ length of the \textbf{longest proper suffix} of \( P[1] \ldots P[x]x \) that is \textbf{prefix} of \( P \)

E.g. \( d(4, a) = ? \)

\[ P[1]...P[4]a = \]

\[ \overline{ababa} \]

is also prefix!

proper suffix
2. Automaton Method

Given Pattern \( P \), how to build the automaton?

\[ P = \begin{array}{cccc}
  a & b & a & b & c \\
  1 & 2 & 3 & 4 & 5
\end{array} \]

\[ \rightarrow \text{for state } k \text{ and symbol } x, \text{ how to build transition } d(k, x)? \]

\[ \rightarrow \text{length of the longest proper suffix of } P[1] \ldots P[x]x \text{ that is prefix of } P \]

E.g. \( d(4, a) = 3 = \text{length( aba )} \)

\[ P[1]...P[4]a = \]

\[ \overbrace{ababa}^{\text{proper suffix}} \]

\[ \text{is also prefix!} \]

\[ \text{Lopopre}(u, v) = \text{longest proper suffix of } u \text{ that is prefix of } v \]
Drawback of Automaton Method

→ matching time: $O(n)$  
nice!

→ preprocessing time: $O(m \times |S|)$  
   can be $O(m \times m)$

not so nice... (for large patterns)

→ **Ideally** would like to have

- $O(n)$ matching time  or $O(n + m)$
- $O(m)$ preprocessing time
END

Lecture 12